

# Ternary $\Gamma$ -SO-semirings-3

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**Abstract:** “In this paper we are introducing the notions of subtractive and strong subsets in partial ternary  $\Gamma$  - semirings.

We show that in a ternary  $\Gamma$  - SO semiring satisfying that every non-zero ideal is strong and subtractive Further we will show that join of any two ideals is equal to the sum of those two ideals in a ternary  $\Gamma$  - SO semiring satisfying the decomposition property. In a ternary  $\Gamma$  - SO semiring satisfying the decomposition property then ideal(R) is a distributive lattice”.

**Keywords:** Subtractive, strong, austere, join, entire.

## I. INTRODUCTION

The notion of ideals in SO-rings studied by G.V.S Acharyulu [1] and M.MuralikrishnaRao[8] studied ideals in  $\Gamma$  - semirings. Further ideals of SO-Partial  $\Gamma$  - semirings investigated by Sivamala.M, Siva Prasad.K [19]. Recently the study of ideals in ternary  $\Gamma$  - semiring [12].

## II. PRELIMINARIES

Throughout this paper ternary  $\Gamma$ -SO –semiring refers to TFSS. And CTF-SS refers to complete ternary  $\Gamma$ -SO –semiring. From below some important definitions is given:

**Definition2.1:** [8] “Let R and  $\Gamma$  be two additive commutative semi groups. R is said to be a **ternary  $\Gamma$ -semiring** if there exist a mapping from  $R \times \Gamma \times R \times \Gamma \times R \rightarrow R$  which maps  $(x_1, \alpha, x_2, \beta, x_3) \rightarrow [x_1 \alpha x_2 \beta x_3]$  satisfying the conditions

- (i)  $(aab\beta c)\gamma d\delta e = a\alpha(b\beta c\gamma d)\delta e = aab\beta(c\gamma d\delta e)$
  - (ii)  $[(a+b)\alpha c\beta d] = [aac\beta d] + [bac\beta d]$
  - (iii)  $[a\alpha(b+c)\beta d] = [aab\beta d] + [aac\beta d]$
  - (iv)  $[a\alpha b\beta(c+d)] = [a\alpha b\beta c] + [a\alpha b\beta d]$
- for all  $a, b, c, d \in R$  and  $\alpha, \beta, \gamma, \delta \in \Gamma$ ”.

**Definition2.2:**[12] “Let M be a ternary  $\Gamma$ -SO-semiring. A non-empty subset A of M is known as **left (lateral, right) ternary  $\Gamma$ -ideal** of M, if it satisfies the following:

- (i) A is a left (lateral, right) partial ternary  $\Gamma$ -ideal of M.
- (ii)  $x \in M$  and  $y \in A$  such that  $x \leq y$  then  $x \in A$ .

If A is left, lateral as well as right ternary  $\Gamma$ -ideal of M, then A is known as ternary  $\Gamma$ -ideal of M”.

**Definition2.3:** [12] “A partial ternary  $\Gamma$ -semiring said to have a **left (lateral, right) unity element** provided there exist a family  $(e_i : i \in I)$  of M and  $(\alpha_i, \beta_i : i \in I)$  of  $\Gamma \ni$

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$\sum e_i \alpha_i e_i \beta_i a = a (\sum e_i \alpha_i a \beta_i e_i = a, \sum a \alpha_i e_i \beta_i e_i = a)$  for any  $a \in M$ ”.

**Definition2.4:**[12] “A TFSS M is said to be **CTF-SS (complete ternary  $\Gamma$ -SO-semiring)** if every family of elements in M is sum able”.

And for more preliminaries the references [12] [13] [14] [15][16][17] and [18].

## III. MAIN RESULTS

**Definition3.1:** U is known as non empty subset PTFS (“partial ternary  $\Gamma$  - semiring”) if  $u_1, u_2 \in R, u_1 + u_2 \in U$  and  $u_2 \in U \Rightarrow u_1 \in U$  then R is called **subtractive**.

**Definition3.2:** U is known as non empty subset of a PTFS R is known as **strong** if  $u_1, u_2 \in R, u_1 + u_2 \in U \Rightarrow u_1, u_2 \in U$ . Since strong subset is clearly subtractive.

**Example: 3.3:** Let  $R = \{0, u_1, u_2, u_3, u_4, u_5\}$ ,  $\Gamma = \{\alpha, \beta\}$  by using R,  $\Sigma$  is described.

$$\sum_i x_i = \begin{cases} x_j & \text{if } x_i = 0 \forall i \neq j, \text{ for some } j \\ z & \text{if } x_j = u_1, x_k = u_2 \text{ for some } j, k \text{ and } x_i = 0 \forall i \neq j, k \\ \infty, & \text{otherwise} \end{cases}$$

$\Gamma$  –monoid is defined by R.

