

# Emission Constrained Economic Dispatch with PV Energy Penetration



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**Abstract**—Power system planners are forced to consider the alarming rate of environmental pollution and rapid depletion of fossil fuels and utilize renewable energy resources to mitigate the environmental effects of thermal power stations. Combined Economic Emission Dispatch (CEED) offers an effective solution to reduce fossil fuel emissions as well as cost. Since 1985, CEED is considered to be a common optimization strategy. Literature contains a lot of optimization methods for the strategy. In the recent times, using PV energy has proved to be a feasible and dependable alternative for electricity generation systems based on fossil fuels. In the developing countries, the dependency on fossil fuels has been seen as inevitable. At present, the use of renewable energy sources is rapidly increasing in unconventional power generation systems.

The present paper puts forward an approach of combining PV energy-based grid integrated PV system with fossil fuel based thermal power plant using evolutionary programming based optimization technique. Among the various optimization techniques, the Particle Swarm Optimization (PSO) is considered to be the most suitable technique for the problem is explained in detailed manner. The proposed method is to combine CEED with the PV energy and thereby reduces the use of conventional energy resources. It also permits an effective utilization of abundantly available PV energy. It is tested on standard IEEE 30 bus system with the real time ratings of proposed PV plant situated in Tamilnadu.

**Index of terms**—Fossil fuel depletion, fuel economy, PV insolation, economic dispatch, emission dispatch, grid integrated PV photovoltaic systems, Particle Swarm optimization.

## I. INTRODUCTION

Combined Economic Emission Dispatch (CEED) is a proven method to effectively reduce greenhouse emissions as laid down by the IPCC (Inter Governmental Panel on Climate Changes). The Paris Summit on Climatic Changes held recently considerably lowered the ceiling of carbon dioxide emissions. The present paper suggests methods wherein renewable energy sources are used with fossil fuels through CEED.

Planning for effective power generation carries tremendous significance for electrical utility. Looking from the perspective of environmental conservation, pollution caused by emissions from fossil fuel-based power generation plants adversely affect life forms on earth in one way or the other.

So, the present times demand a reliable, economic and eco-friendly electrical generation methods [1]. Efficient planning of power generation in thermal power plants includes proper allocation of power generation in order to optimize fuel costs and emissions considering power constraints [2]. Increasing energy prices, environmental concerns and fast depletion of the known fuel resources have significantly enhanced the scope of renewable energy resources. The CEED problem is mathematically defined as multiple objective optimization approaches to examine the effective usage of thermal and conventional resources to sustain the load balancing in power stations [3]. Combining renewable and non-renewable energy sources helps in bringing down greenhouse emissions considerably. A major hurdle in this integration is the uncertainty associated with the availability of renewable power sources. Until now, PSO algorithm is used solely to minimize fuel costs and emission levels [4]. A research done earlier on CEED with power flow constraints uses various evolutionary programming techniques and compares their performance [5]. Until now, the option of utilizing PV energy for minimizing fossil fuel cost alone is considered but that of emissions has not been considered [6]. By integrating renewable energy sources like wind, PV, etc. into the conventional power plants, the expenditure on fuel costs can be reduced significantly [7]. Various non-conventional energy sources have been used to reduce the use of fossil fuels considering valve point loading. However, PV energy has not been accounted for in CEED related problem. [7]. Real time models could achieve best possible solution when the CEED issue is considered along with valve point loading. However, the reduction of expenses related to fuel comes with other augmented losses [7]. Literature review clearly reveals the need for an efficient optimization algorithm to solve the CEED problem. Kennedy and Eberhart came up with an algorithm based on PSO which is based on the behaviour of fish schools and bird swarms. When this Swarm model is differently configured, it can offer almost perfect and easy to apply solution with quicker convergence [8-13]. Considering all the above factors, the authors of the present paper arrived at a decision to consider the classical model of PSO algorithm to solve the problem dealt with in this research work.

