

ECG Denoising using Modified-NLMS Multi band Structured Sub band Adaptive Algorithm

B.Bhaskara Rao, B.Prabhakara Rao

Abstract: Electrocardiogram (ECG) is the procedural electrical action of the heart that emerges from the heart muscle's electrophysiological design. In any case, in clinical environment all through procurement, the ECG flag is debased with various assortments of artifacts. The analysis of ECG records permits the consultants to identification many viscus disorders. However, the accuracy of such diagnostic depends on the signal quality. To effectively correct associated to preserve more underlying parts of an ECG record a powerful tool for elimination of artifact from ECG was introduced. In this research paper a brand new ECG enhancement style exploitation multiband structured sub band adaptive filter (MSAF) is built to unravel structured issues in typical sub band adaptive filter (SAF). The proposed approach is established on integrating the Modified NMLS (MNLMS) adaption technique with SAF. This paper investigates the new detailed adaptive noise canceller (ANC) system for ECG signals with lustiness based mostly on uniform filter bank (UFB) and non-uniform filter bank (NUFB) structured MSAF using MNLMS adaptive algorithm. Computer simulation demonstrates that the projected system provides improved performance and achieves good adaptation. NUFB structured MSAF algorithms are applied on graphical records obtained from standard Massachusetts Institute of Technology-Beth Israel Hospital (MIT-BIH) information base and the performance is compared with UFB structured MSAF algorithms in terms of parameters signal-to-noise ratio before filtering (SNRBF) and signal-to-noise ratio after filtering (SNRAF). The Post -SNR values for various NUFB structured MSAF's was found to be higher than the UFB structured MSAF's.

Index Terms: ANC, ECG, MSAF, MNLMS, NUFB, SNRBF, SNRAF, UFB.

I. BACKGROUND

Our bodies are continuously speaking data about our health. These facts can be trapped through physiological devices that estimate heart rate, blood pressure, oxygen saturation degrees, blood glucose, nerve conduction, brain interest and so on. Electrocardiogram (ECG) is a illustration of the electric hobby of cardiac tissue at some point of systole and diastole. This signal is generally acquired by way of measuring the electrical potential between particular spatial combinations of recording electrodes [1, 2].

Electrocardiography is the process of recording the electrical action of the coronary heart around duration of time

using electrodes positioned over the skin. General goal of appearing an ECG is to gain information about the shape and Characteristic of the heart. Clinical uses for these records are numerous and usually need information of the shape and/or Characteristics of the heart to be interpreted. An ECG tracing is affected by affected person motion. Artifacts are distorted signals resulting from secondary internal or external sources, along with power line interference (PLI), baseline wander (BW), Electromyography noise or muscle artifact (MA) and electrode movement (EM) [3]. Distortion poses large demanding situations to healthcare companies, who hire diverse techniques and strategies to securely understand those false indicators. Accurately keeping apart the ECG artifact from the true ECG signal could have a tremendous effect on patient outcomes and legal liabilities. The artifact elimination in biomedical applications could be very crucial to discriminate the important desired signal capabilities in interference. Diverse adaptive systems are initiated for interference elimination. Figure.1 defines the essential downside and noise cancelling answer [4, 5].

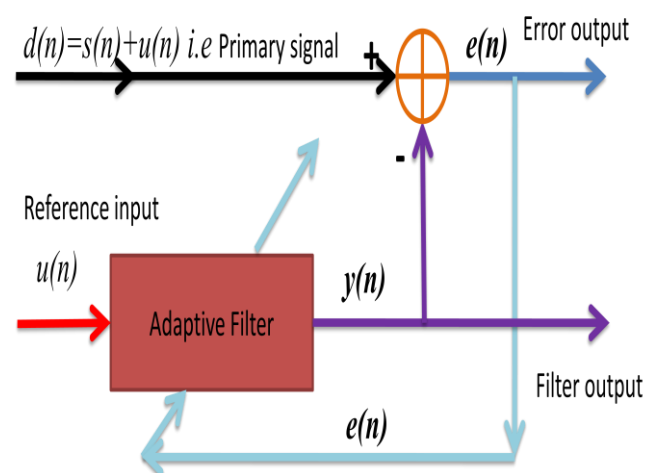


Figure.1: Basic diagram of Adaptive Noise Canceller

In order to eliminate artifact from ECG the clean ECG $s(n)$ is added with a interference $n_1(n)$ which is uncorrelated with the $s(n)$. The predominant input to the ANC is noise contaminated signal $d(n)$ i.e. $s(n)+n_1(n)$. If $n_2(n)$ is another noise/artifact generated from noise source that is unrelated with the $s(n)$ however correlative with $n_1(n)$ that supplies reference input to ANC that is filtered to produce the estimate signal $y(n)$ that's a detailed duplicate of reference input. The response of the adaptive filter $y(n)$ is subtracted from $d(n)$ to yield the error function as shown in equation (1). This adaptive filter can be realized using various structures; the most frequently used structure is transversal finite impulse response (FIR) [6,7].

