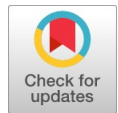


An Empirical Software Reliability Growth Model for Identification of True Failures



Jagadeesh Medapati, Anand Chandulal Jasti, Ranajikanth TV

Abstract: *Software Reliability is a special topic of software engineering that deals with the finding of glitches during the software development. Effective analysis of the reliability helps to understand the quality of the software. It also helps to reveal the number of failures occurred in development phase which facilitates refinement of the failures in the developed software's. If the failures are not minimized the number of reviews in the software development process increases which in turn increase the expenditure to develop the software. Every software organization aims at releasing the software in time and also it becomes a mandate to manage the software such that the time to release the software is optimized. It becomes a mandate for any organization to release software patches so as to minimize the errors after software release and thereby if the number of patches increases, the credibility of the software together with the storage area will be at stake. This article presents a novel case study wherein a procedural layout is presented such that the number of failures can be reduced instantaneously and the failures are identified at the early stage. The development procedure laid in this article helps to formulate a basis for the distinction between true failures and non-failures. The work is presented using benchmark datasets and the results showcase a better recognition rate and failure deduction rate.*

Index Terms: *Gamma Distribution, Quality Metrics, Software Engineering, Software Reliability*

I. INTRODUCTION

Software reliability growth modeling is aimed at using mathematical tools to analyze the failures obtained during the software designing process. This process helps to assess the reliability of software grounded on the developed model and where it takes the generated failure into account and formulates a basis for the identification of the reliability process. These studies help to emphasize the current methodology of the software, describing the Mean Time To Failure (MTTF), Mean Absolute Error (MAE) and understand the Mean Square Error (MSE). Nevertheless, no serious efforts were made to initiate software failures during

the initial development phase to analyze the system together with a process by reducing the failures so that failure-free software can be released just in time. As the number of failures increases, the current study develops different strategies, models and presented various views with the only objective to identify the software failures and to develop the strategies to refine the failures, which are called as review procedures in software firms with a sole purpose to reduce the software failures. If the number of failures increases, then the number of reviews to minimize failures increase substantially is making it difficult for the software to release just-in-time [27]. In the traditional methods of calculating the reliability, the programmers are solely focusing on the failures generated. However, there is no serious effort made in analyzing the failure generated due to some of the internal errors such as network fault, data transmission failure, and other faults at the end output may be tinted as a failure. Overlooking this basic process of analyzing a true failure and an accidental failure, the present traditional systems are evaluating the efficiency of the developed software. In this article the authors try to full fill the gaps and to meet the above two objectives viz., discrimination of true failures and actual failures and identification of the software failures where previous records are not available. This study also suggests an approach wherein the failure rate can be minimized and the true failure is thereby reflected. This approach is completely established on the derived mathematical model based on Exponential Logarithmic Normal Distribution (ELND). The article is categorized as follows: Section 2, Background of the study discusses in depth about the various researches carried out in the field of software reliability. Section 3 of the article presents an overview of the ELND approach and its necessity. Section 4 covers the datasets considered for the study. Section 5 illustrates the methodology of the article, section 6 deals with the experimentation and the results derived thereof. In section 7 of the article, various performance metrics were considered in order to analyze the efficiency of the developed model. In the concluding section 8, the results obtained were discussed.

II. BACKGROUND RESEARCH

To drive the developed software's towards perfection, all software companies try to adopt the policies of software reliability life cycles to develop reliable software. The testing process of software cleared for implementation is generally called as the review. During these reviews, the probability of the failures can be notified.

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If the failure probability is high, steps are to be initiated to substantially bring down the failure rate considerably before releasing the software in to the market.

Many models are demonstrated in the literature by taking this issue and formulating the objectives like developing user-friendly, fully functional software, enhanced capability and ensured maintainability. With these objectives, the software development should be done to prepare failure-free software meeting the user’s requirement. Previously, many models are showcased in the literature that fulfills the objectives of the user requirements. Some of the predominant models in this area of research are coined initially from Hudson [1], by proposing the initial study of software reliability and have published and presented a good number of articles to benefit the potential researchers working in this domain. The research in software testing is further taken into consideration by authors like Jelinski & Moranda model [2], Shooman model [3] and the Littlewood & Verrall model [4]. Jelinski & Moranda model [2] has presented in his article that the errors if at all exeunt are fixed and failure intensity is proportional to the quantity of remaining failures. Shooman model [3] has presented a pictorial view of the failure rates and has thrown an insight to identify that the failure rate may decay during different time intervals. Bayesian method of approach is followed by Littlewood & Verrall model [4] in which the authors have presented a derivation for estimating the effect of failures on the software cost. Yamada and Osaki [5] have executed the works to the next level. According to the authors every failure rate can be shown as a two class discrete time model, where the first model represents the error detection process and the second model is used for estimating the future error. The next level of research work in this direction was initiated by Thoma [6], Brown [7]. In a study carried out by Thoma and Brown estimation of the failure rates was based on measures of dispersions and are restricted to the central limit theorem. Authors have also developed models based on hyper geometric distribution to derive a model which can determine the optimal number of failures from a developed software product. Ohishi et al. [8] have proposed a new method namely Gompertz distribution for estimating the software reliability, this methodology is proven to be a most substantive method for estimation of the failures so far. Research is also carried out not only using the Non-Homogeneous Poisson Processes but other distribution methods like a family of Pareto distribution R. Satya Prasad [9] [10], R.L. Kantham et.al, [11], where the authors have developed new methods to estimate the failure rates and identify the mean time to failure. Latest studies also include works based on Raleigh distribution, Generalized Laplacian distribution, Weibull distribution, and Gaussian distribution. These models are also limited to study of reliability basing on the error rates. Despite of tremendous research in this area, most of the studies demonstrated by the previous authors are confined to the study of the impact of failure rate and few studies tried to project the time between the failures. Efforts to reduce the error rate or to discriminate the true error from the actual error were not found in the literature. This article is aimed to fulfil this objective in a novel approach.