## II. METHODOLOGY

The objective of CEED problem is to plan the generating unit outputs aimed at desired load demand at minimum operating cost and emission value is met while fulfilling the constraints of all the generating units. This problem of CEED can be stated as:

$$\min Q = \sum_{i=1}^n (Eco_i(G_i) + Emi_i(G_i)) \quad (1)$$

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Where Q: objective function

$Eco_i(G_i)$  : Economic fuel cost  
 $Emi_i(G_i)$ : ithunit Emissions of

Equality Constraint

$$\sum_{i=1}^n G_i - G_L - G_d = 0 \quad (2)$$

Where  $G_i$  : i<sup>th</sup> unit Power generation  
 $G_L$ : Power loss  
 $G_d$ : Power demand  
n: number of generating units

Inequality Constraint

$$G_{imin} \leq G_i \leq G_{imax} \quad (3)$$

Where  $G_{imin}$  : Minimum power limits of i<sup>th</sup> unit  
 $G_{imax}$  : Maximum power of i<sup>th</sup>unit

### A. Economic Dispatch

$$Eco_i(G_i) = a_i P_i^2 + b_i P_i + c_i \quad (4)$$

Where  $a_i, b_i$  and  $c_i$  represent the fuel cost coefficients

### B. Emission Dispatch:

$$Emi_i(G_i) = \alpha_i P_i^2 + \beta_i P_i + \gamma_i \quad (5)$$

Where  $\alpha_i, \beta_i$ , and  $\gamma_i$  are the emission coefficients of the generating unit

$$G_L = \sum_{i=1}^n \sum_{j=1}^n G_i B_{ij} G \quad (6)$$

Where  $B_{ij}$ : loss coefficient matrix.

### C. Combined Economic Emission Dispatch

The combined objective problem discussed above is changed into a objective problem by bringing in 'h' factor also known as price penalty factor. The changes that the CEED problem undergoes after introducing 'h' factor can be represented as:

$$Min F_c = \sum_{i=1}^n ((\alpha_i P_i^2 + \beta_i P_i + \gamma_i) + h_i (d_i P_i^2 + e_i P_i + f_i)) \$ / hr \quad (7)$$

Where  $h_i$  is given as:

$$h_i = \frac{a_i P_{imax}^2 + b_i P_{imax} + c_i}{\alpha_i P_{imax}^2 + \beta_i P_{imax} + \gamma_i} \quad (8)$$

### D. Problem Formulation for PV Energy Penetration

The power output of PV plant can be shown as:

$$P_{gs} = P_{rated} \{ 1 + (T_{ref} - T_{amb}) * \alpha \} * \frac{S_i}{1000} \quad (9)$$

Where  $P_{rated}$  - rated power

$T_{ref}$  - Reference temperature

$T_{amb}$  - Ambient temperature

$\alpha$  - Temperature coefficient

$S_i$  - Incident PV radiation (PV insolation)

When m numbers of PV plants take part in dispatch and its share is represented as:

$$PV \text{ share} = \sum_{j=1}^m P_{gsj} * U_{sj} \quad (10)$$

Where  $P_{gsj}$  is power available from jth unit

$U_{sj}$  is status of jth PV unit

The cost of PV power is given as

$$PV \text{ cost} = \sum_{j=1}^m PUcost_j * P_{gsj} * U_{sj} \quad (11)$$

Where  $PUcost_j$  is per unit cost of jth unit

### E. CEED with PV Energy Penetration

The present paper has the goal of efficiently using the abundantly available PV power in addition to reducing fuel costs. After the integration of PV energy, the objective function becomes

$$Min F_T = \sum_{i=1}^n (a_i P_i^2 + b_i P_i + c_i + h_i * (\alpha_i P_i^2 + \beta_i P_i + \gamma_i)) + \sum_{j=1}^m PUcost_j * P_{gsj} * U_{sj} \left( \sum_{j=1}^m P_{gsj} - \sum_{j=1}^m P_{gsj} * U_{sj} \right) \quad (12)$$