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$$e(n)=d(n)-y(n) \quad (1)$$

The adaptive filter extricates the signal or abolishes artifact by iteratively minimizing the minimum mean square error (MSE).

Traditional filters such as adaptive filters [8,9,10], sign based normalised adaptive filters [11] were initiated in the literature to minimise interference/artifacts. Dissimilar practices for ECG denoising with new variable step size NLMS [12] and EEMD-BLMS methods [13]. Promising performance are acquired by non linear adaptive algorithms [14, 15, 16], recently hybrid techniques have been proposed to suppress artifact from ECG signals using cascaded adaptive filters [17,18].

Filter banks had been delivered in an attempt to upgrade the behaviour of time area adaptive filters. The main upgrades are faster convergence and the low computational complexity due to shorter adaptive filters within the sub bands, running at a lower sampling rate. Filter banks (FB) break down an advanced signal into numerous sub band groups. Based totally on time frequency resolution, FB's can be arranged into two categories *i.e.*, uniform filter banks (UFB) and non uniform filter banks (NUFB) [19,20]. Various techniques for disintegrating indicators in to sub groups have turned out to be unmistakable and had been proposed inside the literature [21, 22].

Sub band adaptive filtering (SAF) typically employs multirate filter banks for signal decomposition and reconstruction. This approach allows for instant convergence and decreased computational complexity through use of the robust adaptive algorithms. Currently high-quality artifact elimination techniques are proposed using SAFs comprise variable step size SAF [23], Variable individual step size SAF [24], new standardized SAF [25]. An enhanced cosine modulated NUFB configuration approach has been proposed by Kumar,A.,G K Singh et., all [26]. In customary SAF's each bound uses an individual adaptive sub filter in its personal unique adaption that declines the convergence rate. To solve these structured problems a multiband structured SAF (MSAF) are developed in which the entire band adaptive filter tap weight vectors are updated by a single adaptive algorithm the use of sub band signal [20, 27]. The non-uniform filter bank SAF (NUFBSAF) is developed to procure a higher convergence behaviour with the aid of adapting the band width of analysis filters through proper choice of decimation factors. The goal of this paper is to broaden non uniform multi band structured sub band adaptive filter out that could intensify the overall performance of the traditional ANC design, to examine the application of SAF to noise cancellation hassle in ECG.

II. SUB BAND ADAPTIVE FILTERING METHOD

Sub band adaptive filtering improves convergence under colored signals. LMS is most generally used adaptive algorithm than recursive least square algorithm and kalman filtering algorithm which makes use of a gradient vector to approximate a non stationary signal. A FB incorporates a set of analysis filters which decomposes the input signal of bandwidth into sub band signals. The sub bands supply records from extraordinary frequency bands thus; it is conceivable to function time and frequency based processing of the input signal. A common objective is to create one arrangement of preprocessing filters which is useful in a noise cancellation tasks for ECG processing. In this manner,

a sub band coding based totally adaptive algorithm calculation involves decomposing a signal into frequency sub bands and managing these sub bands as indicated by the current application.

The concept of multiband structured-sub band adaptive filter (MSAF) is introduced in this section. In the proposed design the desired/primary input given to the first SAF consists of noise contaminated ECG record denoted as $d(n)$ in Figure.2. The secondary signal given to second SAF is noise signal $n_2(n)$ denoted as $u(n)$. The full band input signal $u(n)$, primary input signal or desired response signal $d(n)$ and filter estimated signal $y(n)$ are decomposed into N sub bands by means of analysis filters $H_i(z)$; for $i=0,1,2,...(N-1)$. In this Figure.2 $H_0, H_1, H_2, ..., H_{N-1}$ and $F_0, F_1, F_2, ..., F_{N-1}$ are analysis & synthesis filters of N channel perfect reconstruction (PR) filter bank respectively. These sub band signals are decimated to a lower rate using same factor and are processed by individual sub band adaptive sub filters $W_i(z)$. [20]