$R \times \Gamma \times R \times \Gamma \times R \rightarrow R$  is mapped as given below:

$\alpha$	0	$u_1$	$u_2$	$u_3$	$u_4$	$u_5$
0	0	0	0	0	0	0
$u_1$	0	0	0	0	0	0
$u_2$	0	0	0	0	0	0
$u_3$	0	0	0	0	0	0
$u_4$	0	0	0	0	0	0
$u_5$	0	0	0	0	0	0

$\beta$	0	$u_1$	$u_2$	$u_3$	$u_4$	$u_5$
0	0	0	0	0	0	0
$u_1$	0	$u_1$	0	$u_3$	0	$u_1$
$u_2$	0	0	$u_2$	0	$u_4$	$u_2$
$u_3$	0	0	$u_3$	0	$u_1$	$u_3$
$u_4$	0	$u_4$	0	$u_2$	0	$u_4$
$u_5$	0	$u_1$	$u_2$	$u_3$	$u_4$	$u_5$

Then R is a PTFS. Here the subset  $\{0, u_1, u_2, u_5\}$  is strong. Therefore it is subtractive subset.

**Example 3.4:** In example 3.3 the subset  $U = \{0, u_3, u_5\}$  is subtractive but not strong because  $u_1 + u_2 = u_5$  and both  $u_1, u_2 \notin U$ .

**Theorem3.5:** In a TFSS R every non-zero ideal is strong and hence subtractive.



**Proof:** R is non zero which is ideal in condition. Let  $x, y \in R$  such that  $x+y$  exists in R and  $x+y \in X$ . Since X is an ideal and  $x \leq x+y, y \leq x+y \Rightarrow x, y \in X$ . Therefore X is a strong ideal of R.

**Definition3.6:** “A PTFS R is said to be *left austere*. R has no non-zero subtractive left partial ideals. A TFSS R is left Austere if it has no non-zero left ideals”.

**Definition3.7:** A PTFS R is said to be *entire* If it satisfies the conditions  $aab\beta c = 0 \Rightarrow$  either  $b=0$  and  $a=0$  and  $c=0$  where  $\forall a, b, c \in R, \alpha, \beta \in \Gamma$ .

**Theorem3.8:** If R is a left austere TFSS with left unity then R is entire.

**Proof:** Let  $x, y, z \in R$ . Suppose  $xay\beta z = 0 \forall \alpha, \beta \in \Gamma$ .

Let us take  $A = \{r \in R / ray\beta z = 0 \forall \alpha, \beta \in \Gamma\}$

First we show that A is a left ideal of R.

Clearly  $0 \in A$ . Suppose  $x \neq 0$  then  $x \in A \neq \{0\}$ .

Let  $\{a_i : i \in I\}$  in R and  $a_i \in A \forall i \in I$

then for all  $\alpha, \beta \in \Gamma$  each  $a_i \alpha y \beta z = 0$

$\Rightarrow \forall \alpha, \beta \in \Gamma (\sum_i a_i) \alpha y \beta z = 0 \Rightarrow \sum_i a_i \in A$ .

Let  $s \in R$ , and  $t \in A$  such that  $s \leq t$  since  $t \in A$ ,

$tay\beta z = 0 \forall \alpha, \beta \in \Gamma$ . Since  $s \leq t$

$\Rightarrow say\beta z \leq tay\beta z \forall \alpha, \beta \in \Gamma$

$\Rightarrow say\beta z = 0 \forall \alpha, \beta \in \Gamma \Rightarrow s \in A$ .

Let  $q, r \in R, \gamma, \delta \in \Gamma$  and  $x \in A$

Here  $x \in A \Rightarrow xay\beta z = 0 \forall \alpha, \beta \in \Gamma$

Consider

$(q\gamma r\delta x)\alpha y\beta z = q\gamma r\delta(x\alpha y\beta z) = q\gamma r\delta(0) = 0 \forall \alpha, \beta \in \Gamma$

$\Rightarrow q\gamma r\delta x \in A$ .

The value of R is obtained as ideal in left position if the value of A is maintained at non zero condition.

Since R has left unity, then there exist a family  $(e_i : i \in I)$  in R and  $\gamma_i, \beta_i \in \Gamma$  such that  $\sum_i e_i \gamma_i e_i \beta_i r = r \forall r \in R$ .