III. EXPONENTIAL LOGARITHMIC NORMAL DISTRIBUTION

Understanding the pattern of the failures is essential to estimate the failures. This analysis of the pattern helps to calculate the true failures and the possible non-failures. For this purpose, numerous models have been discussed in the literature by Hudson [1], Jelinski and Moranda [2], Littlewood and Verrall [4], Pham [12], Michael [13], John [14], Shooman (1972), Goel and Okumoto [15], Ohba [18], [19], Kapur et.al., [20], [21], Kuo et.al., [22], Khan et.al., [23], Sobhana et.al., [24], Sultan [25], Somasundaram and Chinnaiyan [26]. However, these models failed to attribute the analysis of the true failure as it is evident that every initial data in the failure data model assumes exponential distribution. Hence, in this article we have considered Exponential Logarithmic Normal Distribution [27]. The Probability Density Function (PDF) for fitting the ELND is given by.

$$f(p, q) = q(e^{-px}) \text{ If } x > 0; \quad (1)$$

$$= 0 \text{ otherwise.}$$

Where ‘x’ represents the failure.

Here the values of p and q are calculated using the lease square method and by using the formulae:

$$\sum \mu_i = np + q \sum t_i \quad \text{and} \quad (2)$$

$$\sum u_i t_i = p \sum t_i + q \sum t_i^2 \quad (3)$$

IV. DATASETS CONSIDERED

In order to present the proposed methodology, we have considered two datasets namely, TANDEM presented in Woods (1996) and BROOKS AND MOTELY presented in Brooks and Motley (1980) for highlighting the proposed model. The first dataset of TANDEM consists of failure data executed in four releases, Release 1 to Release 4. Each release consists of failures generated. The second dataset containing a failure data set considered for the experimentation is BROOKS AND MOTELY. The datasets used in the proposed model are given below:

Table I: Original Failures in TANDEM Dataset.

| TW | Release 1 | | Release 2 | | Release 3 | | Release 4 | |
|----|-----------|----|-----------|-----|-----------|----|-----------|----|
| | EH | ND | EH | ND | EH | ND | EH | ND |
| 1 | 519 | 16 | 384 | 13 | 162 | 6 | 254 | 1 |
| 2 | 968 | 24 | 1186 | 18 | 499 | 9 | 788 | 3 |
| 3 | 1430 | 27 | 1471 | 26 | 715 | 13 | 1054 | 8 |
| 4 | 1893 | 33 | 2236 | 34 | 1137 | 20 | 1393 | 9 |
| 5 | 2490 | 41 | 2772 | 40 | 1799 | 28 | 2216 | 11 |
| 6 | 3058 | 49 | 2967 | 48 | 2438 | 40 | 2880 | 16 |
| 7 | 3625 | 54 | 3812 | 61 | 2818 | 48 | 3593 | 19 |
| 8 | 4422 | 58 | 4880 | 75 | 3574 | 54 | 4281 | 25 |
| 9 | 5218 | 69 | 6104 | 84 | 4234 | 57 | 5180 | 27 |
| 10 | 5823 | 75 | 6634 | 89 | 4680 | 59 | 6003 | 29 |
| 11 | 6539 | 81 | 7229 | 95 | 4955 | 60 | 7621 | 32 |
| 12 | 7083 | 86 | 8072 | 100 | 5053 | 61 | 8783 | 32 |
| 13 | 7487 | 90 | 8484 | 104 | 9604 | 36 | | |
| 14 | 7846 | 93 | 8847 | 110 | 10064 | 38 | | |



| | | | | | | |
|----|-------|-----|-------|-----|-------|----|
| 15 | 8205 | 96 | 9253 | 112 | 10560 | 39 |
| 16 | 8564 | 98 | 9712 | 114 | 11008 | 39 |
| 17 | 8923 | 99 | 10083 | 117 | 11237 | 41 |
| 18 | 9282 | 100 | 10174 | 118 | 11243 | 42 |
| 19 | 9641 | 100 | 10272 | 120 | 11305 | 42 |
| 20 | 10000 | 100 | | | | |

Labels in the Table I TW constitutes the Test Weeks, EH constitutes the Execution Hours and ND constitutes the Number of defects. Labels in the Table II TW constitutes the Test Weeks, EH constitutes the Execution Hours and AD constitutes the Number of defects.

Table II. Original Failures in BROOKS AND MOTELY Dataset.

| W | EH | A | W | EH | AD | W | EH | AD |
|----|------|----|---|------|------|----|---------|------|
| 1 | 7.25 | 7 | 1 | 417. | 479 | 25 | 1194.68 | 1166 |
| | | | 3 | 94 | | | | |
| 2 | 10.4 | 2 | 1 | 462. | 559 | 26 | 1260.01 | 1184 |
| | | 2 | 9 | 69 | | | | |
| 3 | 17.5 | 6 | 1 | 505. | 624 | 27 | 1327.84 | 1221 |
| | | 1 | 5 | 02 | | | | |
| 4 | 24.8 | 1 | 1 | 580. | 681 | 28 | 1444.76 | 1236 |
| | | 3 | 0 | 02 | | | | |
| | | | 8 | | | | | |
| 5 | 32.0 | 1 | 1 | 642. | 771 | 29 | 1532.84 | 1244 |
| | | 8 | 3 | 85 | | | | |
| | | | 4 | | | | | |
| 6 | 44.6 | 1 | 1 | 716. | 831 | 30 | 1610.92 | 1272 |
| | | 6 | 5 | 43 | | | | |
| | | | 9 | | | | | |
| 7 | 64.5 | 1 | 1 | 759. | 888 | 31 | 1648.84 | 1278 |
| | | 8 | 7 | 18 | | | | |
| | | | 5 | | | | | |
| 8 | 117. | 2 | 2 | 799. | 978 | 32 | 1689.92 | 1283 |
| | | 08 | 2 | 85 | | | | |
| | | | 3 | | | | | |
| 9 | 164. | 2 | 2 | 896. | 1024 | 33 | 1744.42 | 1286 |
| | | 26 | 5 | 6 | | | | |
| | | | 9 | | | | | |
| 10 | 259. | 3 | 2 | 985. | 1081 | 34 | 1807.42 | 1289 |
| | | 36 | 1 | 18 | | | | |
| | | | 2 | | | | | |
| 11 | 315. | 3 | 2 | 1041 | 1110 | 35 | 1846.92 | 1301 |
| | | 11 | 6 | .93 | | | | |
| | | | 9 | | | | | |
| 12 | 374. | 4 | 2 | 1121 | 1150 | | | |
| | | 36 | 0 | .18 | | | | |
| | | | 8 | | | | | |

V. METHODOLOGY

The datasets for the experimentation of the proposed model are presented in the above section. Every dataset is considered for the study and for each dataset initial estimates of the proposed Exponential Logarithmic Normal Distribution parameters p and q are calculated. The values obtained using the Least Square Estimation are presented in Table III:

Table III: Estimated values of parameters p and q for the datasets considered.

| Datasets Considered | p | q |
|---------------------|-----------|-------|
| Tandem Release 1 | 135.845 | 0.078 |
| Tandem Release 2 | 179.573 | 0.063 |
| Tandem Release 3 | 49.339 | 0.237 |
| Tandem Release 4 | 605.941 | 0.005 |
| Brooks and Motely | 11981.548 | 0.004 |

With these values analysis of the proposed model is carried

out. Here the first dataset considered TANDEM containing four releases 1 to 4 is presented along with the second failure dataset BROOKS AND MOTELY in the above Tables I and II. Against each of the dataset, the analysis is conducted in a phased manner wherein the first phase- the true failures are calculated and the experimentation is carried out to reduce the failure rate. Against each of the data released, the number of the actual defects highlighted is considered and using these defects the actual failures are predicted and are presented as below: Labels in Table IV to Table VIII, TW constitutes the Test Weeks, ND constitutes the Number of Defects, PD represents Predicted Defect, RES constitutes the Residual and Fault classifies whether the failure is a true failure or not. In this study, the identified residuals where the actual notified errors are subtracted from the predicted errors and the process carried out on the two datasets namely TANDEM and BROOKS AND MOTELY are tabulated in Table IV to Table XVI. The Fault column in every table indicates the outcome of the proposed model on the datasets and it clearly specifies how best the proposed model has identified the true failures and in turn reduce the failure rate when compared to the original dataset.

Table IV: Actual Failures for TANDEM Dataset Release 1; KURTOSIS = -1.225, STD DEV = 29.2529, $\mu = 69.45$ and $\lambda = 100$.

| Test Week | Execution Hrs. | No. of Defects | Predicted Error (PE) | PDF | PE - PDF |
|-----------|----------------|----------------|----------------------|-----------|-----------|
| 1 | 519 | 16 | 706.05 | 2.08E+14 | 6.676E+22 |
| 2 | 968 | 24 | 722.05 | 2.169E+14 | 9.021E+22 |
| 3 | 1,430 | 27 | 728.05 | 2.203E+14 | 9.154E+22 |
| 4 | 1,893 | 33 | 740.05 | 2.272E+14 | 9.427E+22 |
| 5 | 2,490 | 41 | 756.05 | 2.367E+14 | 9.804E+22 |
| 6 | 3,058 | 49 | 772.05 | 2.465E+14 | 1.02E+23 |
| 7 | 3,625 | 54 | 782.05 | 2.528E+14 | 1.045E+23 |
| 8 | 4,422 | 58 | 790.05 | 2.579E+14 | 1.066E+23 |
| 9 | 5,218 | 69 | 812.05 | 2.724E+14 | 1.125E+23 |
| 10 | 5,823 | 75 | 824.05 | 2.805E+14 | 1.159E+23 |
| 11 | 6,539 | 81 | 836.05 | 2.888E+14 | 1.193E+23 |
| 12 | 7,083 | 86 | 846.05 | 2.959E+14 | 1.223E+23 |
| 13 | 7,487 | 90 | 854.05 | 3.016E+14 | 1.247E+23 |
| 14 | 7,846 | 93 | 860.05 | 3.06E+14 | 1.266E+23 |
| 15 | 8,205 | 96 | 866.05 | 3.104E+14 | 1.285E+23 |
| 16 | 8,564 | 98 | 870.05 | 3.134E+14 | 1.297E+23 |
| 17 | 8,923 | 99 | 872.05 | 3.149E+14 | 1.304E+23 |
| 18 | 9,282 | 100 | 874.05 | 3.164E+14 | 1.31E+23 |
| 19 | 9,641 | 100 | 874.05 | 3.164E+14 | 1.31E+23 |
| 20 | 10,000 | 100 | 874.05 | 3.164E+14 | 1.31E+23 |



Table V: Actual Failures for the TANDEM Dataset Release 2; KURTOSIS =-1.280, STD DEV = 37.3, μ = 77.79 and λ = 120.

| Test Week | Execution Hrs. | No. of Defects | Predicted Error (PE) | PDF | PE – PDF PE |
|-----------|----------------|----------------|----------------------|----------|----------------|
| 1 | 384 | 13 | 1190.061 | 1.55E+15 | 1.70E+24 |
| 2 | 1,186 | 18 | 1200.061 | 1.57E+15 | 1.72E+24 |
| 3 | 1,471 | 26 | 1216.061 | 1.61E+15 | 1.76E+24 |
| 4 | 2,236 | 34 | 1232.061 | 1.66E+15 | 1.81E+24 |
| 5 | 2,772 | 40 | 1244.061 | 1.69E+15 | 1.84E+24 |
| 6 | 2,967 | 48 | 1260.061 | 1.73E+15 | 1.88E+24 |
| 7 | 3,812 | 61 | 1286.061 | 1.80E+15 | 1.96E+24 |
| 8 | 4,880 | 75 | 1314.061 | 1.88E+15 | 2.05E+24 |
| 9 | 6,104 | 84 | 1332.061 | 1.93E+15 | 2.10E+24 |
| 10 | 6,634 | 89 | 1342.061 | 1.96E+15 | 2.13E+24 |
| 11 | 7,229 | 95 | 1354.061 | 2.00E+15 | 2.17E+24 |
| 12 | 8,072 | 100 | 1364.061 | 2.03E+15 | 2.21E+24 |
| 13 | 8,484 | 104 | 1372.061 | 2.05E+15 | 2.23E+24 |
| 14 | 8,847 | 110 | 1384.061 | 2.09E+15 | 2.27E+24 |
| 15 | 9,253 | 112 | 1388.061 | 2.10E+15 | 2.29E+24 |
| 16 | 9,712 | 114 | 1392.061 | 2.11E+15 | 2.30E+24 |
| 17 | 10,083 | 117 | 1398.061 | 2.13E+15 | 2.32E+24 |
| 18 | 10,174 | 118 | 1400.061 | 2.14E+15 | 2.33E+24 |
| 19 | 10,272 | 120 | 1404.061 | 2.15E+15 | 2.34E+24 |

Table VI: Actual Failures for the TANDEM Dataset Release 3; KURTOSIS =-0.459, STD DEV = 16.883, μ = 38.526 and λ = 42.

