# Calculating Development of Cracks in Roller-Compacted Concrete Gravity Dams based on Self-Adaptive Finite Element Method in Ansys Software

Quang Hung Nguyen, Hoang Hung Vu, Thanh Duong Ha

Abstract: Using ANSYS mechanical APDL, the authors have developed a program to calculate formation of cracks and development of cracks in roller-compacted concrete gravity body dams based on self-adaptive finite element method with grid elements which are subjected to static and dynamic loading capacity. The reliability of the program has been validated through some experimental results found in the literature. Using the program, the authors have also carried out to calculate the crack development of Son La RCC dam under loading capacity combination of earthquakes. The results show some effects of the cracks development to the loading capacity of RCC dams.

Keywords—ANSYS-APDL, crack development, RCC dams, self-adaptive finite element, Son La dam.

#### I. INTRODUCTION

There are now many ways to simulate development process of cracks under effect of superimposed loading capacity or dynamic loading capacity. One of the first researches are mentioned, which is the research of Swartz et al.[1] executed in 1990. The calculation of cracks development by the self-adaptive finite element method of Swartz et al.[1] with the mesh of self-adaptive finite element method was not changed during the destructive process. Many studies on the development of this model applied the mesh of self-adaptive finite element method in the development process of cracks. At each step of superimposed loading capacity, the the mesh of self-adaptive finite element will be altered. After cracks in the integral point will be adjusted through the material properties to simulate cracking, the cracking method uses a distributed model that is not a discrete model. [2], [3]. Based on the APDL parametric programming language in ANSYS software (ANSYS Parametric Design Language), the author has developed a "RCCD CRACK Calculation Program", its aims is to calculate the cracks formation, and develop the cracks in the body of dam with roller-compacted concrete gravity based on self-adaptive finite element method with the mesh of element that is influenced by dead loading capacity and dynamic loading capacity. From there, it is the basis for studying the effect of cracks on the dam's loading capacity

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**Quang Hung Nguyen**, Thuy Loi, University, Hanoi, Vietnam. **Hoang Hung Vu**, Thuy Loi University, Hanoi, Vietnam. **Thanh Duong Ha**, Thuy Loi University, Hanoi, Vietnam. and the gravity of the roller-compacted concrete (RCC).

#### II. THEORY

# A. Basic equations

Dynamic equations for the FE regions of solid can be expressed in the incremental form as:

$$[M_d] \{\Delta u_d^{\mathsf{A}}\}_n + [C_d] \{\Delta u_d^{\mathsf{A}}\}_n + [K_d] \{\Delta u_d\}_n = \{\Delta P_{df}\}_n + \{\Delta P_{dr}\}_n$$

$$\tag{1}$$

Where [M] and [K] are the mass and stiffness matrices; [C] is the Rayleigh damping matrix that is a linear combination of the mass and stiffness matrices;  $\{\Delta P\}$  are the incremental vectors representing the dam-foundation, dam-reservoir,  $\{\Delta u\}$  are the incremental displacement vectors; the subscript n denotes a time step. In this study, Newmark  $\beta$  scheme is used to approximate the derivatives:

$$\begin{aligned}
\left\{\Delta u \right\}_{n} &= \frac{1}{\beta \Delta t^{2}} \left\{\Delta u\right\}_{n} - \frac{1}{\beta \Delta t} \left\{u \right\}_{n} - \frac{1}{2\beta} \left\{u \right\}_{n} \\
\left\{\Delta u \right\}_{n} &= \frac{\delta}{\beta \Delta t} \left\{\Delta u\right\}_{n} - \frac{\delta}{\beta} \left\{u \right\}_{n} - \frac{\delta - 2\beta}{2\beta} \left\{u \right\}_{n} \Delta t
\end{aligned} \tag{2}$$