Since  $A=R$ , and hence  $(e_i : i \in I) \in A. \Rightarrow e_i \alpha y \beta z = 0 \forall \alpha, \beta \in \Gamma$ .

Therefore in particular  $e_i \gamma_i y \beta_i z = 0 \forall i \in I$

$\Rightarrow \sum_i e_i \gamma_i y \beta_i z = 0 \Rightarrow y=0$  or  $z=0$ .

Hence R is entire.

**Note3.9:** In general 3.8 theorem is converse which is not true for this consider the following example.

**Example3.10:** Let  $R = [0, 1]$  is the real number for unit interval.  $(a_i : i \in I)$  is the family in R which defines  $\sum_i a_i = \text{Sup}\{a_i / i \in I\}$  and after that partial ternary monoid R is defined. If we take  $\Gamma=W$  then R is a partial ternary  $\Gamma$ -monoid. Consider the mapping  $(x, \alpha, y, \beta, z) \rightarrow \inf(x, \alpha, y, \beta, z)$  of  $R \times \Gamma \times R \times \Gamma \times R \rightarrow R$  then R is a PTFS. Then R is a TFSS with usual  $\leq$  of real numbers. For any non-zero  $x \in R, [0, x]$  is a non-zero ideal of R and hence R is not left Austere. Since  $xay\beta z = \inf(x, \alpha, y, \beta, z) = 0 \forall \alpha, \beta \in \Gamma \Rightarrow x=0$  or  $y=0$  or  $z=0$ . And hence R is an entire TFSS.

**Theorem3.11:** CTT-SSR is the principal idea to join the two principles of CTT-SSR.

**Remark3.12:** In any CTT-SS  $\forall_i \langle a_i \rangle = \langle \sum_i a_i \rangle$ .

**Definition3.13:** Let X, Y be two ideals of a TFSS then  $X+Y = \{x+y/x \in X, y \in Y\}$ .

**Definition3.14:** A TFSS R is known as have the *decomposition property* iff for any  $a_1, a_2, a_3 \in R, a_1 \leq a_2 + a_3$  then there exist  $b_1, b_2 \in R$  such that  $0 \leq b_1 \leq a_2, 0 \leq b_2 \leq a_3$ , and  $a_1 = b_1 + b_2$ .

**Theorem3.15:** let a TFSS R satisfying the decomposition property and P+Q is obtained for the ideal value of R.

**Proof:** First we show that R is an ideal value for P+Q. In R the summable family is assumed as  $(x_i / i \in I)$  and  $x_i \in P + Q \forall i \in I$  then  $x_i = a_i + b_i$  for some  $a_i \in P$  and  $b_i \in Q \forall i \in I$

$\Rightarrow \sum_i x_i = \sum_i a_i + \sum_i b_i$  where  $\sum_i a_i \in P$  and  $\sum_i b_i \in Q$ .

$\Rightarrow \sum_i x_i \in P + Q$

Let  $x \in R, b \in P + Q$  for some  $p \in P$  and  $q \in Q$  the value  $x \leq b \Rightarrow x \leq b = p + q$ .

By decomposition property there exist  $0 \leq p_1 \leq p, 0 \leq q_1 \leq q$  such that  $x = p_1 + q_1$ .

Since  $p_1 \leq p, p \in P \Rightarrow p_1 \in P$  and  $q_1 \leq q,$

$q \in Q \Rightarrow q_1 \in Q$

Therefore  $x = p_1 + q_1 \in P + Q$ .

Let  $r_1, r_2 \in R, x \in P + Q$  and  $\alpha, \beta \in \Gamma$

then  $r_1, r_2 \in R, x = p + q$  where  $p \in P, q \in Q$  and

$\alpha, \beta \in \Gamma$ .

Consider

$r_1 \alpha r_2 \beta x = r_1 \alpha r_2 \beta (p + q) = r_1 \alpha r_2 \beta p + r_1 \alpha r_2 \beta q$

Where  $r_1 \alpha r_2 \beta p \in P, r_1 \alpha r_2 \beta q \in Q$ .

$\Rightarrow r_1 \alpha r_2 \beta x \in P + Q$  And

$r_1 \alpha x \beta r_2 = r_1 \alpha (p + q) \beta r_2 = r_1 \alpha p \beta r_2 + r_1 \alpha q \beta r_2$

where  $r_1 \alpha p \beta r_2 \in P, r_1 \alpha q \beta r_2 \in Q$

$\Rightarrow r_1 \alpha x \beta r_2 \in P + Q$

Now

$x \alpha r_1 \beta r_2 = (p + q) \alpha r_1 \beta r_2 = p \alpha r_1 \beta r_2 + q \alpha r_1 \beta r_2$

where  $p \alpha r_1 \beta r_2 \in P, q \alpha r_1 \beta r_2 \in Q$

$\Rightarrow x \alpha r_1 \beta r_2 \in P + Q$ . Hence P+Q is an ideal of R.