| Test Week | Execution Hrs. | No. of Defects | Predicted Error (PE) | PDF | PE – PDF PE |
|-----------|----------------|----------------|----------------------|-------------|----------------|
| 1 | 162 | 6 | -51.048 | 2.94886E+12 | 3.33699E+21 |
| 2 | 499 | 9 | -47.337 | 2.21329E+12 | 2.18616E+21 |
| 3 | 715 | 13 | -42.389 | 1.45757E+12 | 1.18239E+21 |
| 4 | 1,137 | 20 | -33.730 | 6.19326E+11 | 3.37142E+20 |
| 5 | 1,799 | 28 | -23.834 | 1.73314E+11 | 5.28792E+19 |
| 6 | 2,438 | 40 | -8.990 | 6358282047 | 5.00248E+17 |
| 7 | 2,818 | 48 | 0.906 | 2686956.251 | 8.79047E+12 |
| 8 | 3,574 | 54 | 8.328 | 394506986.8 | 2.24388E+15 |
| 9 | 4,234 | 57 | 12.039 | 2879255046 | 5.71953E+16 |
| 10 | 4,680 | 59 | 14.513 | 7281596606 | 2.51723E+17 |
| 11 | 4,955 | 60 | 15.750 | 10797670257 | 4.69986E+17 |
| 12 | 5,053 | 61 | 16.987 | 15455443389 | 8.27782E+17 |
| 13 | 9,604 | 36 | -13.938 | 26462530861 | 3.60478E+18 |
| 14 | 10,064 | 38 | -11.464 | 13817749287 | 1.45285E+18 |
| 15 | 10,560 | 39 | -10.227 | 9551078809 | 8.72229E+17 |
| 16 | 11,008 | 39 | -10.227 | 9551078809 | 8.72229E+17 |
| 17 | 11,237 | 41 | -7.753 | 4041980208 | 2.71818E+17 |
| 18 | 11,243 | 42 | -6.516 | 2424855358 | 1.38498E+17 |
| 19 | 11,305 | 42 | -6.516 | 2424855358 | 1.38498E+17 |

Table VII: Actual Failures for the TANDEM Dataset Release 4; KURTOSIS =-1.556, STD DEV = 11.243, μ = 17.666 and λ = 32.

| Test Week | Execution Hrs. | No. of Defects | Predicted Error (PE) | PDF | PE – PDF PE |
|-----------|----------------|----------------|----------------------|----------|----------------|
| 1 | 254 | 1 | -605.024 | 2.68E+25 | 1.95983E+45 |
| 2 | 788 | 3 | -603.014 | 2.64E+25 | 1.92134E+45 |
| 3 | 1,054 | 8 | -597.989 | 2.56E+25 | 1.82785E+45 |
| 4 | 1,393 | 9 | -596.984 | 2.54E+25 | 1.80961E+45 |
| 5 | 2,216 | 11 | -594.974 | 2.51E+25 | 1.7736E+45 |
| 6 | 2,880 | 16 | -589.949 | 2.42E+25 | 1.68616E+45 |
| 7 | 3,593 | 19 | -586.934 | 2.37E+25 | 1.63545E+45 |
| 8 | 4,281 | 25 | -580.904 | 2.28E+25 | 1.53783E+45 |
| 9 | 5,180 | 27 | -578.894 | 2.25E+25 | 1.50638E+45 |
| 10 | 6,003 | 29 | -576.884 | 2.22E+25 | 1.47548E+45 |
| 11 | 7,621 | 32 | -573.869 | 2.17E+25 | 1.43012E+45 |
| 12 | 8,783 | 32 | -573.869 | 2.17E+25 | 1.43012E+45 |

Table VIII: Actual Failures for the BROOKS AND MOTLEY Dataset. KURTOSIS =-1.577, STD DEV = 468.221, μ = 748 and λ = 1301.

| Test Week | Execution Hrs. | No. of Defects | Predicted Error (PE) | PDF | PE – PDF PE |
|-----------|----------------|----------------|----------------------|----------|----------------|
| 1 | 7.25 | 7 | -11978 | 1.25E+31 | 1.1E+54 |
| 2 | 10.42 | 29 | -11955 | 1.25E+31 | 1.09E+54 |
| 3 | 17.5 | 61 | -11923 | 1.23E+31 | 1.07E+54 |
| 4 | 24.83 | 108 | -11876 | 1.21E+31 | 1.04E+54 |
| 5 | 32.08 | 134 | -11850 | 1.20E+31 | 1.03E+54 |
| 6 | 44.66 | 159 | -11825 | 1.19E+31 | 1.02E+54 |
| 7 | 64.58 | 175 | -11809 | 1.19E+31 | 1.01E+54 |
| 8 | 117.08 | 223 | -11761 | 1.17E+31 | 9.84E+53 |
| 9 | 164.26 | 259 | -11725 | 1.15E+31 | 9.66E+53 |
| 10 | 259.36 | 312 | -11671 | 1.13E+31 | 9.4E+53 |
| 11 | 315.11 | 369 | -11614 | 1.11E+31 | 9.13E+53 |
| 12 | 374.36 | 408 | -11575 | 1.10E+31 | 8.95E+53 |
| 13 | 417.94 | 479 | -11504 | 1.07E+31 | 8.63E+53 |
| 14 | 462.69 | 559 | -11423 | 1.04E+31 | 8.27E+53 |
| 15 | 505.02 | 624 | -11358 | 1.02E+31 | 8E+53 |
| 16 | 580.02 | 681 | -11301 | 9.95E+30 | 7.76E+53 |
| 17 | 642.85 | 771 | -11210 | 9.64E+30 | 7.39E+53 |
| 18 | 716.43 | 831 | -11150 | 9.44E+30 | 7.16E+53 |
| 19 | 759.18 | 888 | -11093 | 9.24E+30 | 6.94E+53 |
| 20 | 799.85 | 978 | -11003 | 8.95E+30 | 6.61E+53 |
| 21 | 896.6 | 1024 | -10956 | 8.80E+30 | 6.45E+53 |
| 22 | 985.18 | 1081 | -10899 | 8.62E+30 | 6.25E+53 |
| 23 | 1041.93 | 1110 | -10870 | 8.53E+30 | 6.15E+53 |

