

# A Proposed Fuzzy Optimization Technique for Software Release Time Problem

Shubhra Gautam, Deepak Kumar, L.M. Patnaik

**Abstract:** Reliability is very important in software system to maintain the trust of the customer. At the same time, the software needs to be developed within the time and budget constraint, as software developed with excess budget or taking too much time will affect the entire system. Therefore, it is of prime importance to release the software under the stipulated time without wastage of the budget or impacting reliability of the system. Present work proposes a fuzzy logic approach to find the release time of the software. Current study focuses on a fuzzy model with two fuzzy inputs and one output. The inputs of the fuzzy model are reliability and cost and time is the output. Mamdani Inference System is used to map inputs to outputs. The optimization problem proposed in this study is tested and also validated on the real-time dataset taken from Industry. The results of experiment show that the proposed model gives better time as compared with the models described in the literature. This proposed model can be utilized as a competency model to predict the estimated time of release of any new software.

**Index Terms:** Software Release time, fuzzy optimization, Mamdani Inference, Optimization, software reliability, rule base

## I. INTRODUCTION

Software development takes place in phases, requirement and analysis phase at the first and implementation and documentation phase at the last. The most essential of all the phases is testing phase as it determines the software quality. Timely delivery of software along with cost and reliability are the quality parameters of any software. Software users look for fast delivery, low development price and quality software, whereas the aim of software developer is to minimize development cost, maximize profit and meet the competitive edge. This results in the tradeoff between the user requirement and developers aim. To avoid this trade off the software developer need to find the time as when can we stop the testing of software and make it release ready as per the user requirement of best quality within the budget constraint, these release problems are referred to as “Software Release Time Decision Problem”.

Optimization problems are formulated to obtain the optimal time of release of the software based on targets that

are set by the software user and management. The cost and time are important constraint for the Software developer. The cost has various components like development cost, testing cost, maintenance cost etc. All these cost has to be minimized and at the same time, the developer has to meet the quality constraints.

The traditional approaches in literature focus on crisp [12] or fuzzy optimization [11] of software release time problem. However, the usability of these models has limited coverage. Therefore, there is a need of a model which can have vast coverage and is more adaptable. The authors have explored the use of soft computing tools to solve the optimization problem with two inputs and one output. In this research study, fuzzy rule base model is presented and a rule base is defined to ascertain the relation of cost, reliability & time. The proposed study uses Mamdani Inference System of fuzzy logic and is tested and validated on real time dataset.

The flow of the paper as follows - Section II focuses on the related work. Section III presents the proposed optimization model with input and output functions using Fuzzy Rule Base. In section IV, implementation of proposed model is discussed. In section V, experimental results are discussed and Section VI presents the Conclusion.

## II. RELATED WORK

The optimization problem of software release time roots back to 1980s. In past, many authors have discussed the optimization problem. The optimization problems discussed in literature were single, bi-criteria crisp optimization or fuzzy optimization. A glimpse of optimization work done in past is presented in this section.

The problem of determining the optimum time as to when to stop the testing of system was discussed by Okumoto and Goel [21]. Their optimization problem was dependent on the failure phenomenon of software and the criterion that they used was readiness of the software system. The decision policies involving cost and reliability optimization on existing software were investigated by Yamada et al [27].

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Optimal release policies of software systems by maximizing expected gain were discussed by Kapur et al. [14] and simultaneously they discussed the effect of testing effort expenditure to achieve a given level of failure intensity for SRGMs.

Huang et al [6] discussed the consequences of using different testing techniques or tools to increase the efficiency of testing of software. They formulated an economic policy for software that gives the comprehensive analysis based on the cost of software and its test efficiency. Their policy helped project managers to determine when to stop testing and what is the right time to release the software.