Subject to

$$P_d + P_L - \sum_{i=1}^n P_i - \sum_{j=1}^m P_{gsj} * U_{sj} \quad (13)$$

$$P_{imin} \leq P_i \leq P_{imax} \quad (14)$$

$$\sum_{j=1}^m P_{gsj} * U_{sj} \leq 0.3 * P_d \quad (15)$$

$$\forall U_{sj} \in \{0,1\} \quad (16)$$

Where  $K_s$  : constant

## III. OPTIMIZATION METHOD

Developed by Eberhart and Kennedy in 1995, Particle Swarm Optimization algorithm of swarm intelligence was influenced by the behavior of fish and bird swarms. This algorithm combines personal and social knowledge to arrive at optimum solution for a problem. The algorithm considers swarming particles that move together in a search space in order to obtain optimum value. In the algorithm, swarming particles are solutions and they move together in the direction of suitable area to reach an overall perfection. The algorithm correlates the unpredictable but orderly movement of a swarm of bird with the changing conditions and available solutions for a given problem. Each particle of the swarm stands for a vector for each particle in search space. This particular vector has an assigned vector (or the velocity vector) that decides the successive movements of particles.

The PSO algorithm helps to update the swarm velocity. Each particle in the swarm modifies its velocity based on the present velocity of the swarm, the best positions it had explored so far and the overall optimal position explored by the swarm.

### Parameters of the PSO algorithm:

**P** : Population of agents

**p<sub>i</sub>**: agent location **a<sub>i</sub>** in the solution space

**f**: Objective function

**v<sub>i</sub>**: Velocity of agent's **a<sub>i</sub>**

**N(a<sub>i</sub>)** : Neighborhood of agent's **a<sub>i</sub>** (fixed)

Particle update rule

$$p = p + v \quad (17)$$

with,

$$v = v + c_1 * \text{rand} * (P_{best} - p) + c_2 * \text{rand} * (G_{Best} - p) \quad (18)$$

where

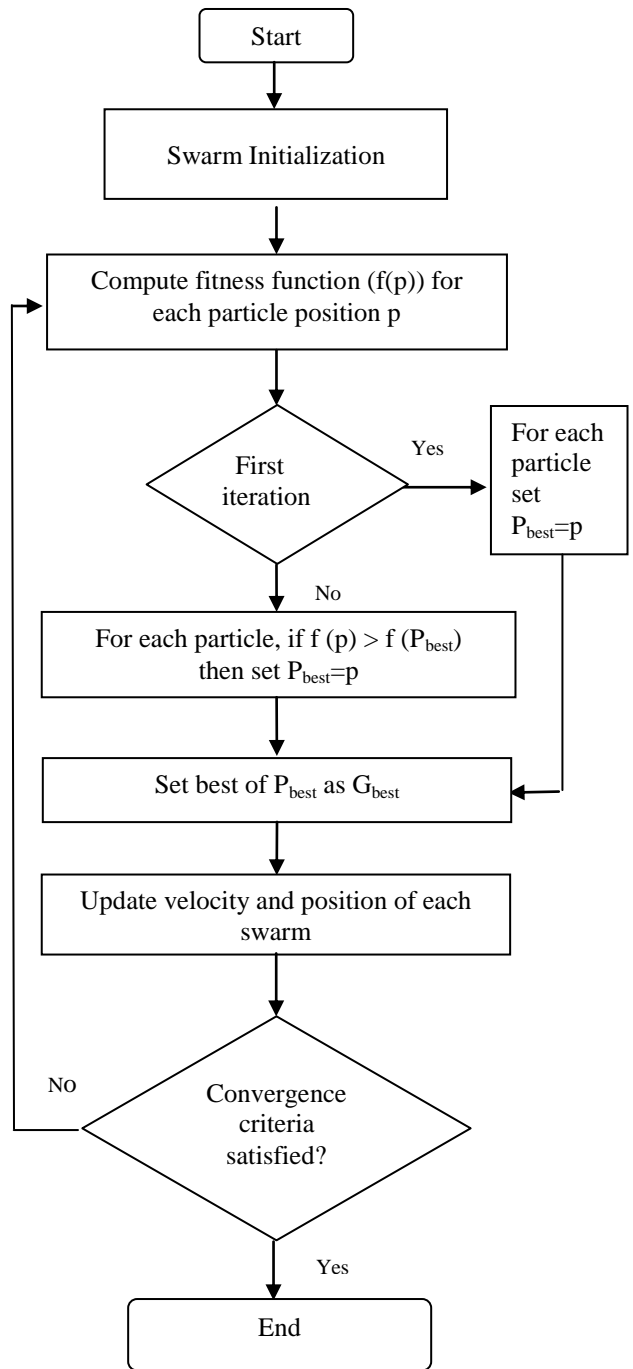
- p: Particle position
- v: Particle direction
- $w_1$  : Local particle weights
- $w_2$  : Global particle weights
- $P_{best}$ : Optimal position of the particle
- $G_{Best}$ : Optimal position of the swarm
- rand: Randomness of the variable