| | | | | | |
|----|---------|------|--------|----------|----------|
| 24 | 1121.18 | 1150 | -10830 | 8.40E+30 | 6.02E+53 |
| 25 | 1194.68 | 1166 | -10814 | 8.35E+30 | 5.96E+53 |
| 26 | 1260.01 | 1184 | -10796 | 8.30E+30 | 5.91E+53 |
| 27 | 1327.84 | 1221 | -10759 | 8.18E+30 | 5.79E+53 |
| 28 | 1444.76 | 1236 | -10744 | 8.14E+30 | 5.74E+53 |
| 29 | 1532.84 | 1244 | -10736 | 8.11E+30 | 5.71E+53 |
| 30 | 1610.92 | 1272 | -10707 | 8.03E+30 | 5.62E+53 |
| 31 | 1648.84 | 1278 | -10701 | 8.01E+30 | 5.6E+53 |
| 32 | 1689.92 | 1283 | -10696 | 8.00E+30 | 5.59E+53 |
| 33 | 1744.42 | 1286 | -10693 | 7.99E+30 | 5.58E+53 |
| 34 | 1807.42 | 1289 | -10690 | 7.98E+30 | 5.57E+53 |
| 35 | 1846.92 | 1301 | -10678 | 7.94E+30 | 5.53E+53 |

Table IX: Goodness of fit statistics for the TANDEM Datasets and BROOKS AND MOTELY Dataset.

| Datasets Considered | Statistic | Independent | Full |
|---------------------|--------------------|-------------|--------------|
| TANDEM R1 | -2 Log(Likelihood) | 42.04619255 | -1.270866512 |
| | AIC | 46.04619255 | 4.729133488 |
| | SBC | 48.0376571 | 7.716330309 |
| TANDEM R2 | -2 Log(Likelihood) | 43.80049811 | 3.261328331 |
| | AIC | 47.80049811 | 9.261328331 |
| | SBC | 49.68937607 | 12.09464527 |
| TANDEM R3 | -2 Log(Likelihood) | 39.65728411 | -2.536318299 |
| | AIC | 43.65728411 | 3.463681701 |
| | SBC | 45.54616206 | 6.296998639 |
| TANDEM R4 | -2 Log(Likelihood) | 34.03443602 | 21.5696264 |
| | AIC | 38.03443602 | 27.5696264 |
| | SBC | 39.00424932 | 29.02434635 |
| BROOKS AND MOTELY | -2 Log(Likelihood) | 101.0392227 | 75.08236094 |
| | AIC | 105.0392227 | 81.08236094 |
| | SBC | 108.1499189 | 85.74840513 |
| | AICC | 105.4142227 | 81.85655449 |

Table X: Test of the null hypothesis H0: beta=0 for TANDEM Datasets and BROOKS AND MOTELY Dataset.

| Datasets Considered | Statistic | DF | Chi-square |
|---------------------|--------------------|----|-------------|
| TANDEM R1 | -2 Log(Likelihood) | 1 | 43.31705906 |
| | Score | 1 | 10782.16663 |
| | Wald | 1 | 315.2263742 |
| TANDEM R2 | -2 Log(Likelihood) | 1 | 40.53916978 |
| | Score | 1 | 6753.258705 |
| | Wald | 1 | 210.4971408 |
| TANDEM R3 | -2 Log(Likelihood) | 1 | 42.1936024 |

| | | | |
|-------------------|--------------------|---|-------------|
| TANDEM R4 | Score | 1 | 8298.533324 |
| | Wald | 1 | 596.7414912 |
| | -2 Log(Likelihood) | 1 | 12.46480962 |
| BROOKS AND MOTELY | Score | 1 | 450.2293414 |
| | Wald | 1 | 29.1319165 |
| | -2 Log(Likelihood) | 1 | 25.95686181 |
| | Score | 1 | 12010.51314 |
| | Wald | 1 | 48.3723997 |

Table XI: Regression coefficients for TANDEM Datasets and BROOKS AND MOTELY Dataset.

| Datasets Considered | Variable | Value | Standard Error | Wald Chi-Square |
|---------------------|-----------|-------|----------------|-----------------|
| TANDEM R1 | Intercept | 3.171 | 0.058 | 3015.252 |
| | Test Week | 0.112 | 0.007 | 274.739 |
| | Scale | 0.179 | 0.051 | 12.460 |
| TANDEM R2 | Intercept | 3.035 | -Inf | -Inf |
| | Test Week | 0.145 | -Inf | -Inf |
| | Scale | 0.262 | -Inf | -Inf |
| TANDEM R3 | Intercept | 1.802 | 0.145 | 153.863 |
| | Test Week | 0.264 | 0.023 | 127.997 |
| | Scale | 0.213 | 0.047 | 20.176 |
| TANDEM R4 | Intercept | 0.785 | 0.329 | 5.689 |
| | Test Week | 0.268 | 0.050 | 29.132 |
| | Scale | 1.044 | -Inf | -Inf |
| BROOKS AND MOTELY | Intercept | 4.324 | 0.277 | 244.392 |
| | Test Week | 0.104 | 0.015 | 48.372 |
| | Scale | 1.479 | -Inf | -Inf |

Table XII: Predictions and Residuals for the TANDEM Dataset Release 1.

| No. of Def ects | Residuals | Cox-Snell Residuals | Cumulative Distributions | Hazard Function | Survival Distribution Function | Failure (YES/NO) |
|-----------------|-----------|---------------------|--------------------------|-----------------|--------------------------------|------------------|
| 16 | -0.511 | 0.600 | 0.451 | 0.329 | 0.549 | Y |
| 24 | -0.218 | 0.804 | 0.553 | 0.360 | 0.447 | Y |
| 27 | -0.213 | 0.809 | 0.554 | 0.360 | 0.446 | Y |
| 33 | -0.124 | 0.883 | 0.587 | 0.365 | 0.413 | Y |
| 41 | -0.019 | 0.981 | 0.625 | 0.368 | 0.375 | Y |
| 49 | 0.047 | 1.048 | 0.649 | 0.367 | 0.351 | N |
| 54 | 0.031 | 1.032 | 0.644 | 0.368 | 0.356 | N |
| 58 | -0.009 | 0.991 | 0.629 | 0.368 | 0.371 | Y |
| 69 | 0.052 | 1.053 | 0.651 | 0.367 | 0.349 | N |
| 75 | 0.023 | 1.023 | 0.641 | 0.368 | 0.359 | N |
| 81 | -0.012 | 0.988 | 0.628 | 0.368 | 0.372 | Y |
| 86 | -0.065 | 0.937 | 0.608 | 0.367 | 0.392 | Y |