Yun et al. [28] considered three different cost components and used average total profit as criterion. The optimal value of release time was found to be finite and unique. They also found that the optimal release time is inversely proportional to the error rate. The optimization problem considering effect of imperfect fault debugging was proposed by Kapur et al [15]. Pham et al. [22] addressed the questions like How the resources can be scheduled to confirm on-time delivery and Is the software system sufficiently reliable to release. They included warranty cost along with risk cost due to software failure in their cost function. Their models were used to evaluate the accurate total software cost.

Jha et al [10] first discussed the software release time decision problem under fuzzy environment. One of the important decisions for a project manager is to plan the delivery of software in the scheduled expected time. When to stop testing and release the software the software is the most crucial decision for the management. Several factors like size of development team, its experience, cost, etc effect the release of the software. In real, these values cannot be taken as fixed as certain amount of uncertainty or fuzziness is always attached with them. A bi-criterion release time problem with two conflicting objective functions cost reliability and taking available budget as a constraint was discussed by Jha et al.

Further researchers discussed various single or bi-criterion optimization methods using different mean value function and cost function in consideration. The fuzzy rule base optimization of release time is proposed in this study. The proposed model would help in determining the release time of the software and thus improving the quality of software product significantly.

### III. PROPOSED FUZZY OPTIMIZATION PROBLEM

The various optimization problem proposed in history for software release time problem have considered the static or crisp values only. A static or crisp value can have a value as True(1) or False(0) i.e. it either completely belongs to or does not belong to. However, in reality these values cannot have crisp values always. A degree of uncertainty is always attached to the input values as the inputs are dependent on several other factors like experience of team, team size, technology used etc. These value effect our inputs in such a way that the input can have values as somewhat true or somewhat false instead of a complete true and complete false.

A degree of uncertainty is attached with the input values. To accommodate this uncertainty we use fuzzy inputs and propose the problem in fuzzy environment [2]. A fuzzy environment deals with the fuzziness of the inputs and transforms the fuzzy inputs into crisp output. In fuzzy environment; a membership value is attached with every variable. The membership values have values like no membership, complete membership or full membership.

In fuzzy optimization vague or ambiguous information is expressed as precise value and quantify the uncertainty involved in the inputs[1]. Fuzzy optimization is considered to be more flexible as it saves time since it operates on the fuzzy values.

In case of imprecise and uncertain environment of decision making, fuzzy inference systems are best to employ [26].It uses human like reasoning of if-then statements which are termed as rules [29].It also involve understanding of fuzzy variables, their membership functions and knowledge of if-then rules [19].In order to find the optimal release time a fuzzy optimization model with if-then rules is proposed.

#### A. Features of the proposed model

The proposed model uses the if-then rules of fuzzy logic and is implemented in MATLAB. Mamdani inference system is used in this study. Two inputs and one output are identified for the proposed fuzzy optimization model. The input features used are as follows:

Cost (Ct): Ct describe the cost function i.e. it is the total testing cost [13]. Ct is defined as

$$Ct = C_{t1} + C_{t2}m(t) + C_{t3}(m(t+t') - m(t)). \quad (1)$$

Here,  $C_{t1, 2, 3}$  are different testing cost and  $t'$  is warranty period. Total cost is always minimized by the software development team.

Reliability (Rt): Reliability is described as “a function which gives the probability of a fault-free function of any software for a specific period of time within certain given environment”[25].

It is defined as

$$Rt = exp -((m(t+t') - m(t))). \quad (2)$$

Reliability should be maximized to give the best quality software.

The mean number of failure  $m(t)$  used above in cost and reliability function is defined by Sharma et al. [24] considering imperfect debugging with learning function and is defined as

$$m(t) = a * (1 - ((1 + b * t) ** (p * (\beta / (b * b) - \alpha / b)) * \exp(-p * \beta * t / b))) \quad (3)$$

Where  $a$  is initial number of fault in software  
 $b$  is constant fault removal rate  
 $\alpha, \beta$  are constant of intelligence function  
 $p$  is probability of perfect debugging

The output feature is

Time ( $T_t$ ): The time  $T_t$  is the optimal time of release of the software. It is the time at which the software should be released considering the cost function as minimum and reliability function as maximum [5].

