

Forms of supra $g^\# \alpha$ - Continuous Functions

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Abstract: This paper encompasses and particularly throws light on the new classes of functions called strongly supra $g^\# \alpha$ -Continuous and perfectly supra $g^\# \alpha$ - continuous functions and to analyze some of the unique properties and relations amid them. Subsequently, the conception of almost supra $g^\# \alpha$ -continuous function is also conferred and the relationship of these functions with other functions were investigated and portrayed. Furthermore, a mildly supra $g^\# \alpha$ -normal space have been defined and analyzed.

Keywords : supra $g^\# \alpha$ -closed (open) sets, supra $g^\# \alpha$ -continuous, supra $g^\# \alpha$ -irresolute, strongly supra $g^\# \alpha$ -continuous and perfectly supra $g^\# \alpha$ -continuous and almost supra $g^\# \alpha$ -continuous function.

I. INTRODUCTION

The concept Supra topological spaces and studied S-continuous maps and S^* -continuous maps was introduced by Mashhour et al [2] in 1983. Moreover, in 2008, Devi et al. [1] initiated and studied a class of sets called supra α -open and a class of maps called $s\alpha$ -continuous maps between topological spaces, respectively. In addition to in 2011, G.Ramkumar et al [3] explored Supra g -Closed set and supra g -continuity maps.

In lieu with the above concept, Kokilavani and Bhuvanewari have introduced and investigated supra $g^\# \alpha$ -closed sets and supra $g^\# \alpha$ continuous functions. Subsequently in this paper we tend to introduce strongly supra $g^\# \alpha$ -continuous and perfectly supra $g^\# \alpha$ -continuous functions and also we have arrived a concept of almost supra $g^\# \alpha$ -continuous function and further investigated the relationship with other functions in supra topological spaces. Finally, a new type of normal space called mildly supra $g^\# \alpha$ -normal space is also defined and its properties have been investigated.

II. PRELIMINARIES

Definition: 2.1[5] A subfamily of μ of X is said to be a supra topology on X , if (i) $X, \phi \in \mu$

(ii) if $A_i \in \mu$ for all $i \in J$ then $\cup A_i \in \mu$.

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The pair (X, μ) is called supra topological space. The elements of μ are called supra open sets in (X, μ) and complement of a supra open set is called a supra closed set.

Definition: 2.2[5] (i) The supra closure of a set A is denoted by $cl^\mu(A)$ and is defined as

$$cl^\mu(A) = \cap \{B : B \text{ is a supra closed set and } A \subseteq B\}.$$

(ii) The supra interior of a set A is denoted by $int^\mu(A)$ and defined as

$$int^\mu(A) = \cup \{B : B \text{ is a supra open set and } A \supseteq B\}.$$

Definition: 2.3[5] Let (X, τ) be a topological spaces and μ be a supra topology on X . We call μ a supra topology associated with τ if $\tau \subset \mu$.

Definition: 2.4 [2] Let (X, μ) be a supra topological space. A Subset A of X is called supra α -open set if $A \subseteq int^\mu(cl^\mu(int^\mu(A)))$. The complement of supra α -open set is supra α -closed set.

Definition: 2.5 [5] Let (X, μ) be a supra topological space. A Subset A of X is called g -closed set if $cl^\mu(A) \subseteq U$, whenever $A \subseteq U$ and U is supra open set of X .

Definition: 2.6 [5] Let (X, μ) be a supra topological space. A Subset A of X is called gs -closed set if $scl^\mu(A) \subseteq U$ whenever $A \subseteq U$ and U is supra open set of X .

Definition: 2.7[6] Let (X, μ) be a supra topological space. A Subset A of X is called supra g^* -closed set if $cl^\mu(A) \subseteq U$ whenever $A \subseteq U$ and U is supra g -open set of X . The complement of

supra g^* - closed set is supra g^* - open set.

Definition: 2.8[6] Let (X, μ) be a supra topological space. A Subset A of X is called supra αg - closed set if $\alpha cl^{\mu}(A) \subseteq U$, whenever $A \subseteq U$ and U is open set of X .

Definition: 2.9[3] Let (X, μ) be a supra topological space. A Subset A of X is called supra $g^{\#}\alpha$ -closed set if $\alpha cl^{\mu}(A) \subseteq U$, whenever $A \subseteq U$ and U is supra g - open set of X . The

complement of supra $g^{\#}\alpha$ - closed set is called supra $g^{\#}\alpha$ -open set.