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| | | | | | | | | | | | | | |
|-----|--------|-------|-------|-------|-------|---|----|--------|-------|-------|-------|-------|---|
| 90 | -0.132 | 0.877 | 0.584 | 0.365 | 0.416 | Y | 42 | -3.086 | 0.046 | 0.045 | 0.044 | 0.955 | Y |
| 93 | -0.211 | 0.810 | 0.555 | 0.360 | 0.445 | Y | 48 | 0.219 | 1.245 | 0.712 | 0.358 | 0.288 | N |
| 96 | -0.292 | 0.747 | 0.526 | 0.354 | 0.474 | Y | 54 | 0.073 | 1.076 | 0.659 | 0.367 | 0.341 | N |
| 98 | -0.383 | 0.682 | 0.494 | 0.345 | 0.506 | Y | 57 | -0.137 | 0.872 | 0.582 | 0.365 | 0.418 | Y |
| 99 | -0.485 | 0.615 | 0.460 | 0.333 | 0.540 | Y | 59 | -0.367 | 0.693 | 0.500 | 0.347 | 0.500 | Y |
| 100 | -0.588 | 0.556 | 0.426 | 0.319 | 0.574 | Y | 60 | -0.615 | 0.541 | 0.418 | 0.315 | 0.582 | Y |
| 100 | -0.700 | 0.497 | 0.391 | 0.302 | 0.609 | Y | 61 | -0.862 | 0.422 | 0.344 | 0.277 | 0.656 | Y |

Table XIII: Predictions and Residuals for the TANDEM Dataset Release 2.

| No. of Defects | Residuals | Cox-Snell Residuals | Cumulative Distributions | Hazard Function | Survival Distribution Function | Failure (YES/NO) |
|----------------|-----------|---------------------|--------------------------|-----------------|--------------------------------|------------------|
| 13 | -0.614 | 0.541 | 0.418 | 0.315 | 0.582 | Y |
| 18 | -0.434 | 0.648 | 0.477 | 0.339 | 0.523 | Y |
| 26 | -0.211 | 0.810 | 0.555 | 0.360 | 0.445 | Y |
| 34 | -0.088 | 0.916 | 0.600 | 0.367 | 0.400 | Y |
| 40 | -0.070 | 0.932 | 0.606 | 0.367 | 0.394 | Y |
| 48 | -0.033 | 0.968 | 0.620 | 0.368 | 0.380 | Y |
| 61 | 0.062 | 1.064 | 0.655 | 0.367 | 0.345 | N |
| 75 | 0.124 | 1.132 | 0.678 | 0.365 | 0.322 | N |
| 84 | 0.092 | 1.097 | 0.666 | 0.366 | 0.334 | N |
| 89 | 0.005 | 1.005 | 0.634 | 0.368 | 0.366 | N |
| 95 | -0.074 | 0.929 | 0.605 | 0.367 | 0.395 | Y |
| 100 | -0.168 | 0.846 | 0.571 | 0.363 | 0.429 | Y |
| 104 | -0.273 | 0.761 | 0.533 | 0.356 | 0.467 | Y |
| 110 | -0.362 | 0.696 | 0.502 | 0.347 | 0.498 | Y |
| 112 | -0.489 | 0.613 | 0.458 | 0.332 | 0.542 | Y |
| 114 | -0.616 | 0.540 | 0.417 | 0.315 | 0.583 | Y |
| 117 | -0.735 | 0.479 | 0.381 | 0.297 | 0.619 | Y |
| 118 | -0.871 | 0.418 | 0.342 | 0.275 | 0.658 | Y |
| 120 | -0.999 | 0.368 | 0.308 | 0.255 | 0.692 | Y |

Table XIV: Predictions and Residuals for the TANDEM Dataset Release 3.

| No. of Defects | Residuals | Cox-Snell Residuals | Cumulative Distributions | Hazard Function | Survival Distribution Function | Failure (YES/NO) |
|----------------|-----------|---------------------|--------------------------|-----------------|--------------------------------|------------------|
| 6 | -0.274 | 0.760 | 0.532 | 0.355 | 0.468 | Y |
| 9 | -0.133 | 0.875 | 0.583 | 0.365 | 0.417 | Y |
| 13 | -0.030 | 0.971 | 0.621 | 0.368 | 0.379 | Y |
| 20 | 0.137 | 1.147 | 0.682 | 0.364 | 0.318 | N |
| 28 | 0.209 | 1.233 | 0.708 | 0.359 | 0.292 | N |
| 36 | -1.654 | 0.191 | 0.174 | 0.158 | 0.826 | Y |
| 38 | -1.864 | 0.155 | 0.144 | 0.133 | 0.856 | Y |
| 39 | -2.103 | 0.122 | 0.115 | 0.108 | 0.885 | Y |
| 39 | -2.367 | 0.094 | 0.090 | 0.085 | 0.910 | Y |
| 40 | 0.301 | 1.352 | 0.741 | 0.350 | 0.259 | N |
| 41 | -2.581 | 0.076 | 0.073 | 0.070 | 0.927 | Y |
| 42 | -2.821 | 0.060 | 0.058 | 0.056 | 0.942 | Y |

Table XV: Predictions and Residuals for the TANDEM Dataset Release 4.

| No. of Defects | Residuals | Cox-Snell Residuals | Cumulative Distributions | Hazard Function | Survival Distribution Function | Failure (YES/NO) |
|----------------|-----------|---------------------|--------------------------|-----------------|--------------------------------|------------------|
| 1 | -1.053 | 0.349 | 0.295 | 0.246 | 0.705 | Y |
| 3 | -0.222 | 0.801 | 0.551 | 0.360 | 0.449 | Y |
| 8 | 0.491 | 1.634 | 0.805 | 0.319 | 0.195 | N |
| 9 | 0.341 | 1.407 | 0.755 | 0.345 | 0.245 | N |
| 11 | 0.274 | 1.315 | 0.732 | 0.353 | 0.268 | N |
| 16 | 0.381 | 1.464 | 0.769 | 0.339 | 0.231 | N |
| 19 | 0.285 | 1.330 | 0.736 | 0.352 | 0.264 | N |
| 25 | 0.292 | 1.339 | 0.738 | 0.351 | 0.262 | N |
| 27 | 0.101 | 1.107 | 0.669 | 0.366 | 0.331 | N |
| 29 | -0.095 | 0.909 | 0.597 | 0.366 | 0.403 | Y |
| 32 | -0.264 | 0.768 | 0.536 | 0.356 | 0.464 | Y |
| 32 | -0.532 | 0.587 | 0.444 | 0.326 | 0.556 | Y |