### B. Proposed Fuzzy Model:

A system which use the concept of fuzzy set theory for mapping fuzzy I/O into fuzzy O/P resulting in the crisp optimization problem is referred as Fuzzy Inference System (FIS). The two types of fuzzy inference systems are Mamdani fuzzy inference system and Sugeno fuzzy inference system [4].

In this research study, Mamdani inference system is used for mapping of inputs into outputs. It uses following steps for mapping of fuzzy input to fuzzy output.

1. Identify fuzzy rules.
2. Fuzzify inputs using membership function.
3. Decide fuzzy rules.
4. Determine the strength of fuzzy rules by using rule base with fuzzified inputs.
5. Identify the effect of the strength of fuzzy rule with the membership function of output.
6. Merge the result of step 5 to find the distribution pattern of output, and
7. Defuzzify the above output distribution in order to get the crisp output, if needed.

The fig 1 below gives the proposed fuzzy model in soft computing tool MATLAB. The fuzzy model below shows the relationship between cost ( $C_t$ ) and reliability ( $R_t$ ) (Input variables) and Time ( $T_t$ ) (output variable).

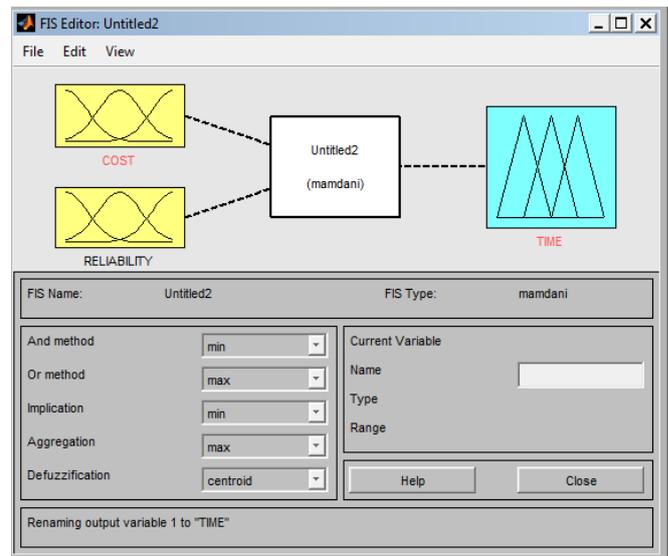


Fig.1: Proposed Fuzzy Model

The values of input variables, reliability ( $R_t$ ) and cost ( $C_t$ ), and output variable Time ( $T_t$ ) are not precise and hence are described in linguistic terms [23].

We have considered fuzzy triangular membership function of Mamdani inference system. Fuzzy triangular membership function considers three different levels of linguistic values for each input and output variable. The three different level of linguistic value is defined as:

- COST: Low (LC), Medium (MC), High (HC)
- RELIABILITY: Low (LR), Medium (MR), High (HR)
- TIME: Low (LT), Medium (MT), High (HT)

On the basis of the knowledge and skill of the development team, a fuzzy rule base is defined. The fuzzy rule base gives the relationship between the linguistic values of inputs with the linguistic value of output.

Table I: Rule base

Rule	If Cost and Reliability		Then Time
	Cost	Reliability	Time
1	LC	LR	LT
2	MC	LR	LT
3	HC	LR	MT
4	LC	MR	MT
5	MC	MR	MT
6	HC	MR	MT
7	LC	HR	MT
8	MC	HR	HT
9	HC	HR	HT

The rule base of fuzzy input/output defined above in table 1 can be implemented in fuzzy software, MATLAB and is viewed on the fuzzy rule viewer as in Fig 2. The 3D graph of the fuzzy rule base defined above is shown in fig. 3.