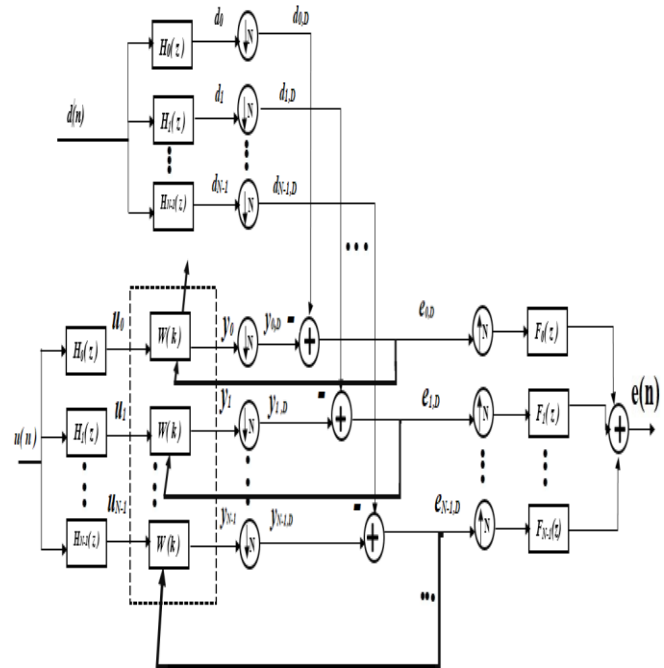


Figure.2: Block diagram of MSAF (from Reference [20])

Non uniform filter banks have non uniform frequency partition. One technique of constructing NUFB is to cascade UFB in a tree structure using a two channel FB as elementary building blocks. The distinct gain of the equivalent structure of the tree-structured FB is the possibility of realizing analysis and synthesis filters for extra vital tasks than easy band separation [19]. As an instance of this method, NUFB with decimation elements (16,16, 8,4,2) is illustrated. The proposed tree-structured non uniform filter bank's analysis section is shown in Figure.3.

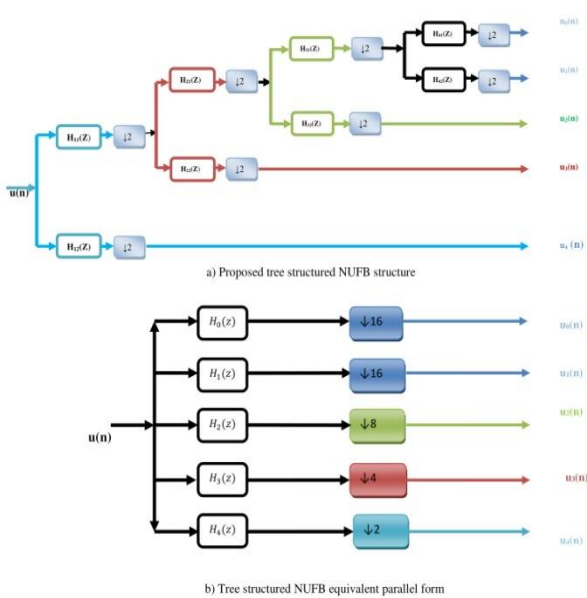


Figure.3: Proposed block diagram of (a) tree structured NUFB & (b) equivalent NUFB parallel form

The proposed structure makes use of low pass FIR filter with filter length 32, cut off frequency 100 Hz and sampling frequency 360 Hz design in both analysis and synthesis FB that give near-perfect reconstruction by permitting little measure of distortion at the output. $H_0(z)$ is the transfer function of FIR filter i.e the frequency response of low pass FIR filter and $h(n)$ is the impulse response of $H_0(z)$ or initial FIR filter numerator polynomial coefficients which are generated by using Walsh-Hadamard transformations. These filter coefficients satisfies linear phase condition. Walsh-Hadamard transformation codes are the most common fixed length orthogonal codes used in CDMA applications. A set of Walsh codes of length 'P' consists of the P rows of an P by P Walsh matrix. The generalized structure of N-channel NUFB based on tree structured procedure having decimation $N_0, N_1, N_2 \dots N_{N-1}$ for each band then the decimation factors must fulfill the accompanying condition [21].

$$\sum_{k=0}^{N-1} \frac{1}{N_k} = 1 \quad (2)$$

In N-channel NUFB the PR is possible if

$$\sum_{k=0}^{N-1} |H_k(e^{jw})|^2 = 1 \quad \text{for } 0 \leq w \leq \frac{\pi}{N} \quad (3)$$

Where $H_k(e^{jw})$ is frequency response of k^{th} filter in equivalent NUFB parallel form For tree structured NUFB design having decimation factors (16,16,8,4,2) the PR condition can be achieved by using following equation

$$|H_0(e^{jw})|^2 + |H_1(e^{jw})|^2 + |H_2(e^{jw})|^2 + |H_3(e^{jw})|^2 + |H_4(e^{jw})|^2 = 1 \quad \text{for } 0 \leq w \leq \frac{\pi}{5} \quad (4)$$