Where  $\Delta t$  is time interval,  $\gamma$  and  $\beta$  are integration parameters. Equation (1) can be solved by the Newmark  $\beta$ -method. According to this method, equation (1) is rewritten as:

$$\left[\frac{1}{\beta \Delta t} [M_d] + \frac{\delta}{\beta \Delta t} [C_d] + [K_d] \right] \{\Delta u\}_n = \left[D_f\right] \{\Delta F\}_n + \left[\frac{1}{2\beta} [M_d] + \frac{\delta - 2\beta}{2\beta} [C_d] \Delta t\right] \{\mathcal{A}\}_n + \left[\frac{1}{\beta \Delta t} [M_d] + \frac{\delta}{\beta} [C_d] \right] \{\mathcal{A}\}_n \tag{3}$$

Where  $\Delta t$  is time interval,  $\delta$  and  $\beta$  are integration parameters and the subscript t denotes a time step.

# B. Smeared crack model of concrete

The nonlinear tensile behavior of concrete is represented by the smeared crack model [4]. The initiation and propagation of cracking are based on the strength criterion. The principal stress of an element is checked in terms of a bilinear failure criterion. If the failure criterion is met, cracking takes place

over the element in the direction normal to the maximum principal stress. After cracking, the stiffness



of the concrete normal to the crack plane is reduced to zero and the concrete model becomes orthotropic. When the strain normal to the crack plane is less than zero, the crack is considered to become closing and the concrete recovers its original stiffness in the direction normal to crack plane without the tensile strength recovered. Any tensile stress normal to the closed crack will bring about reopening of the crack.

# III. PROGRAMMING THE CALCULATION ON DEVELOPMENT OF THE CRACK IN THE BODY OF DAMS WITH ROLLER-COMPACTED CONCRETE GRAVITY BY THE PROGRAMMING LANGUAGE OF APDL PARAMETER.

# A. Structural simulation of the roller-compacted concrete dams

The highlight of ANSYS software is the ability to use the parametrization language to design the APDL (a type of FORTRAN programming language) that programmatically generates a general problem based on predefined parameters [5].

For the cross-sections of the dams with normal concrete gravity, these are classified into five material areas, and the ground is divided into horizontal geologic layers [6]. Depending on the specific problem to choose the corresponding size.

The stimulation of the dam 's structure in terms of stereometrical problem by finite element method consists of two types of elements:

- The element of dam's body is the SOLID65 block element, which simulates the material properties of the concrete.
- The foundation elements are SOLID45 block elements simulating the characteristics of foundation.

Simulating the dam's structure using adaptive mesh under finite element method, all input data is made through the user interface, which is very convenient and easy to test. [7-9]

### B. Checking the reliability of the program

For the purpose of assessing the reliability of the "RCCD\_CRACK Calculation Program" in the APDL programming language, the authors calculated the stress, deformation and fracture strength of the Koyna-India gravity dam with the conic cross section size. The Koyna gravity Dam is one of the few concrete dams in the world that was damaged during the earthquake. Historical acceleration - the time of the Koyna earthquake recorded in 1967 in the vertical and horizontal directions, shown in **Fig.** 2 [3]. Many studies in the world have performed computational and empirical simulations and experimental research on the destruction of the dam. A typical example is a recent research of Mridha S in 2014 [2].

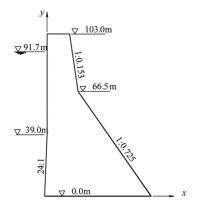


Fig. 1. Cross section of the Koyna dam - India

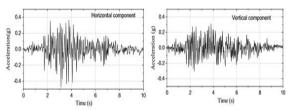


Fig. 2. Koyna earthquake in November 1967

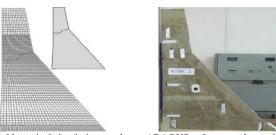


Fig. 3. Numerical simulation results on ABAQUS software and experiments

Fig. 3 shows the final crack of the Koyna dam under the influence of the earthquake in 1967, from a numerical simulation using ABAQUS software with unmodified particle mesh and experimental model with mechanical norms of concrete given in Table 1 [2]. The result of simulation and experiments are relatively uniform in terms of destructive forms.