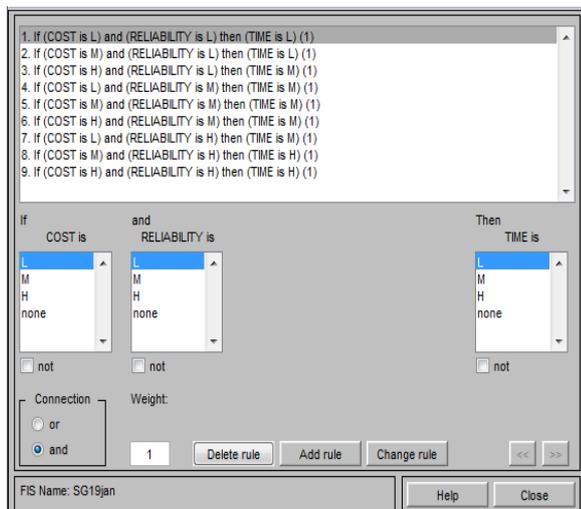


Fig 2: Fuzzy Rule base for DS

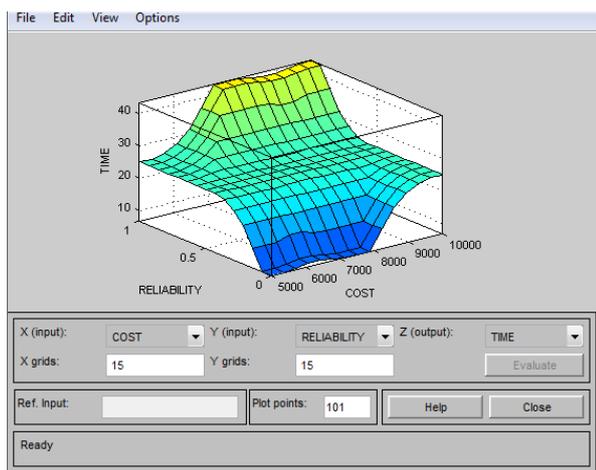


Fig. 3: Cost, Reliability and Time Relationship

The bi criterion optimization problem is solved by using fuzzy rule base(with triangular membership function) as defined in section III(B).

C. Datasets:

A real time dataset is used from Jeske and Zhang [8] for implementation of our method. The software testing period is of 36 weeks and 181 total faults were discovered. By focusing more on System level testing there is a scope to improve overall release quality, reduce defects and timely release of the software in next release.

Table II: Number of Faults

Week Index	Cummulative Failures	No of Failures per week	Week Index	Cummulative Failures	No of Failures per week
1	5	5	19	105	7
2	6	1	20	110	5
3	13	7	21	117	7
4	13	0	22	123	6
5	22	9	23	128	5
6	24	2	24	130	2
7	29	5	25	136	6
8	34	5	26	141	5
9	40	6	27	148	7
10	46	6	28	156	8
11	53	7	29	156	0
12	63	10	30	164	8
13	70	7	31	166	2
14	71	1	32	169	3
15	74	3	33	170	1
16	78	4	34	176	6
17	90	12	35	180	4
18	98	8	36	181	1

Table III: Cost per fault

Timeline	Phase	Description	Cost (\$)
Cost statistics of Release 1	Cost per defect found during testing	Cost incurred to remove fault during testing	254
	Cost per defect before system level testing	Cost incurred to remove fault found in s/w build test or entity level testing before SLT	906
	Cost per fault after release of s/w	Cost incurred to remove fault found by customer	1760

The above values of number of faults and cost are used to estimate the values of total cost and reliability .The values so obtained are used to find the optimal time of release.

IV. IMPLEMENTATION

Fuzzy Logic Toolbox of MATLAB [7] is used for implementing the proposed optimization model. It takes fuzzy input values and generates crisp output value. Table IV below gives the details of set up for proposed model.