Here $H_0(z), H_1(z), H_2(z), H_3(z), H_4(z)$ analysis filters with the following relations[21]

$$H_0(z) = H_{11}(z)H_{21}(z^2)H_{31}(z^4)H_{41}(z^8) \quad (5)$$

$$H_1(z) = H_{11}(z)H_{21}(z^2)H_{31}(z^4)H_{42}(z^8) \quad (6)$$

$$H_2(z) = H_{11}(z)H_{21}(z^2)H_{32}(z^4) \quad (7)$$

$$H_3(z) = H_{11}(z)H_{22}(z^2) \quad (8)$$

$$H_4(z) = H_{12}(z) \quad (9)$$

Where $H_{11}, H_{21}, H_{31}, H_{41}$ are low pass filters in the first, second, third and fourth stages respectively and $H_{12}, H_{22},$

H_{32}, H_{42} are high pass filters in the first, second, third and fourth stages respectively. To evaluate performance MSAF's various UFB & NUFB structured such as three channel with decimation factors (3,3,3) UFB (TCUFB), three channel with decimation factors (4,4,2) NUFB (TCNUFB), four channel with decimation factors (4,4,4,4) UFB (FCUFB), four channel with decimation factors (8,8,4,2) NUFB (FCNUFB), five channel with decimation factors (5,5,5,5,5) UFB (FVCUFB) and five channel with decimation factors (16,16,8,4,2) NUFB (FVCNUFB) using different adaptive algorithms.

III. MSAF WITH MODIFIED NLMS ALGORITHM

The traditional ANC shown in Figure.1 incorporates filter whose input parameters are $d(n)$ and $u(n)$. Here $u(n)$ is the time delayed input vector

$$u(n) = [u(n), u(n-1), u(n-2), \dots, u(n-M+1)]^T,$$

$w(n) = [w_0(n), w_1(n), w_2(n), \dots, w_{M-1}(n)]^T$ represents the numerator polynomial coefficients of the filter at time index n . Figure.2 shows two equivalent structures for the selected input portion of the multiband system as indicated that the full band adaptive filter $W(z)$ of length M is stationary (i.e. the adaptation is frozen), it can be transposed with the analysis filter bank as each sub band signal occupies only a segment of the original frequency range. The N sub band signals of MSAF algorithms require-particular computational steps in every emphasis as takes after [20]. It is significant to note that n denotes the time index of original sequence & decimated signal time index is denoted by k .

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Proposed algorithm summary

For $s = 1, 2, \dots, N$ where s is stages

Analysis filters $H_i(z)$

for $i = 0, 1, 2, \dots, N-1$

$$H_i(z) = H_{s,i}(z^{s-i}) \cdot (z^{s-i}) \cdot (z^{s-i}) \dots H_{s,i}(z^{s-i})$$

$$H_{i+1}(z) = H_{s,i}(z^{s-i}) \cdot (z^{s-i}) \cdot (z^{s-i}) \dots H_{s,h}(z^{s-i})$$

For $k = 0, 1, 2, \dots, kN$ where $kN = n$

Error estimation:

$$e_D(k) = d_D(k) - U^T(k)w(k)$$

Normalization matrix:

$$\Lambda(k) = \text{diag}[U^T(k)U(k) + \alpha]$$

Tap-weight adaptation:

$$w(k+1) = w(k+1) + \mu U(k)\Lambda^{-1}(k)e_D(k)$$

Input signal Band partitioning:

$$U_1^T(k) = H^T A(kN)$$

Desired signal Band partitioning:

$$d_D(k) = H^T A(kN)$$

Synthesis:

$$e(kN) = F e_D(k)$$

Parameters:

L & h - Basic Low pass & high pass filter notation

M - Number of adaptive tap weights

N - Number of sub bands

L - Length of the analysis and synthesis filters

Variables:

$$U^T(k) = [U_1^T(k), U_2^T(k-1)].$$

$$U_2^T(k-1) - \text{first } M-N \text{ columns of } U^T(k-1)$$

$$A(kN) = [a(kN), a(kN-1), a(kN-2), \dots, a(kN-N+1)]$$

$$a(kN) = [u(kN), u(kN-1), u(kN-2), \dots, u(kN-L+1)]^T.$$

$$d(kN) = [d(kN), d(kN-1), d(kN-2), \dots, d(kN-L+1)]^T.$$

This basic principle is used to design a constraint optimization criterion for deriving the adaptive algorithm. In the MSAF shown in Figure.2 with the sub band signals sets $\{U(k), d_D(k)\}$, a criterion that ensures convergence to the optimum solution after a adequate number of iterations is to have the updated tap weight vector $w(k+1)$ in all N sub bands at each iteration k as follows