Table 1. Physico-mechanical properties used in the calculation of the Koyna dam

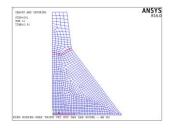
Material	E	Poisson	ρ	ft	fc
	(kN/m <sup>2</sup>	coefficient	(T/m <sup>3</sup>	(kN/m <sup>2</sup>	(kN/m <sup>2</sup> )
Concrete	3.1×10 <sup>7</sup>	0.2	2.643	2.9×10 <sup>3</sup>	24.1×10

When using the "RCCD\_CRACK Calculation Program" in the APDL programming language to calculate stress states, deformation and crack development of Koyna gravity concrete dams with the above and below dimensions, and the effect of the accelerated earthquake has the final cracking

effect as shown in Fig. 4. The results of fracture development calculations are



consistent with Mridha S's experimental study [2]. This is the basis for ensuring the reliability of "RCCD\_CRACK Calculation Program".



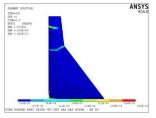


Fig. 4. Damaged area of Koyna Dam by RCCD\_CRACK Calculation

Program

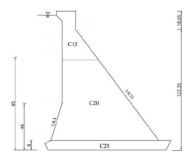


Fig. 5. Cross section of the Guandi Dam

Another example of destructive research on Guandi concrete gravity dam construction in China under the effect of the Koyna earthquake [3],[10]. The cross-sectional area of the Guandi dam is given in Fig.5 . The physicomechanical properties of the concrete are shown in Table 2.

Table 2. The physicomechanical properties used in Guandi dam calculation

Material	E (kN/m <sup>2</sup> )	Poisson coefficien t	ρ (T/m <sup>3</sup>	f <sub>t</sub> (kN/m <sup>2</sup> )	$f_{c} (kN/m^{2})$
C15	5.6×10 <sup>7</sup>	0.167	2.552	1.453×10	14.53×10
C20	5.76×10	0.167	2.552	1.94×10 <sup>3</sup>	19.38×10
C25	5.88×10	0.167	2.552	2.15×10 <sup>3</sup>	21.45×10

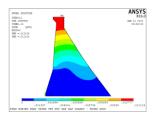
In the results of Gaohui Wang's study, Wang et al [3] found that when the dam was affected by the earthquake, the first crack appeared at the lower section of the dam and developing the upstream. The next crack destroys from the upstream at the break into several sections site and develops the lower section of the dam, damaging the dam structure, see Fig. 6.





Fig. 6. The destruction of the Guandi Dam under the effect of Koyna earthquake [3]

The calculation of the Guandi dam use "RCCD\_CRACK calculation" method, gave the results of displacement and stress before the dam was completely destroyed Fig.7 and Fig.8. The last damaging area in the dam was shown in Fig.9. This result is in line with the results of Gaohui Wang's research. Once again, we can confirm the reliability of the "RCCD\_CRACK calculation program" set up by the author.



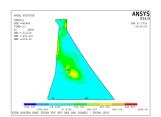
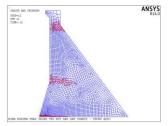


Fig. 7. Distribution of general displacements

Fig. 8. Distribution of the main stress S1



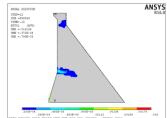


Fig. 9. Destructive area caused the crack of Guandi dam by the RCC\_CRACK Program

# IV. DESTRUCTION LEADING TO THE CRACK OF SON LA ROLLER-COMPACTED CONCRETE DAM

The Son La roller-compacted concrete dam is the tallest roller-compacted concrete gravity dam in Vietnam up to now. The dam is the 138.1m height, 105m width, the peak 's width of 10m. The physicomechanical properties of the materials are given in Table 3.