Since  $P \subseteq P + Q, Q \subseteq P + Q$ .

$P+Q \subseteq K$  is obtained based on  $P \subseteq K$  &  $Q \subseteq K$ , when R is the ideal value. Here P and Q is obtained as the smallest value of R which is given as P+Q.

**Note3.16:** A TFSS R which does not satisfy the decomposition property then there exist two ideals P and Q such that R is independent of P+Q.

**Example3.17:** “Let  $R = \{0, r_1, r_2, r_3, r_4, r_5\}, \Gamma = \{\alpha, \beta\}$  define  $\Sigma$  on R as

$\sum_i x_i = \begin{cases} x_j & \text{if } x_i = 0 \forall i \neq j, \text{ for some } j \\ \text{undefined, otherwise} \end{cases}$

Then R is a ternary SO -monoid.

Define the mapping  $R \times \Gamma \times R \times \Gamma \times R \rightarrow R$  as follows:

$\alpha$	0	$r_1$	$r_2$	$r_3$	$r_4$	$r_5$
0	0	0	0	0	0	0
$r_1$	0	0	0	0	0	0
$r_2$	0	0	0	0	0	0
$r_3$	0	0	0	0	0	0
$r_4$	0	0	0	0	0	0
$r_5$	0	0	0	0	0	0

$\beta$	0	$r_1$	$r_2$	$r_3$	$r_4$	$r_5$
0	0	0	0	0	0	0
$r_1$	0	0	0	0	0	$r_1$
$r_2$	0	0	0	0	0	$r_2$
$r_3$	0	0	0	0	0	$r_3$
$r_4$	0	0	0	0	0	$r_4$
$r_5$	0	$r_1$	$r_2$	$r_3$	$r_4$	$r_5$

Then R is a TFSS. In R we have  $r_3 \leq r_4 = r_1 + r_2$  and there exist no  $x, y \in R$  such that  $0 \leq x \leq r_1, 0 \leq y \leq r_2$  and  $r_3 = x + y$  implies that the decomposition property fails. Take  $P = \{0, r_1\}, Q = \{0, r_2\}$ . Then P, Q are ideals of R and  $P+Q = \{0, r_1, r_2, r_4\}$  is not ideal. Since  $r_3 \leq r_4$  and  $r_3 \notin \{0, r_1, r_2, r_4\}$ ”.

**Theorem3.18:** “Let R be a TFSS satisfying the decomposition property then ideal(R) is a distributive lattice”.

**Proof:** Note that ideal(R) together with set inclusion forms a lattice where  $\inf\{I, J, K\} = I \wedge J \wedge K, \sup\{I, J\} = I \vee J$ . Let J, K, L, M are the ideal values of R.

Let  $x \leq p + q$  is obtained for  $x \in (J \wedge K \wedge L) \vee (J \wedge K \wedge M)$

where  $q \in (J \wedge K \wedge M), p \in (J \wedge K \wedge L) \Rightarrow x \leq p + q$  where  $p, q \in J, p, q \in K, p \in W$  and  $q \in Y$ . Since p, q are in J, K and J, K implies the ideals of R that is given as  $p + q \in J \& p + q \in K$ . So  $x \in J, x \in K$ .

Since  $x \leq p + q, p \in W$  and  $q \in M \Rightarrow x \leq p + q \in L + M = L \vee M$ .  $\Rightarrow x \in L \vee M$ . Therefore  $x \in (J \wedge K \wedge L) \vee (J \wedge K \wedge M)$ .

Hence  $(J \wedge K \wedge L) \vee (J \wedge K \wedge M) \subseteq (J \wedge K \wedge L \vee M)$ .