A) Modified Normalized Least Mean Square (MNLMS) Algorithm

$$w(k+1) = w(k) + \mu \frac{u_i(k)}{\|u_i(k)\|^2 + \alpha} e_{i,D}(k) \quad (10)$$

Where μ is learning rate parameter and it should be selected in the stability bound i.e $0 < \mu < \frac{2}{N*P_u}$, here $P_u = u^T(n)u(n)$ and α is a small positive constant used to avoid possible division by zero. These algorithms replace the filter coefficients of sub band adaptive filter the usage of the following equation.

$$w(k+1) = w(k) + \mu G(k)U(k)\Lambda^{-1}(k)e_{i,D}(k) \quad (11)$$

Where $\Lambda(k)$ is normalization matrix

$$\Lambda(k) = \text{diag}[U^T(k)U(k) + \alpha] \quad (12)$$

The filter coefficients or weight vectors of the filter are changed for the next iteration for Modified Normalised Least Mean Square (MNLMS) depending on $w(k)$. Here $w(k)$ is Walsh-Hadamard transformation matrix defined as follows

$$w_{2P} = (w_P \ w_P; w_P - w_P); \quad (13)$$

Here initial $w_1 = I$ and P is the dimension of the matrix.

IV. RESULTS & DISCUSSION

In this simulation the Physionet website MIT-BIH arrhythmia database [28] was utilized to take a look at the execution of various UFB & NUFB structured MSAF's adaptive algorithms for ECG denoising. The recordings had been sampled at 360 samples per seconds with 11-bit resolution over a 10 mV range. 'Mat' files of ECG data were used from the database to load into MATLAB. The simulations have been executed by using accumulating 3600 samples of ECG. A records set of 5 ECG records: data100, data105, data108, data203 and data228 are considered to guarantee the consistency of the results. The secondary noise signal $n_2(n)$ shown in Figure.1 is taken from noise generator. In order to check the filtering potentiality in shift variant domain a synthetic PLI, artificial BW, real muscle artifacts and real electrode motion artifacts with 3600 array size are taken from Physionet website MIT-BIH normal sinus rhythm database (NSTDB) [29]. The performance of proposed UFB and NUFB structured MSAF adaptive noise cancellation systems are compared by quality assessment parameters signal-to-noise ratio before filtering (SNRBF) and signal-to-noise ratio after filtering (SNRAF) are outlined as follows.

$$SNR \text{ Before filtering} = 10 \log_{10} \left(\frac{\sum_{n=0}^{N-1} |s(n)|^2}{\sum_{n=0}^{N-1} |d(n) - s(n)|^2} \right) \quad (14)$$

$$SNR \text{ After filtering} = 10 \log_{10} \left(\frac{\sum_{n=0}^{N-1} |s(n)|^2}{\sum_{n=0}^{N-1} |e(n) - s(n)|^2} \right) \quad (15)$$

Table.1. SNR (in dB) obtained by applying UFB and NUFB structured SAF's using MNLMS algorithms

Type of Artifact	Type of FB	Rec.No 100	Rec.No 105	Rec.No 108	Rec.No 203	Rec.No 228	Avg. Val
PLI	SNRBF	0.2144	0.712	-0.0059	2.9671	-1.0532	0.56688
	TCUFB	16.3719	16.4944	16.2976	17.2302	16.0925	16.49732
	FCUFB	17.9727	18.0984	17.9218	18.6091	17.8072	18.08184
	FVCUFB	17.3967	17.5185	17.3397	18.0974	17.1878	17.50802
	TCNUFB	21.4798	21.5736	21.4448	22.0147	21.3507	21.57276
	FCNUFB	19.4775	20.0189	19.3838	21.1584	19.1374	19.83514
	FVCNUFB	22.8367	22.3902	22.8692	23.773	22.0445	22.78272
BW	SNRBF	5.8558	3.5196	8.5884	2.524	9.1149	5.92054
	TCUFB	8.8078	6.9116	10.8087	6.209	11.49	8.84542
	FCUFB	8.19	6.6061	10.4334	6.1044	10.7709	8.42096
	FVCUFB	8.6402	7.1406	10.8305	5.9152	11.0596	8.71722
	TCNUFB	10.5667	9.2235	12.9634	8.2884	13.5013	10.90866
	FCNUFB	13.0221	11.9046	15.5653	11.1224	15.8109	13.48506
	FVCNUFB	19.7958	17.4199	21.5669	15.939	22.6482	19.47396
EM	SNRBF	3.6096	4.1072	6.521	6.3623	2.342	4.58842
	TCUFB	16.2509	14.1066	8.9615	12.4623	13.1471	12.98568
	FCUFB	16.5984	14.5366	9.2073	12.8888	13.495	13.34522
	FVCUFB	16.7281	14.5181	9.1277	12.766	13.6919	13.36636
	TCNUFB	18.7811	16.7365	11.463	15.1281	15.6005	15.54184
	FCNUFB	21.8703	19.8173	14.4517	18.2009	18.608	18.58964
	FVCNUFB	25.6934	22.3742	17.4809	19.695	23.3621	21.72112
MA	SNRBF	4.1514	4.6489	7.0628	6.904	2.8837	5.13016
	TCUFB	14.9317	14.308	9.2159	13.0591	12.743	12.8515
	FCUFB	15.2808	14.7296	9.4417	13.4921	13.0665	13.2021
	FVCUFB	15.4517	14.6708	9.3951	13.3694	13.3065	13.2387
	TCNUFB	13.3965	12.3752	8.4101	10.8585	12.2425	11.4566
	FCNUFB	16.2377	15.549	11.277	13.933	15.0395	14.4072
	FVCNUFB	22.285	19.661	16.147	16.905	21.776	19.3547