TABLE IV: Details of Fuzzy logic set up

Features	Fuzzy Logic Toolbox
Fuzzy Inference system	Mamdani Inference

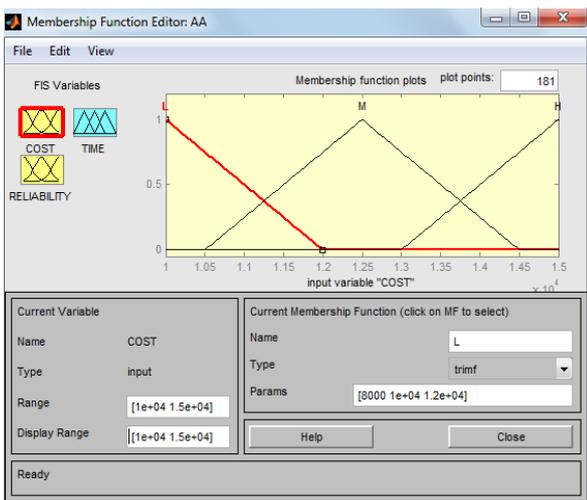
Editor	Fuzzy Toolbox
Membership Function	Triangular
Inputs	Reliability and Cost
Output	Time

In triangular membership function, each of the fuzzy variables, cost, reliability and time, are represented in three range i.e. Low(L), Medium(M) and High(H). The fuzzy model defines the membership function for three fuzzy inequality and constraint corresponding to the objective function, each representing one fuzzy set and is described as

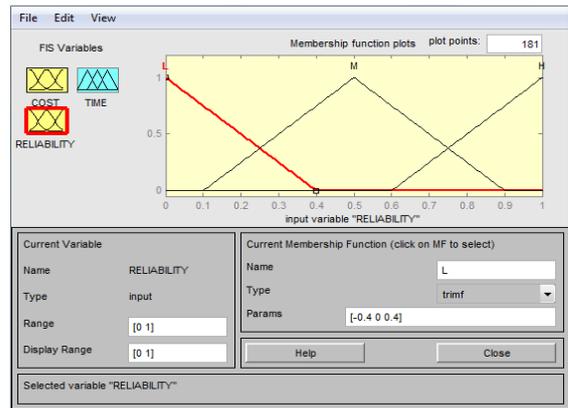
Table V: Cost, Reliability and Time Membership Function

Variable	Membership Function
Cost	$\mu_1(C) = \begin{cases} 1 & ; C \leq C_0 \\ \frac{C - C_0}{C^* - C_0} & ; C_0 < C < C^* \\ 0 & ; C \geq C^* \end{cases}$
Reliability	$\mu_2(R) = \begin{cases} 1 & ; R \geq R_0 \\ \frac{R - R^*}{R_0 - R^*} & ; R^* \leq R < R_0 \\ 0 & ; R < R^* \end{cases}$
Time	$\mu_3(T) = \begin{cases} 1 & ; T \leq T_0 \\ \frac{T - T_0}{T^* - T_0} & ; T_0 < T < T^* \\ 0 & ; T \geq T^* \end{cases}$

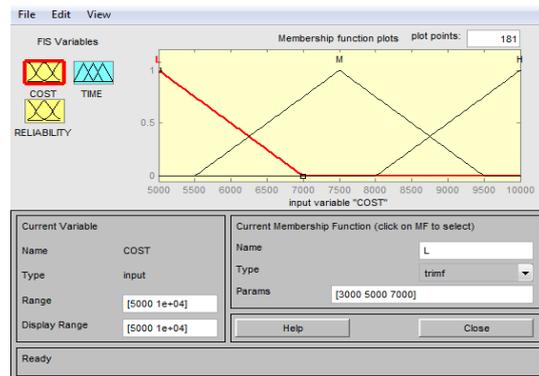
Where  $C_0$ ,  $R_0$ , and  $T_0$  are the restriction or aspiration level of cost, reliability and time respectively and  $C^*$ ,  $R^*$  and  $T^*$  are the corresponding tolerance levels. These membership functions are depicted graphically in below figures 3(a-c):



(a)



(b)



(c)

Fig 3: Cost, Reliability & Time Membership Function

## V. EXPERIMENTAL RESULTS

Methods of Fuzzy mathematical programming are used for solving the optimization problem [9]. In section 4, we have defined the membership function of cost and reliability. Soft computing tool, MATLAB, is used to implement the membership functions.