Let  $x \in (J \wedge K \wedge L \vee M) \Rightarrow x \in J, x \in K$  and  $x \in L \vee M$  then by theorem3.11  $L \vee M = L + M$

And the value  $x = p + q$  for some  $p \in L$  and  $q \in M$ , Since we have  $p, q \in J, p, q \in K$  for  $p \leq p + q, q \leq p + q$ . Therefore for  $p \in (J \wedge K \wedge L),$

$q \in (J \wedge K \wedge M)$  the value  $x = p + q \Rightarrow x \in (J \wedge K \wedge L) \vee (J \wedge K \wedge M)$

Thus  $(J \wedge K \wedge L \vee M) \subseteq (J \wedge K \wedge L) \vee (J \wedge K \wedge M)$

Hence  $(J \wedge K \wedge L \vee M) = (J \wedge K \wedge L) \vee (J \wedge K \wedge M)$

**Note3.19:** The decomposition property in a TFSS fails then the lattice of ideals is not distributive for this considers the following example. Consider the TFSS R given in example 3.17 take  $A = \{0, r_1\}, B = \{0, r_2\}, C = \{0, r_3\}, Q = \{0, r_4\}$ . Then  $A \wedge B \wedge A (C \vee D) = \{0, r_1\}$ , whereas  $(A \wedge B \wedge C) \vee (A \wedge B \wedge D) = \{0\}$ .

**Theorem3.20:** “Let R be a CTF-SS R then ideal(R) forms a complete lattice with supremum as  $\vee$  and infimum as  $\wedge$ ”.

**Proof:** Obviously, ideal(R) with set inclusion forms a lattice with  $\{0\}$  as the least element and R as the greatest element  $\{R_i / i \in I\}$  family of ideals of R,  $\bigwedge_{i \in I} R_i$  and  $\bigvee_{i \in I} R_i$  are ideals

of R. So  $\inf\{R_i / i \in I\}$  and  $\sup\{R_i / i \in I\}$  are in ideal(R) and hence ideal (R) is a complete lattice.

**Theorem3.21:** “For any ideals A, B, C, D of CTF-SS R,  $A \Gamma B \Gamma (C \vee D) = (A \Gamma B \Gamma C) \vee (A \Gamma B \Gamma D)$ ”.

**Proof:** Let  $x \in A \Gamma B \Gamma (C \vee D)$  then  $x \leq \sum_i a_i \alpha_i b_i \beta_i c_i$  for some  $a_i \in A, b_i \in B, c_i \in C \vee D$  and  $\alpha_i, \beta_i \in \Gamma$ . Since  $c_i \in C \vee D, c_i \leq d_i + e_i$  for some  $d_i \in C$  and  $e_i \in D$ . So  $x \leq \sum_i a_i \alpha_i b_i \beta_i (d_i + e_i) \Rightarrow x \leq \sum_i a_i \alpha_i b_i \beta_i d_i + \sum_i a_i \alpha_i b_i \beta_i e_i$  where  $a_i \in A, b_i \in B, d_i \in C, e_i \in D$  and  $\alpha_i, \beta_i \in \Gamma. \Rightarrow x \in (A \Gamma B \Gamma C) \vee (A \Gamma B \Gamma D)$ .

Conversely if  $x \in (A \Gamma B \Gamma C) \vee (A \Gamma B \Gamma D)$  then  $x \leq x_1 + x_2$  where  $x_1 \in A \Gamma B \Gamma C$  and  $x_2 \in A \Gamma B \Gamma D$

Since  $x_1 \in A \Gamma B \Gamma C, x_1 \leq \sum_i a_i \alpha_i b_i \beta_i c_i$  for some  $a_i \in A, b_i \in B, c_i \in C$  and  $\alpha_i, \beta_i \in \Gamma$

Since  $x_2 \in A \Gamma B \Gamma D, x_2 \leq \sum_j d_j \gamma_j e_j \delta_j f_j$  where  $d_j \in A, e_j \in B, f_j \in C$  and  $\gamma_j, \delta_j \in \Gamma$ .

Therefore  $x \leq \sum_i a_i \alpha_i b_i \beta_i c_i + \sum_j d_j \gamma_j e_j \delta_j f_j \leq \sum_i \sum_j (a_i + d_j)(\alpha_i + \gamma_j)(c_i + f_j)(\beta_j + \delta_j)(b_i + e_j)$

Where  $(a_i + d_j) \in A, (b_i + e_j) \in B, (c_i + f_j) \in C \vee D$  and  $(\alpha_i + \gamma_j), (\beta_i + \delta_j) \in \Gamma$

$\Rightarrow x \in A \Gamma B \Gamma (C \vee D)$  and hence

$A \Gamma B \Gamma (C \vee D) = (A \Gamma B \Gamma C) \vee (A \Gamma B \Gamma D)$

#### IV. CONCLUSION

Mainly we introduced in this paper about regular TFSS and characterized TFSS. In this paper we introduce the notions of subtractive and strong subsets in partial ternary  $\Gamma$ - semirings. We conclude that join of any two ideals is equal to the sum of those two ideals in a TFSS

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