Average SNR values shown in Table.1 are acquired by using averaging record numbers. 100m, 105m, 108m, 203m and 228m procured from MIT-BIH database. Table.1 shows the SNR values obtained for different recordings of MIT-BIH data base. The SNR values calculated by applying UFB and NUFB structured SAF's using MNLMS algorithm. As shown in Table 1 . Average SNR's for 5 records obtained by applying UFB and NUFB structured SAF's using MNLMS algorithms for PLI noise has **22.78272** dB, for BW artifact has **19.47396** dB, for EM noise has **21.72112** dB and for Muscle artifact has **19.3547** dB. The computer simulations state that NUFB structured MSAFs has appreciable effectiveness than UFB structured MSAFs. Various artifact cancellations using MNLMS adaptive filtering are shown in Figures 4-7 for MIT-BIH record number 105m, by evaluating the range of data samples and magnitude (in milli volts) on x-axis and y-axis respectively. The same technique can be applied on the different MIT-BIH data base recordings with different UFB and NUFB structured SAF's. For convenience the results of only one record using only one FVCNUFB structured sub band adaptive filter are depicted in figures.



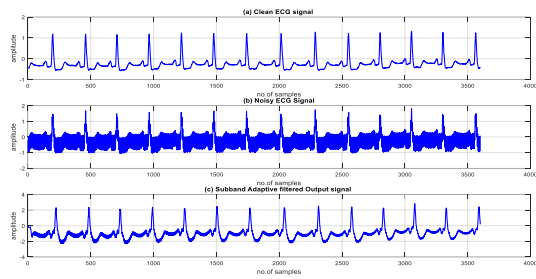


Figure.4: PLI cancellation using MSAF using MNLMS (a) clean ECG (b) PLI noise corrupted ECG (c) FVCNUFB structured Sub band adaptive filtered signal using MNLMS algorithm.

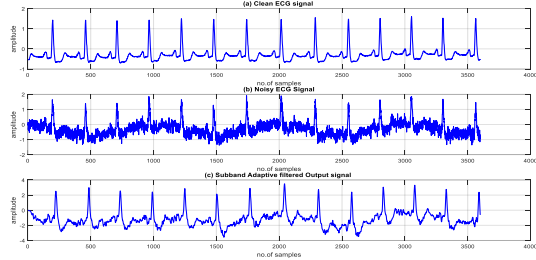


Figure.5: Adaptive filtering simulation of BW artifact removal (a) clean ECG (b) BW noise corrupted ECG (c) FVCNUFB structured sub band adaptive filtered signal using MNLMS algorithm.

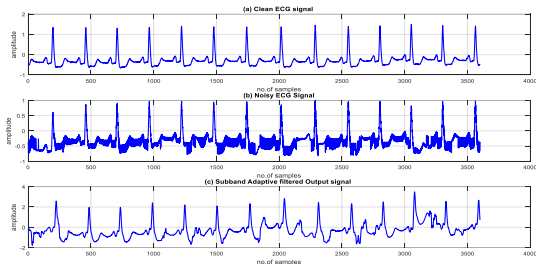


Figure.6: Adaptive filtering simulation of EM artifact cancellation (a) clean ECG (b) EM artifact corrupted ECG (c) FVCNUFB structured Sub band adaptive filtered signal using MNLMS algorithm.