Table XVI: Predictions and Residuals for Brooks and Motley Dataset.

| No. of Defects | Residuals | Cox-Snell Residuals | Cumulative Distributions | Hazard Function | Survival Distribution Function | Failure (YES/NO) |
|----------------|-----------|---------------------|--------------------------|-----------------|--------------------------------|------------------|
| 7 | -2.482 | 0.084 | 0.080 | 0.077 | 0.920 | Y |
| 29 | -1.164 | 0.312 | 0.268 | 0.228 | 0.732 | Y |
| 61 | -0.524 | 0.592 | 0.447 | 0.327 | 0.553 | Y |
| 108 | -0.057 | 0.945 | 0.611 | 0.367 | 0.389 | Y |
| 134 | 0.055 | 1.056 | 0.652 | 0.367 | 0.348 | N |
| 159 | 0.122 | 1.130 | 0.677 | 0.365 | 0.323 | N |
| 175 | 0.114 | 1.121 | 0.674 | 0.365 | 0.326 | N |
| 223 | 0.252 | 1.287 | 0.724 | 0.355 | 0.276 | N |
| 259 | 0.298 | 1.347 | 0.740 | 0.350 | 0.260 | N |
| 312 | 0.380 | 1.463 | 0.768 | 0.339 | 0.232 | N |
| 369 | 0.444 | 1.559 | 0.790 | 0.328 | 0.210 | N |
| 408 | 0.441 | 1.554 | 0.789 | 0.329 | 0.211 | N |
| 479 | 0.497 | 1.644 | 0.807 | 0.318 | 0.193 | N |
| 559 | 0.548 | 1.730 | 0.823 | 0.307 | 0.177 | N |
| 624 | 0.554 | 1.740 | 0.825 | 0.305 | 0.175 | N |

| | | | | | | |
|------|--------|-------|-------|-------|-------|---|
| 681 | 0.537 | 1.712 | 0.819 | 0.309 | 0.181 | N |
| 771 | 0.558 | 1.747 | 0.826 | 0.305 | 0.174 | N |
| 831 | 0.529 | 1.697 | 0.817 | 0.311 | 0.183 | N |
| 888 | 0.491 | 1.634 | 0.805 | 0.319 | 0.195 | N |
| 978 | 0.484 | 1.622 | 0.803 | 0.320 | 0.197 | N |
| 1024 | 0.426 | 1.531 | 0.784 | 0.331 | 0.216 | N |
| 1081 | 0.376 | 1.457 | 0.767 | 0.339 | 0.233 | N |
| 1110 | 0.299 | 1.348 | 0.740 | 0.350 | 0.260 | N |
| 1150 | 0.230 | 1.259 | 0.716 | 0.357 | 0.284 | N |
| 1166 | 0.140 | 1.150 | 0.683 | 0.364 | 0.317 | N |
| 1184 | 0.051 | 1.053 | 0.651 | 0.367 | 0.349 | N |
| 1221 | -0.022 | 0.979 | 0.624 | 0.368 | 0.376 | Y |
| 1236 | -0.113 | 0.893 | 0.590 | 0.366 | 0.410 | Y |
| 1244 | -0.211 | 0.810 | 0.555 | 0.360 | 0.445 | Y |
| 1272 | -0.293 | 0.746 | 0.526 | 0.354 | 0.474 | Y |
| 1278 | -0.392 | 0.676 | 0.491 | 0.344 | 0.509 | Y |
| 1283 | -0.492 | 0.612 | 0.458 | 0.332 | 0.542 | Y |
| 1286 | -0.593 | 0.552 | 0.424 | 0.318 | 0.576 | Y |
| 1289 | -0.695 | 0.499 | 0.393 | 0.303 | 0.607 | Y |
| 1301 | -0.790 | 0.454 | 0.365 | 0.288 | 0.635 | Y |

VI. PERFORMANCE EVALUATION METRICS

To assess the outputs derived from the proposed model, we have considered the metrics such as Mean Squared Error (MSE), R2, Sum of Squares Error (SSE) and Root Mean Squared Error (RMSE). The formulas for the calculation of the above metrics are appended below:

Mean Squared Error

$$MSE = \frac{\sum(|Actual Failure_i - Estimated Failure_i|)^2}{n-1} \quad (4)$$

Mean Absolute Percent Error

$$MAPE = \frac{\sum \frac{|Actual Failure_i - Estimated Failure_i|}{Actual Failure_i} \times 100}{n} \quad (5)$$

Error of Sum of Squares

$$SSE = \sum_{i=1}^n (x_i - \bar{x})^2 \quad (6)$$

Coefficient of Determination

$$R^2 = 1 - \frac{SSE_{res}}{SSE_{tot}} \quad (7)$$

Root Mean Square Error

$$RMSE = \sqrt{\frac{\sum(|Actual Failure_i - Estimated Failure_i|)^2}{n-1}} \quad (8)$$

The results of the performance evaluation metrics are presented in the following Table XVII.

Table XVII: Comparison of Performance Evaluation Metrics.

| Dataset | MSE | R ² | SSE | RMSE |
|---------|-----|----------------|-----|------|
|---------|-----|----------------|-----|------|

| Considered | | | | |
|-------------------|----------|-------|------------|--------|
| Tandem R1 | 11.317 | 0.988 | 192.388 | 3.364 |
| Tandem R2 | 26.088 | 0.982 | 417.408 | 5.108 |
| Tandem R3 | 116.630 | 0.664 | 1866.081 | 10.800 |
| Tandem R4 | 3.861 | 0.980 | 34.749 | 1.965 |
| Brooks and Motely | 9659.621 | 0.966 | 309107.871 | 98.283 |

Table XVII clearly shows that the MSE is less for the Release 1 and the R² is almost coming to 1, which indicates that the model performs better. The SSE and RMSE metrics also showcase significant measures. This demonstrates that the proposed methodology is delivering an outstanding performance in predicting the failures.

VII. EXPERIMENTATION

The experimentation conducted across the two datasets viz., TANDEM and BROOKS AND MOTELY was represented graphically as shown in Figures 1 to Figure 5.