Definition 2.10[9] Let (X, μ) be a supra topological space. A set A of X is called supra regular open if $A = int^{\mu}(cl^{\mu}(A))$ and supra regular closed if $A = cl^{\mu}(int^{\mu}(A))$.

Definition: 2.11 Let (X, μ) and (Y, σ) be two topological spaces and $\tau \subset \mu$. A map $f: (X, \tau) \rightarrow (Y, \sigma)$ is called

(i) supra continuous [2] if the inverse image of each open set of Y is a supra open set in X .

(ii) supra α -continuous [2] if the inverse image of each open set of Y is a supra α -open set in X .

(iii) supra g -continuous [6] if the inverse image of each closed set of Y is a supra g -closed set in X .

(iv) Supra gs -continuous [6] if the inverse image of each closed set of Y is a supra gs -closed set in X .

(v) Supra αg -continuous [7] if the inverse image of each closed set of Y is a supra αg -closed set in X .

Definition: 2.12 Let (X, μ) and (Y, σ) be two topological spaces and $\tau \subset \mu$. A map

$f: (X, \tau) \rightarrow (Y, \sigma)$ is called

(i) Supra closed [2] if the image of each closed set of X is a supra closed set in Y .

(ii) Supra α -closed [2] if the image of each closed set of X is a supra α -closed set in Y .

(iii) Supra g -closed [5] if the image of each closed set of X is a supra g -closed set in Y .

(iv) Supra gs -closed [3] if the image of each closed set of X is a supra gs -closed set in Y .

(v) Supra αg -closed [4] if the image of each closed set of X is a supra αg -closed set in Y .

(vi) supra regular open [7], if $int^{\mu} cl^{\mu}(A)$ The complement of the above mentioned sets are their respective open and closed sets and vice-versa.

Definition 2.13 Let (X, μ) and (Y, σ) be two topological spaces and $\tau \subset \mu$. A map

$f: (X, \tau) \rightarrow (Y, \sigma)$ is called

(i) Supra irresolute [3] if $f^{-1}(V)$ is supra closed in X for every supra closed set V of Y .

(ii) Supra α -irresolute [7] if $f^{-1}(V)$ is supra α -closed in X for every supra α -closed set V of Y .

(iii) Supra αg -irresolute [4] if $f^{-1}(V)$ is supra αg -closed in X for every supra αg -closed set V of Y .

Definition: 2.14[3] Let (X, τ) and (Y, σ) be two topological spaces and μ be an associated supra topology with τ . A function $f: (X, \tau) \rightarrow (Y, \sigma)$ is called supra $g^{\#}\alpha$ - Continuous if $f^{-1}(V)$ is $g^{\#}\alpha$ -closed in (X, μ) for every closed set V of (Y, σ) .

Definition: 2.15 [3] Let (X, τ) and (Y, σ) be two topological spaces and μ be an associated supra topology with τ . A function $f: (X, \tau) \rightarrow (Y, \sigma)$ is called $g^{\#}\alpha$ - irresolute if $f^{-1}(V)$ is supra $g^{\#}\alpha$ -closed in

(X, μ) for every supra $g^\# \alpha$ -closed set V of (Y, σ) .

III. .STRONGLY SUPRA $g^\# \alpha$ CONTINUOUS AND PERFECTLY SUPRA $g^\# \alpha$ CONTINUOUS.

Definition 3.1 Let (X, τ) and (Y, σ) be two topological spaces and μ be an associated supra topology with τ . A function $f: (X, \tau) \rightarrow (Y, \sigma)$ is called Strongly supra $g^\# \alpha$ -Continuous if the inverse image of every supra $g^\# \alpha$ -closed in Y is supra closed in X .

Definition 3.2 Let (X, τ) and (Y, σ) be two topological spaces and μ be an associated supra topology with τ . A function $f: (X, \tau) \rightarrow (Y, \sigma)$ is called perfectly supra $g^\# \alpha$ -Continuous if the inverse image of every supra $g^\# \alpha$ -closed in Y is both supra closed and supra open in X .

Theorem 3.3 Let (X, τ) be a topological spaces and μ be an associated supra topology with τ . A function $f: (X, \tau) \rightarrow (Y, \sigma)$ is Strongly supra $g^\# \alpha$ -Continuous then it is supra $g^\# \alpha$ -Continuous.

Example 3.4 Let $X=Y=\{a,b,c\}$, $\tau = \{X, \phi, \{a\}\}$ and $\sigma = \{Y, \phi, \{b\}, \{a,b\}\}$.