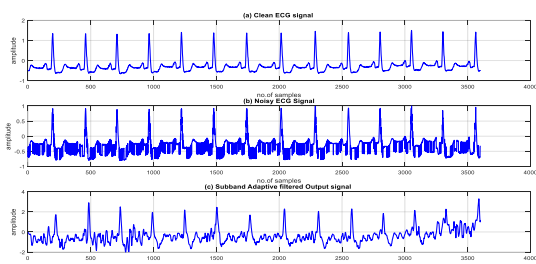
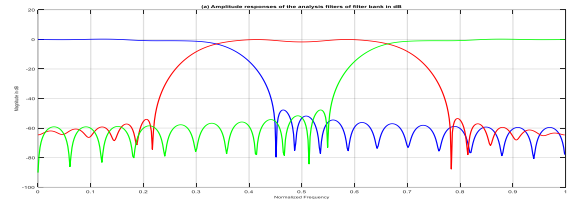
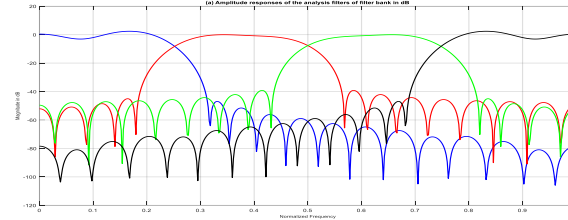


Figure.7: Adaptive filtering simulation of MA removal (a) clean ECG (b) Muscle artifact corrupted ECG (c) FVCNUFB structured Sub band adaptive filtered signal using MNLMS algorithm.

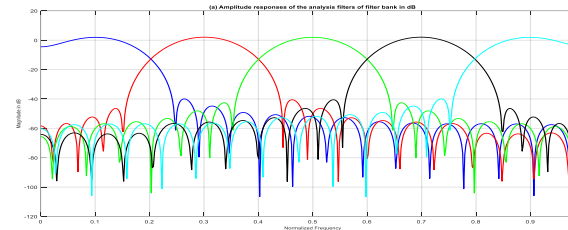
The frequency response simulation results of a proposed method with proto type filter for UFB structured SAF's and NUFB structured SAF's are shown in Figure.8.



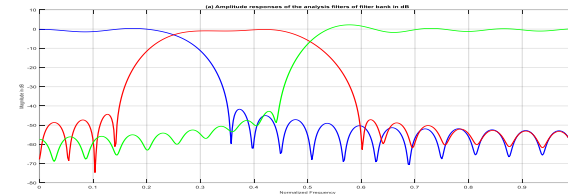
(a) Magnitude spectrum of TCUFb



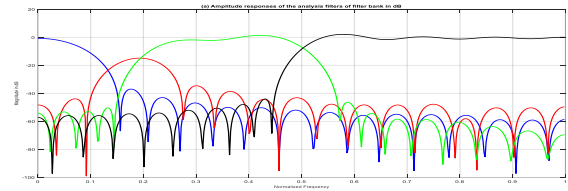
(b) Magnitude spectrum of FCUFb



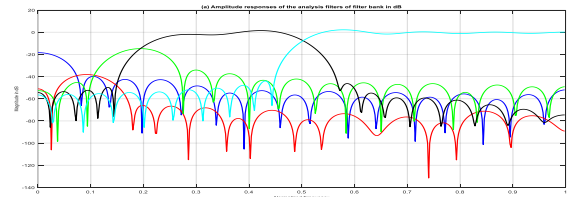
(c) Magnitude spectrum of FVCUFb



(d) Magnitude spectrum of TCNUFB



(e) Magnitude spectrum of FCNUFB



(f) Magnitude spectrum of FVCNUFB

Figure.8: The frequency response of a proposed UFB structured SAF's and NUFB structured SAF's