**ALGORITHM:**

- Generate an agent group (particles) which has a uniform distribution over X
  - Identify the position of each particle with respect to the objective function.
  - Update the current position of the particle, if it is better than the previous position
  - Determine the best particle from the sequence of previous best of each particle
  - Update velocity of each particle using the below equation
- $$v_i^{t+1} = v_i^t + c_1 * U_1^t * (pB_i^t - p_i^t) + c_2 * U_2^t * (gB_i^t - p_i^t) \quad (19)$$
- Move the particles to new position by
- $$p_i^{t+1} = p_i^t + v_i^{t+1} \quad (20)$$
- Repeat the process from step 2 until convergence criteria is achieved

**Table 1: Problem Parameters for the Assessed Method**

Algorithm Parameters	Problem Parameters	Initialization of Parameters
Population	Optimum Generation of Generators	30
Swarm	Iteration	1000
Particles	Optimum Generation of Generators	100
Velocity	Turbine speed	0.9,0.99
Inertial(weight) Factor	Moment of inertia of the rotor	1,1.5
$P_{best}$	Individual best fuel cost/emission parameter of each generator	-
$G_{best}$	Overall best fuel cost/emission parameter of 6 generators	-



**Fig 1: PSO Algorithm Flow Chart**

**IV. TEST SYSTEM**

The method presented is carried out on a standard test system consisting of six thermal power generation units and six PV plants. The ratings of the PV Photo Voltaic Panel are taken from an independent power producer installed in Tamilnadu. The thermal units ratings are taken from [20]. Table 2 presents the fuel cost coefficients. Table 3 represents minimum and maximum power limits. Table 4 represents the emission coefficients of the thermal units. The data for PV plants is presented in table 5 and 6 [20].

Table 5 shows the power ratings and per unit costs of various PV plants and Table 6 provides the global PV radiation data of Kamudhi for the 1<sup>st</sup> day of January 2016 [23].

**Table 2: Thermal Unit cost coefficients**

Generator	$\alpha$ (\$/MW <sup>2</sup> hr)	$\beta$ (\$/MW h)	$\gamma$ (\$/h)
1	0.15247	38.53973	756.79
2	0.10587	46.15916	451.32
3	0.02803	40.39655	1049.32
4	0.03546	38.30553	1243.53
5	0.02111	38.32782	1658.56
6	0.01799	38.27041	1356.27

**Table 3: Thermal units generation capacities**

Generator	$G_{min}$ (MW)	$G_{max}$ (MW)
1	10	125
2	10	150
3	40	250
4	35	210
5	130	325
6	125	315

**Table 4: Thermal unit emission coefficients**

Generator	$d$ (kg/MW <sup>2</sup> h)	$e$ (kg/MWh)	$f$ (kg/h)
1	0.00419	0.32767	13.85932
2	0.00419	0.32767	13.85932
3	0.00683	-0.54551	40.2669
4	0.00683	-0.54551	40.2669
5	0.00461	-0.51116	42.89553
6	0.00461	-0.51116	42.89553

**Table 5: PV plant power capacity and unit rates**

PV Photo Voltaic Plant	$P_{rated}$ (MW)	Unit rate(\$/KW h)
1	108	0.11
2	108	0.11
3	108	0.11
4	108	0.11
5	108	0.11
6	108	0.11

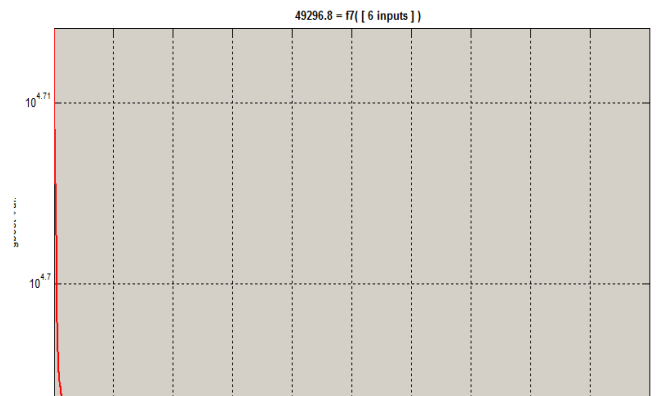
**Table 6: GlobalPV radiation data of the location**