Let $f: (X, \tau) \rightarrow (Y, \sigma)$ be an identity map.

Then f is supra $g^\# \alpha$ -continuous but not strongly supra $g^\# \alpha$ -continuous, since for the supra $g^\# \alpha$ -closed set $V = \{a\}$ in Y , $f^{-1}(V) = f^{-1}(\{a\}) = \{a\}$ is not supra closed in X .

Theorem 3.5 A function $f: (X, \tau) \rightarrow (Y, \sigma)$ be strongly supra $g^\# \alpha$ -continuous if and only if the inverse image of every supra $g^\# \alpha$ -closed set in Y is supra closed in X .

Theorem 3.6 If a function $f: X \rightarrow Y$ is strongly supra $g^\# \alpha$ -continuous and a map $g: Y \rightarrow Z$ is supra

$g^\# \alpha$ -Continuous, then the composition $g \circ f: X \rightarrow Z$ is strongly $g^\# \alpha$ -continuous

Theorem 3.7 If a function $f: X \rightarrow Y$ is supra continuous then it is strongly supra $g^\# \alpha$ -continuous but not conversely.

Converse of the above theorem need not be true as seen from the following example.

Example 3.8 Let $X=Y=\{a,b,c\}$, $\tau = \{X, \phi, \{a\}\}$ and $\sigma = \{Y, \phi, \{b\}, \{a,b\}\}$.

Let $f: (X, \tau) \rightarrow (Y, \sigma)$ be an identity map. Then f is Strongly supra $g^\# \alpha$ -continuous, $V = \{a\}$ is supra $g^\# \alpha$ -closed in Y , $f^{-1}(V) = f^{-1}(\{a\}) = \{a\}$ is supra closed in X . Since $V = \{a\}$ is not supra closed in Y , f is not supra continuous.

Theorem 3.9 Let (X, τ) be a topological spaces and μ be an associated supra topology with τ . A function $f: (X, \tau) \rightarrow (Y, \sigma)$ is perfectly supra $g^\# \alpha$ Continuous then it is strongly supra $g^\# \alpha$ -Continuous.

Example 3.10 Let $X=Y=\{a,b,c\}$, $\tau = \{X, \phi, \{a\}, \{a,b\}\}$ and $\sigma = \{Y, \phi, \{a\}, \{c\}, \{a,b\}, \{a,c\}\}$. Let $f: (X, \tau) \rightarrow (Y, \sigma)$ be an identity map. Then f is strongly supra $g^\# \alpha$ -continuous but not perfectly supra $g^\# \alpha$ -continuous, since for the supra $g^\# \alpha$ -closed set $V = \{a,c\}$ in Y , $f^{-1}(V) = f^{-1}(\{a,c\}) = \{a,c\}$ is not in both supra open and supra closed in X .

Theorem 3.11 A function $f: (X, \tau) \rightarrow (Y, \sigma)$ be perfectly supra $g^\# \alpha$ -continuous if and only if the inverse image of set in Y is both supra open and supra closed in X .

Theorem 3.12 If a function $X \rightarrow Y$ is strongly supra $g^\# \alpha$

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-continuous then it is supra $g^\# \alpha$ -irresolute but not conversely.

Converse of the above theorem need not be true as seen from the following example.

Example 3.13 Let $X=Y=\{a,b,c\}$, $\tau = \{X, \phi, \{a\}\}$ and $\sigma = \{Y, \phi, \{b\}, \{a,b\}\}$.

Theorem 3.14 If a function $X \rightarrow Y$ is perfectly supra $g^\# \alpha$ -continuous then it is supra $g^\# \alpha$ -irresolute but not conversely.

Example 3.15 Let $X=Y=\{a,b,c\}$, $\tau = \{X, \phi, \{a\}\}$ and $\sigma = \{Y, \phi, \{b\}, \{a,b\}\}$. Let $f: (X, \tau) \rightarrow (Y, \sigma)$ be an identity map.