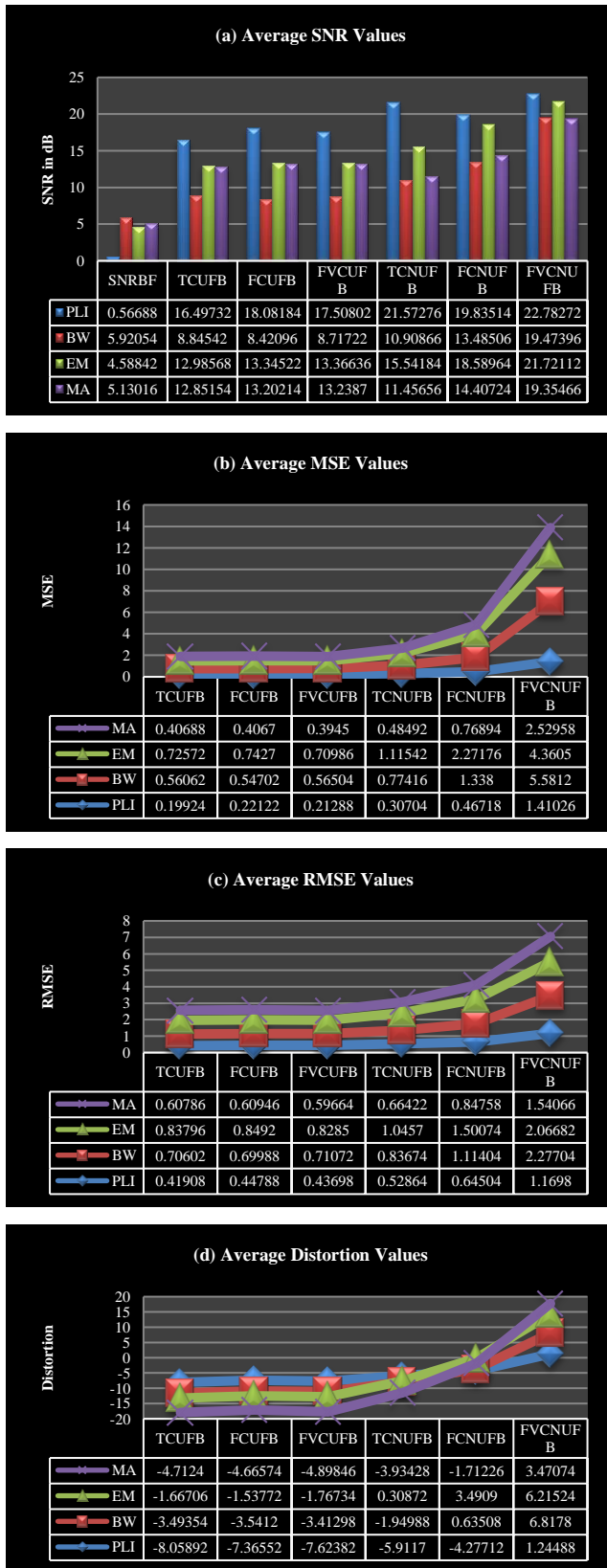


Figure.9: Artifact cancellation Using UFB& NUFB structured Sub band adaptive MNLMS algorithm simulation results (a) Average SNR values (b) Average MSE values (c) Average RMSE values (d) Average Distortion values

The perfect reconstruction error (PRE) simulation results of a proposed method with proto type filter for UFB structured SAF's and NUFB structured SAF's using MNLMS adaptive algorithms are shown in Figure.9.

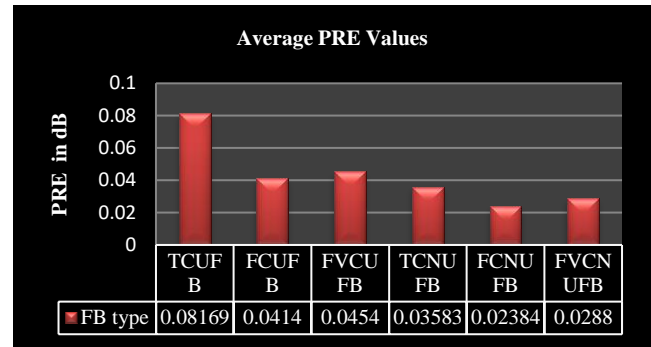


Figure.10: The peak reconstruction error (PRE) values

The perfect reconstruction error (PRE) is decreased appreciably. The average PRE got in FVCNUFB is 0.0288dB. The simulation results of a proposed method the usage of MNLMS adaptive algorithms with proto type filter for three channel, four channel and five channel UFB's and NUFB's are shown in above Figure.7. The average PRE obtained for three channel, four channel and five channel UFB's are 0.08169 dB, 0.0414 dB and 0.0454dB respectively. The average PRE obtained for three channel, four channel and five channel NUFB's are 0.03583 dB, 0.0238393 dB and 0.0288 dB respectively. The PRE values shown in table depict that the FCNUFB has minimum PRE compared to the remaining algorithms.

V. CONCLUSIONS

This research paper presents the new comprehensive ANC system of ECG signals with robustness based on UFB & NUFB structured MSAF's using Modified NLMS adaptive algorithms. The theoretical analysis of NUFB structured MSAF system is carried out and simulations are performed. The performance of the proposed design a comparison has been made between six different ECG denoising schemes *i.e* three channel, four channel and five channel UFB & NUFB structured SAFs using Modified NLMS adaptive algorithms respectively. The performance of proposed system is compared quantitatively by parameter SNR. Better filtering performance results are obtained by NUFB structured SAF MNLMS adaptive algorithm and also these algorithms guarantee the better estimation of noise. Computer simulation demonstrates that the proposed system gives improved performance and achieves good adaptation. The SNR for various NUFB structured SAF's was found to be higher than the UFB structured SAF's. The five channel NUFB structured SAF performs better SNR values than UFB structured SAF using MNLMS.

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