The function used for defuzzification of fuzzy inputs is  $F'(A) = (aL + 2a + aU)/4$  where  $aL$ ,  $a$ ,  $aU$  is the lower, middle and upper range of the input or output respectively. Management decides the restriction levels of input parameters. The various parameters of SRGM used in the study are estimated and their values are given in table VI below:

Table VI: Parameters of SRGM

a	b	A	$\beta$	p
378.938	0.050	0.009	0.009	0.783

The values of restriction (or aspiration) level and tolerance levels of fuzzy inequalities cost, reliability and time as decided by management are given in table VII below:

Table VII: Aspiration and Tolerance level of Cost and Reliability



Cost		Reliability	
C0	C*	R0	R*
13000	14680	0.99	0.70

Using the above values the optimal release time is found by using the fuzzy function. The model is tested on fuzzy rule base as described above and implemented on MATLAB. The fuzzy rule base of proposed model can be viewed on rule viewer and is shown in fig. 4 below:

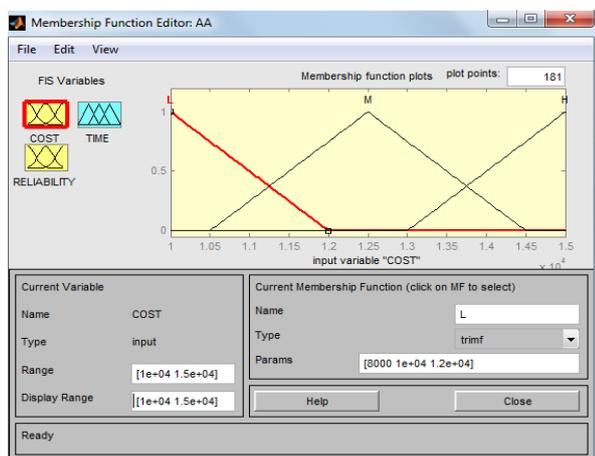


Fig 4: Rules as viewed on rule viewer

The proposed model is tested for different restriction levels of cost and reliability, the time obtained to release the software is summarized in table VIII below:

Table VIII: Optimal Release time for different set of Cost and Reliability

S. No.	Cost(\$)	Reliability	Time(weeks)
1	13000	0.99	34
2	12000	0.20	14
3	14500	0.20	19
4	13000	0.51	20

From the above table we can see that for the restriction levels of inputs, Reliability and cost taken as 0.99 and 13000\$ respectively and the release time obtained is 34 weeks. The proposed model was further tested on other restriction levels values of reliability and cost and corresponding value of release time is recorded. The proposed model is tested on other datasets as well and proved to be of considerable use for software developers as it provides an insight of how much time it will take to release the software under different constraints of cost and reliability. The software schedules can be made accordingly software release with high reliability and within the time budget and time constraint. This will remove any tradeoff between the quality of software developed and budget constraint of the development team. Eventually, there will be an increase in the confidence level of development team and at the same time will ensure trust of the customer on the team.

## VI. CONCLUSION

This paper proposes a bi-criteria fuzzy optimization problem for software release time problem. Many researchers have discussed the optimization of software release time, but they have not considered the fuzziness of the input values. As cost and reliability both are dependent on various external factors, the authors have considered inputs as fuzzy inputs. Fuzzy logic is the field of soft computing that deals with imprecision of the values. A bi-criterion fuzzy optimization problem is formulated with two inputs as cost and reliability and output as time of release. To validate the proposed model, different fuzzy rules are defined, and numerical example is taken to show the results of proposed model. The results are compared with existing optimization models and results show better goodness of fit. There are other factors as well which affect the software release time like team size, working environment etc. These factors can also be taken as input values with cost and reliability to determine the optimal release time. This can be considered as future research in this area.

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