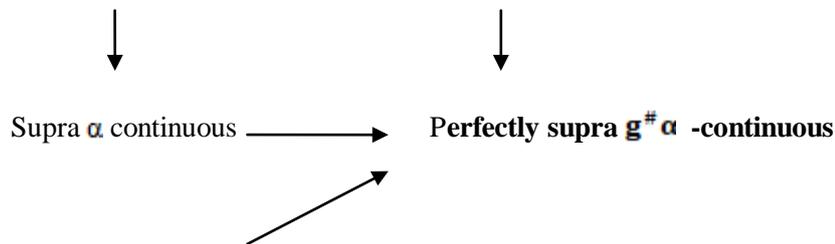
Then f is supra $g^\# \alpha$ -irresolute but not perfectly supra $g^\# \alpha$ - continuous, since for the

supra $g^\# \alpha$ - closed set $V = \{b\}$ in Y , $f^{-1}(V)$

$= f^{-1}(\{b\}) = \{b\}$ is not in both supra open and

supra closed in

Supra continuous \longrightarrow **Perfectly supra $g^\# \alpha$ -irresolute** \longrightarrow supra $g^\# \alpha$ -irresolute



supra $g^\#$ -continuous \longrightarrow
supra gs -continuous

4. ALMOST SUPRA $g^\# \alpha$ -CONTINUOUS FUNCTION

Definition 4.1 A map $f:(X, \tau) \rightarrow (Y, \sigma)$ is called Almost supra continuous function if $f^{-1}(V)$ is supra open set in (X, τ) for every supra regular open set V of (Y, σ) .

Definition 4.2 A map $f:(X, \tau) \rightarrow (Y, \sigma)$ is called Almost supra $g^\# \alpha$ -continuous function if $f^{-1}(V)$ is supra $g^\# \alpha$ -open in (X, τ) for every supra regular open set V of (Y, σ) .

Theorem 4.3 For a function $f:(X, \tau) \rightarrow (Y, \sigma)$, the following are equivalent:

- i) f is almost supra $g^\# \alpha$ -continuous.
- ii) $f^{-1}(V)$ is supra $g^\# \alpha$ -closed in X for every supra regular closed set V of Y .
- iii) $f^{-1}(cl^\mu int^\mu(V))$ is supra $g^\# \alpha$ -closed in X , for every supra closed set V of Y
- iv) $f^{-1}(int^\mu cl^\mu(V))$ is supra $g^\# \alpha$ -open in X , for every supra open set V of Y .

Proof

(i) \Rightarrow (ii) Let V be supra regular closed set in Y . Then $Y-V$ is supra regular open set in Y . Since f is almost supra $g^\# \alpha$ -continuous, $f^{-1}(Y-V)=X-f^{-1}(V)$ is supra $g^\# \alpha$ -open in X . Hence $f^{-1}(V)$ is supra $g^\# \alpha$ -closed in X .

(ii) \Rightarrow (iii) Let V be supra closed set in Y . Then $V = int^\mu cl^\mu(V)$ is supra regular closed set in Y , then by hypothesis, $f^{-1}(int^\mu cl^\mu(V))$ is supra $g^\# \alpha$ -closed in X .

(iii) \Rightarrow (iv) Let V be supra open set in Y . Then $V = int^\mu cl^\mu(V)$ is supra regular open set in

Y . Then $Y - int^\mu cl^\mu(V)$ is supra regular closed set in Y .

Then by hypothesis,

$f^{-1}(Y - int^\mu cl^\mu(V)) = X - f^{-1}(int^\mu cl^\mu(V))$ is supra $g^\# \alpha$ -closed in X . Hence $f^{-1}(int^\mu cl^\mu(V))$ is supra $g^\# \alpha$ -open in X .

(iv) \Rightarrow (i) Let V be supra open set in Y . Then $V = int^\mu cl^\mu(V)$ is supra regular open set and every

regular open set is open set in Y . Then by hypothesis,

$f^{-1}(int^\mu cl^\mu(V)) = f^{-1}(V)$ is supra $g^\# \alpha$ -open in X .

Hence f is almost supra $g^\# \alpha$ -continuous.

Theorem 4.4 Every supra $g^\# \alpha$ -continuous function is almost supra $g^\# \alpha$ -continuous function.

Example 4.5 Let $X=Y=\{a, b, c\}$ and $\tau = \{X, \phi, \{a\}, \{a, b\}\}$, $\sigma = \{Y, \phi, \{a\}, \{b\}, \{a, b\}, \{b, c\}\}$. $g^\# \alpha$ -open set in (X, τ) are $\{X, \phi, \{a\}, \{b\}, \{a, b\}, \{a, c\}\}$. $g^\# \alpha$ -open set in (Y, σ) are $\{Y, \phi, \{a\}, \{b\}, \{a, b\}, \{b, c\}\}$. $f:(X, \tau) \rightarrow (Y, \sigma)$ be the function defined by $f(a)=b, f(b)=c, f(c)=a$. Here f is almost supra $g^\# \alpha$ -continuous but not supra $g^\# \alpha$ -continuous, since $V=\{a, b\}$ is supra open in (Y, σ) but $f^{-1}(\{a, b\}) = \{b, c\}$ is not supra $g^\# \alpha$ -open set in (X, τ)

Theorem 4.6 Every strongly supra $g^\# \alpha$ -continuous function is almost supra $g^\# \alpha$ -continuous function.