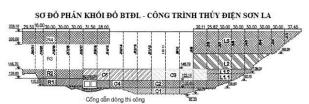
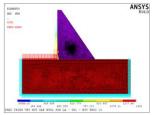


Fig.10 Diagram of dam construction block



# Calculating development of cracks in roller-compacted concrete gravity dams based on self-adaptive finite element method in Ansys software



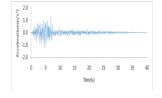


Fig. 11. Adaptive mesh of the Son La dam

Fig. 12. Earthquake accelerator tape designed for SonLa dam

Table 3. The physicomechanical properties of the physicomechanical properties' materials

Material	Е	N	ρ	f <sub>t</sub>	f <sub>c</sub>	α	В
	$(kN/m^2)$		(T/m <sup>3</sup> )	$(kN/m^2)$	$(kN/m^2)$		
RCC	2.5×10 <sup>7</sup>	0.167	2,4	1.2×10 <sup>3</sup>	16.0×10 <sup>3</sup>	0.3	0.5

Using the "RCCD\_CRACK calculation program" in order to calculate the crack development of Son La roller-compacted concrete dam under the effect of a special loading capacitying capacity combination of the earthquake. displacement at the top of the dam is shown in the Fig. 10 and Fig.11. The fracture behavior is shown in Fig. 12. The first crack appeared at the upstream of dam footing, then the upstream surface two thirds above the dam bottom and eventually developing lower section near the top of the dam. The dam is destroyed when the cracks cross from upstream to downstream (Fig. 13).

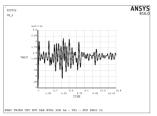


Fig. 10. horizontal displacement of the crest

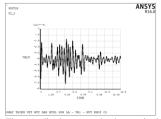


Fig. 11. displacement in the vertical direction of the crest

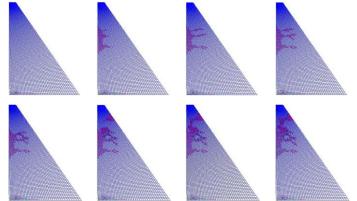


Fig. 12. The destructive process of Son La roller-compacted concrete dam under the effect of earthquake loading capacitying capacity.

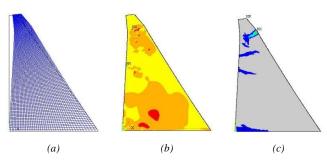


Fig. 13. The result at the time, the roller-compacted concrete dam is completely destroyed

(a) Deformation of the element mesh; (b) The distribution of the main stress  $S1; (c)\ Destructive\ area$ 

# V. CONCLUSION

The author has set up a specialized program for calculating the deformation, stress, and cracking of the roller-compacted concrete dam, called RCCD\_CRACK through using the parametric programming language (APDL). The input data is imported through the user's interface and the output is shown thanks to the ANSYS software functions, so it is very easy and convenient for the user without any difficulty.

On the basis of the roller-compacted concrete dam calculations using the RCCD\_CRACK calculation program with APDL programming language in ANSYS software, it is enough reliability to calculate the crack development of the Son La roller-compacted concrete dam under the effect of earthquake loading capacity. The results show clearly the destructive process of the dam.

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Quang Hung Nguyen was born in 1975 in Hanoi, Viet Nam. He received the Engineering's degree and M.S. degrees in hydraulic construction from the Thuyloi University of Vietnam, in 1997 and 2000 and the PhD. degree in hydraulic structure from Wuhan University, China. Since 1998, he is a lecture in Faculty of Civil

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**Hoang Hung Vu** was born in 1978 in Hanoi, graduated from Thuy Loi University, received a Doctorate in Marine Structure Engineering from Hohai University - China, Associate Professor of Thuy Loi University. He teaches hydraulic structures, chairs and participates in

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