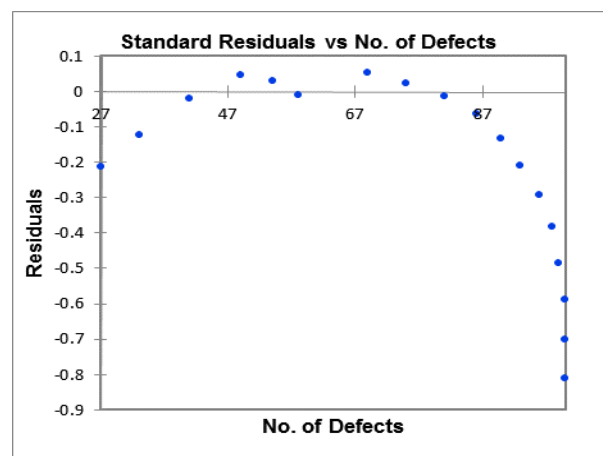


Fig. 1: Standard Residuals versus Number of Defects for the TANDEM Dataset Release 1.

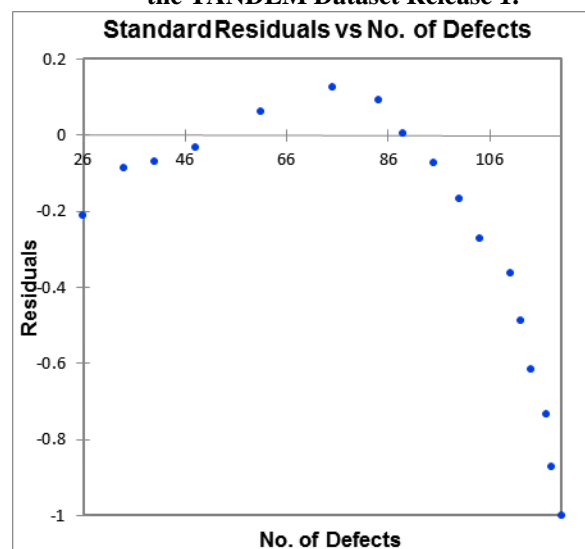


Fig. 2: Standard Residuals versus Number of Defects for the TANDEM Dataset Release 2.



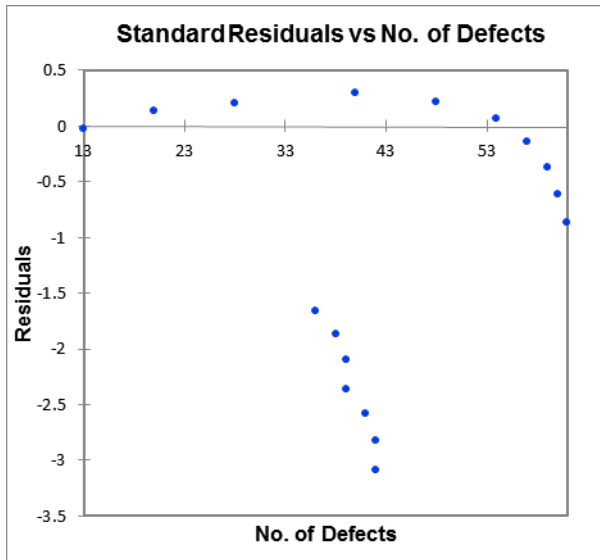


Fig. 3: Standard Residuals versus Number of Defects for the TANDEM Dataset Release 3.

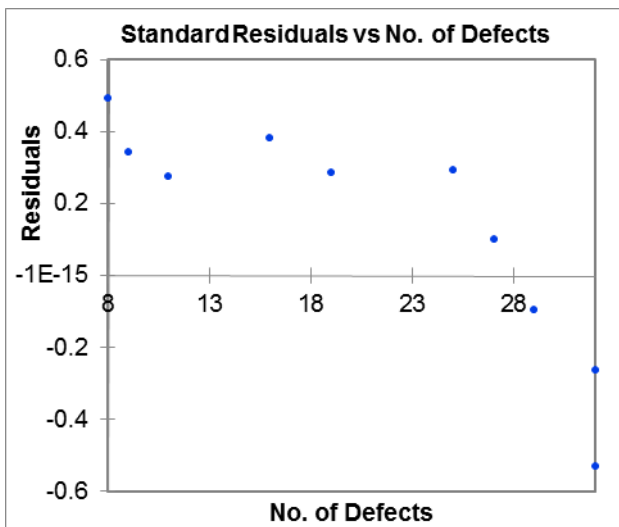


Fig. 4: Standard Residuals versus Number of Defects for the TANDEM Dataset Release 4.

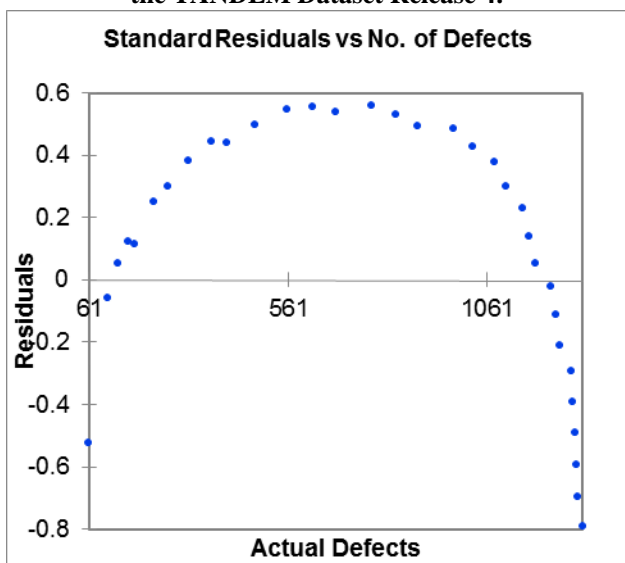


Fig. 5: Standard Residuals versus Number of Defects for the Brooks and Motley Dataset.

VIII. CONCLUSION

In this article a novel methodology has been presented to minimize the number of failures and also for helping the software developers to understand the actual failures that are derived from the project due to technical flaws and also underlined the predicted failures, which are not the failures but reported as failures due to the technical issues or human failures. The results presented in this article on two benchmark datasets helps to understand the potentiality of the model. The results also attribute the significance of the model which can be applied in a software firm to reduce the review times and also to release the software just in time along with increased the profits.

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