Example 4.7 Let $X=Y=\{a, b, c\}$ and $\tau = \{X, \phi, \{a\}, \{a, b\}\}$, $\sigma = \{Y, \phi, \{a\}, \{b\}, \{a, b\}, \{b, c\}\}$. $g^\# \alpha$ -open set in (X, τ) are $\{X, \phi, \{a\}, \{b\}, \{a, b\}, \{a, c\}\}$. $g^\# \alpha$

-open set in (Y, σ) are $\{Y, \phi, \{a\}, \{b\}, \{a, b\}, \{b, c\}\}$.
 $f: (X, \tau) \rightarrow (Y, \sigma)$ be the function defined by $f(a)=b$,
 $f(b)=c$, $f(c)=a$. Here f is almost supra $g^\# \alpha$ -continuous
 but not strongly supra $g^\# \alpha$ -continuous, since $V=\{a, b\}$
 is supra $g^\# \alpha$ -open in (Y, σ) but $f^{-1}(\{a, b\}) = \{b, c\}$ is
 not supra open set in (X, τ) .

Theorem 4.8 Every perfectly supra $g^\# \alpha$ -continuous
 function is almost supra $g^\# \alpha$ -continuous function.

Example 4.9 Let $X=Y=\{a, b, c\}$ and $\tau = \{X, \phi, \{a\}, \{a, b\}\}$,
 $\sigma = \{Y, \phi, \{a\}, \{b\}, \{a, b\}, \{b, c\}\}$. $g^\# \alpha$ -open set
 in (X, τ) are $\{X, \phi, \{a\}, \{b\}, \{a, b\}, \{a, c\}\}$. $g^\# \alpha$ -
 open set in (Y, σ) are $\{Y, \phi, \{a\}, \{b\}, \{a, b\}, \{b, c\}\}$.
 $f: (X, \tau) \rightarrow (Y, \sigma)$ be the function defined by $f(a)=b$,
 $f(b)=c$, $f(c)=a$. Here f is almost supra $g^\# \alpha$ -continuous
 but not perfectly supra $g^\# \alpha$ -continuous, since $V=\{a, b\}$
 is supra $g^\# \alpha$ -open in (Y, σ) but $f^{-1}(\{a, b\}) = \{b, c\}$ is
 not supra clopen set in (X, τ) .

Theorem 4.10 Every almost supra continuous function
 is almost supra $g^\# \alpha$ -continuous function.

Example 4.11 Let $X=Y=\{a, b, c\}$ and $\tau = \{X, \phi, \{a\}, \{a, b\}\}$,
 $\sigma = \{Y, \phi, \{a\}, \{b\}, \{a, b\}, \{b, c\}\}$. $g^\# \alpha$ -
 open set in (X, τ) are $\{X, \phi, \{a\}, \{b\}, \{a, b\}, \{a, c\}\}$. $g^\# \alpha$ -
 open set in (Y, σ) are $\{Y, \phi, \{a\}, \{b\}, \{a, b\}, \{b, c\}\}$.
 $f: (X, \tau) \rightarrow (Y, \sigma)$ be the function defined by
 $f(a)=b$, $f(b)=c$, $f(c)=a$. Here f is almost supra $g^\# \alpha$ -
 continuous but not almost supra continuous, since
 $V=\{a\}$ is supra regular open in (Y, σ) but $f^{-1}(\{a\}) =$
 $\{c\}$ is not supra open set in (X, τ) .

Theorem 4.12 If $f: (X, \tau) \rightarrow (Y, \sigma)$ is supra $g^\# \alpha$ -
 irresolute and $g: (Y, \sigma) \rightarrow (Z, \eta)$ is almost supra $g^\# \alpha$ -
 continuous then $g \circ f: (X, \tau) \rightarrow (Z, \eta)$ is almost supra
 $g^\# \alpha$ -continuous.

Theorem 4.13 If $f: (X, \tau) \rightarrow (Y, \sigma)$ is strongly supra
 $g^\# \alpha$ -continuous and $g: (Y, \sigma) \rightarrow (Z, \eta)$ is almost supra
 $g^\# \alpha$ -continuous then $g \circ f: (X, \tau) \rightarrow (Z, \eta)$ is almost
 supra $g^\# \alpha$ -continuous.