Time	Global PV Radiation(W/m <sup>2</sup> )	Temperature(°C)
1:00	0	31
2:00	0	30
3:00	0	30
4:00	0	30
5:00	0	30
6:00	0	30

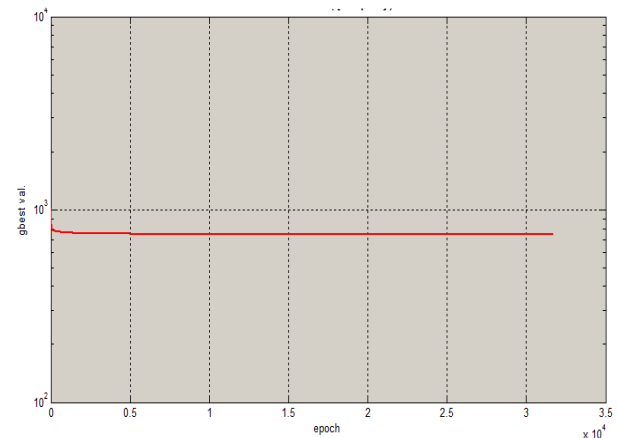
7:00	209	31
8:00	520	32
9:00	790	33
10:00	1001	33
11:00	1137	33
12:00	1189	34
13:00	1154	34
14:00	1034	34
15:00	837	33
16:00	578	33
17:00	273	32
18:00	0	31
19:00	0	31
20:00	0	31
21:00	0	30
22:00	0	30
23:00	0	30
24:00	0	30

**V. RESULTS**

The suggested method was implemented in MATLAB 2016a software. The following control settings were used for PSO: velocity  $w1=0.9$ ,  $w2=0.99$ , random numbers between 0 and 1, maximum no. of iterations=1000, number of particles =100, weight factor =1, 1.5.



**Fig 2: CEED Results for Minimum Fuel Cost**



**Fig 3: CEED Results for Minimum Emission Value**

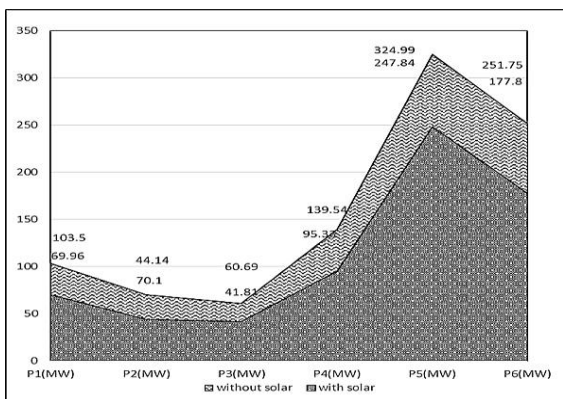


**Table 7: Results of CEED for 900 MW Demand**

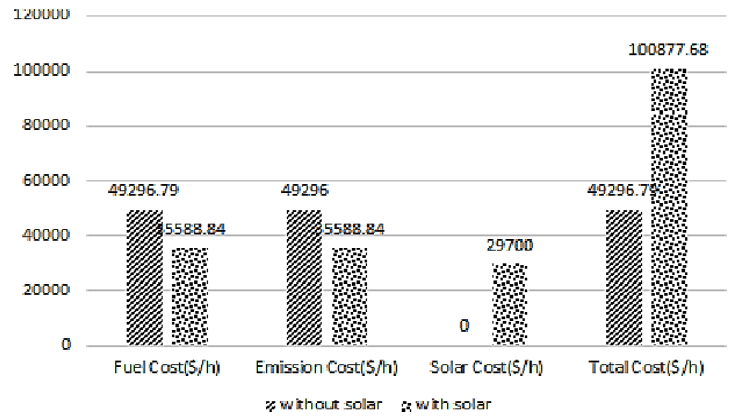
Thermal Generation	P <sub>1</sub> (MW)	103.50
	P <sub>2</sub> (MW)	70.10
	P <sub>3</sub> (MW)	60.69
	P <sub>4</sub> (MW)	139.54
	P <sub>5</sub> (MW)	324.99
	P <sub>6</sub> (MW)	251.75
Cost	Fuel cost (\$/h)	49,296.79
	Emission cost (\$/h)	49,296.00
	Total Cost(\$/h)	98,592
Others	Emission(Kg/h)	749.463

**Table 8: CEED results with PV for 900MW Demand**

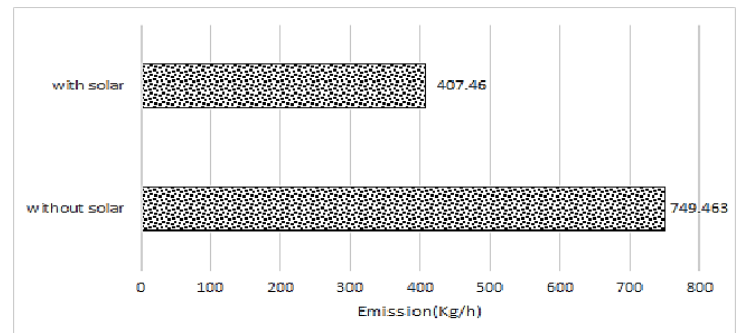
Thermal Generation	P <sub>1</sub> (MW)	69.96
	P <sub>2</sub> (MW)	44.14
	P <sub>3</sub> (MW)	41.81
	P <sub>4</sub> (MW)	95.33
	P <sub>5</sub> (MW)	247.84
	P <sub>6</sub> (MW)	177.80
PV Generation	PV power share(MW)	270.00
Cost	Fuel cost (\$/h)	35,588.84
	Emission cost(\$/h)	35,588.84
	PV cost	29,700.00
	Total Cost(\$/h)	1,00,877.68
Others	Emission(Kg/h)	407.46



**Fig 4: Generation details after rescheduling with PV power.**



**Fig 5: Comparative analysis of cost after CEED with solar penetration.**



**Fig 6 Comparative analysis of emission cost CEED before and after PV penetration.**

Tables 7 and 8 shows the results of CEED with PV penetration for the demand of 900MW in IEEE 30 bus system. After the introduction of PV energy, the total power generation of six units in the test system reduced to 273.72MW. PV penetration resulted in considerable reduction of emission from 749.46Kg/h to 407.46Kg/h. Fossil fuel cost for the six units also reduced to 13,707.96\$/h. Total cost includes the Tariff cost for IPP produced units from PV plant, maintenance cost for PV Photo Voltaic Plant and the Transmission cost. The results of CEED with PV power penetration in various aspects such as Generation cost and emission cost is depicted pictorially. By switching the connected PV units, the thermal power generation can be increased or decreased accordingly. The additional operating cost of integrating the PV units adds to the overall fuel cost. However, it reduces emissions and the cost spent on the thermal units.

**VI. CONCLUSION**

The present paper presents an optimal solution for CEED problem using PV energy as an alternative. It considers the environmental conditions and makes use of renewable PV energy which has not only become essential but inevitable. The study was carried out for a standard system consisting six generators and six PV plants and using PSO as its optimization method.

The results obtained by PSO for CEED with PV penetration were compared with CEED without PV penetration. It is important to note that emission levels, related costs and fossil fuel costs were considerably reduced. However, but the overall cost of power generation is increased. Power generation cost of the hybrid plant can be expected to be the same as the unit cost of wind mills. This could become a reality when the manufacturing cost of thin film PV Photo Voltaic cell or single crystalline Photo Voltaic cell is made lesser. The disadvantage of the present method is that the power is considered for a loss account and the gap between generation and demand is increased after PV penetration. This is due to the fact that PV plant requires large area of land for its infrastructure and high insolation area; hence it is not possible to commission the large size PV Photo Voltaic plant very near the load centre. This creates a gap between power generation and power demand which can be considered as transmission loss. This paper is certainly an initiative to counter Global warming and serious hazards of pollution.

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