Theorem 4.14 If $f: (X, \tau) \rightarrow (Y, \sigma)$ is contra supra $g^\# \alpha$ -
 irresolute and $g: (Y, \sigma) \rightarrow (Z, \eta)$ is almost contra
 supra $g^\# \alpha$ -continuous then $g \circ f: (X, \tau) \rightarrow (Z, \eta)$ is almost
 supra $g^\# \alpha$ -continuous.

Definition 4.15 (i) A Space (X, τ) is said to be normal if
 for any pair of disjoint closed sets A and B , there exist
 disjoint supra open sets U and V such that $A \subset U$ and
 $B \subset V$

(ii) A Space (X, τ) is said to be supra $g^\# \alpha$ normal if for
 any pair of disjoint closed sets A and B , there exist
 disjoint supra $g^\# \alpha$ open sets U and V such that $A \subset U$
 and $B \subset V$

(iii) A space X is said to be mildly supra $g^\# \alpha$ -normal if
 for every pair of disjoint supra regular closed sets A and
 B of X , there exist disjoint supra $g^\# \alpha$ -open sets U and V
 such that $A \subset U$ and $B \subset V$.

Theorem 4.16 Every supra normal space is mildly supra
 $g^\# \alpha$ -normal.

Example 4.17 Let $X=\{a, b, c, d\}$ and $\tau = \{X, \phi, \{a\}, \{a, b\}, \{c, d\}, \{a, b, c\}, \{b, c, d\}\}$ supra $g^\# \alpha$ -
 open sets in (X, τ) are $\{X, \phi, \{a\}, \{b\}, \{c\}, \{d\}, \{a, b\}, \{a, d\}, \{b, d\}, \{c, d\}, \{b, c\}, \{a, c\}, \{a, b, c\}, \{a, b, d\}, \{b, c, d\}, \{a, c, d\}\}$. Here (X, τ) is mildly
 supra $g^\# \alpha$ -normal but not supra normal, since $A=\{a, b\}$
 and $B=\{d\}$ is supra closed in (X, τ) but A and B is not
 contained in disjoint supra open sets.

Theorem 4.18 Every supra $g^\# \alpha$ -normal space is mildly
 supra $g^\# \alpha$ -normal.

Example 4.19 Let $X=\{a, b, c, d\}$ and $\tau = \{X, \phi, \{a\}, \{d\}, \{a, b\}, \{c, d\}, \{a, b, c\}, \{b, c, d\}\}$
 supra $g^\# \alpha$ -open sets in (X, τ) are $\{X, \phi, \{a\}, \{b\}, \{c\}, \{d\}, \{a, b\}, \{a, d\}, \{b, d\},$

$\{c, d\}, \{b, c\}, \{a, c\}, \{a, b, c\}, \{a, b, d\}, \{b, c, d\}, \{a, c, d\}$. Here (X, τ) is mildly supra $g^\# \alpha$ -normal but not supra $g^\# \alpha$ -normal, since $A = \{a, b\}$ and $B = \{d\}$ is supra closed in (X, τ) but A and B is not contained in disjoint supra $g^\# \alpha$ -open sets.

Theorem 4.20 Every weakly supra $g^\# \alpha$ -normal space is mildly supra $g^\# \alpha$ -normal.

Example 4.21 Let $X = \{a, b, c, d\}$ and $\tau = \{X, \phi, \{a\}, \{d\}, \{a, b\}, \{c, d\}, \{a, b, c\}, \{b, c, d\}\}$ supra $g^\# \alpha$ -open sets in (X, τ) are $\{X, \phi, \{a\}, \{b\}, \{c\}, \{d\}, \{a, b\}, \{a, d\}, \{b, d\}, \{c, d\}, \{b, c\}, \{a, c\}, \{a, b, c\}, \{a, b, d\}, \{b, c, d\}, \{a, c, d\}\}$. Here (X, τ) is mildly supra $g^\# \alpha$ -normal but not weakly supra $g^\# \alpha$ -normal, since $A = \{a, b\}$ and $B = \{d\}$ is supra $g^\# \alpha$ -closed in (X, τ) but A and B is not contained in disjoint supra open sets.

Theorem 4.22 If $f : (X, \tau) \rightarrow (Y, \sigma)$ be supra $g^\# \alpha$ -open map, almost supra $g^\# \alpha$ -continuous surjective, and if X is weakly supra $g^\# \alpha$ -normal, then Y is mildly supra $g^\# \alpha$ -normal.

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