

# Power efficient 5G Wireless Networks based on Self-Organized Utility Function

Madan Mohan Rao. Nelluri, Habibullah Khan

**Abstract:** *The problem of power control in uplink transmission for 5G wireless networks is studied in detail in this research paper, and an optimal technique in which power control in uplink direction is proposed using a Utility function in turn it can be treated as a self-organized technique. It is necessary that wireless networks of next generation must handle both multimedia and data services which may be real time or non-real time in an efficient way to achieve optimal data rates to all users. By using optimal power control scheme and also rate control schemes system resources can be utilized efficiently. With the help of Utility function based on economic theory the efficient power control algorithm is being developed. The solution of Utility function for control of uplink power is derived by Lagrangian equation method. It can also be proved that the self-organizing utility function can be best used to achieve the optimal uplink power control scheme and the unique results are obtained which in turn depend on the different user environment. Numerical results of the algorithm presented here also show that optimal power control scheme is achieved using self-organized utility function.*

**Index terms:** power control, 5G networks, utility function, self-organized network (SON), Lagrangian equation

## I. INTRODUCTION

The research on the concept of Self organizing network (SON) is essential to minimize the operating expenditure (OPEX) and also to improve the system performance of the next generation wireless networks viz. LTE-A/5G networks [1]. The concept of self-organizing network (SON) includes self-optimization, self-configuration and self-healing. The important research task of SON is power control and which is beneficial for wireless communication systems in different ways [2].

Because the battery energy for mobile users is limited, the power control has gained challenging research interest in wireless networks especially for LTE-A and 5G networks which again is a difficult issue and effects output performance of the wireless network system [3].

The optimization issue of power control is an ambitious concept which requires resource optimization for the improvement of performance in wireless communication networks [8].

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Our research work concentrates on 5G networks and proposes a utility function based optimal uplink power control strategy for getting maximum utilities in transmission. The required parameters pertaining to self-improvement of energy reduction are collected where the transmitting power is obtained using UE measurements without changing the capacity of the network [5]. To meet service requirements of users' applications utility theory has been used extensively to solve optimized resource allocation problem in wireless networks. Resource optimization problem in networks can be solved by using the utility concept in many of the related works. It is a co-operative power control technique which means all the user equipment are divided based on coverage levels of base stations and also accessing probability. Each user in the network being allocated optimized power levels for obtaining flexible data rates and to maintain maximum utility function. Considering the inter cell interference parameter the proposed algorithm got the advantage of calculating the most accurate overall system capacity of the 5G mobile networks.

Generally power control schemes can be classified into two types. They are centralized and distributed. As the name indicates in centralized power control, mobile switching center will continuously monitor and calculate the optimum power levels for all mobile stations in the network. On the other hand in distributed power control, powers are computed by determining the transmitter power of base station within mobile stations.

The key aspect of this work is in considering power control scheme based on utility function and finding out energy cost because of congestion. The proposed research model meets the target of maximizing the utility level of total transmission with tradeoff between network throughput and power consumption. In this paper a novel optimal target and a new parameter based power control technique is proposed on contrary with the existing power control schemes.

The entire paper is divided as follows: Section II gives the related works in optimum power control techniques of LTE-A/5G networks. Section III explains optimum power control approach based on utility function. Section IV shows the solutions to proposed model in Section III and also different outputs of the model. Section IV describes heuristic power

control algorithm in series of steps in tabular format. Section V gives the numerical results for the proposed model. Conclusion of the entire paper is given the last section.

II. SYSTEM MODEL

In this section, the uplink power control scheme based on utility function will be discussed in detail.

The complete mathematical expressions are derived and also explained how this work will be applied to the 5G network model as shown in fig.(1) below and it is assumed with N users distributed over each of the M base stations (eNB) in the network.

The transmit data power level of x<sup>th</sup> user which is connected with y<sup>th</sup> base station is denoted by P<sub>xy</sub>.

There are some users which are served by one or more base stations.

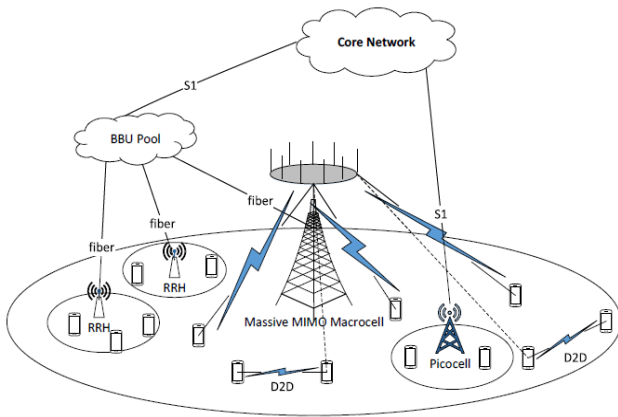


Figure 1 5G network Architecture

Let us assume that the Gaussian noise variance for the uplink to be σ<sup>2</sup>. The channels experienced by a path loss exponent δ at a distance of l<sub>xy</sub> meters of x<sup>th</sup> user and h<sub>xy</sub> is flat Rayleigh fading function then the expression for SINR at user n γ<sub>xy</sub> can be expressed as

$$\gamma_{xy} = \frac{P_{xy}}{\sigma^2} l_{xy}^{-\delta} |h_{xy}|^2 \quad \text{--- (1)}$$

Fig 1.shows Relay 5G network architecture with 3 relay stations is considered and users UEs which are directly connected to base stations are considered as mUEs and users UEs which are connected via relay are named as rUEs. The relays sometimes cause interference to neighboring base stations.

The expected rate of transmission between x<sup>th</sup> mobile user equipment and y<sup>th</sup> base station is r<sub>xy</sub> then we can express the Utility function as

$$U_{xy}(P_{xy}) = r_{xy} - \beta_{xy} P_{xy} - \phi_{xy} P_{xy} \quad \text{--- (2)}$$

Where β<sub>xy</sub> is Utility function positive parameter and φ<sub>xy</sub> is a cost parameter of congestion which is positive and also termed as costing parameters.

In the above formula each user's energy cost is dependent on the transmitted power that is denoted by φ<sub>xy</sub> P<sub>xy</sub>.

The expected rate of transmission between x<sup>th</sup> user and y<sup>th</sup> mobile station r<sub>xy</sub> can be written as

$$r_{xy} = \log_2(1 + \gamma_{xy}) \quad \text{--- (3)}$$

Where γ<sub>xy</sub> is the SINR of x<sup>th</sup> user denoted by equation 1. After substituting equation 3 in equation 2 the utility function can be written as

$$U_{xy}(P_{xy}) = \log_2(1 + \gamma_{xy}) - \beta_{xy} P_{xy} - \phi_{xy} P_{xy} \\ = \log_2\left(1 + \frac{P_{nm}}{\sigma^2} l_{xy}^{-\delta} |h_{xy}|^2\right) - (\beta_{xy} + \phi_{xy}) P_{xy}$$

$$U_{xy}(P_{xy}) = \log_2(1 + \alpha_{xy} P_{xy}) - (\beta_{xy} + \phi_{xy}) P_{xy} \quad \text{--- (4)}$$

$$\text{where, } \alpha_{xy} = \frac{l_{xy}^{-\delta} |h_{xy}|^2}{\sigma^2} \quad \text{--- (5)}$$

The throughput of each user i.e. the addition of all mobile user data rates can be noted as capacity and also it is an important resource restriction of BW of each base station in the wireless network, that can be expressed as

$$\sum_{x \in N} r_{xy} \leq C_y \quad \text{--- (6)}$$

Where C<sub>x</sub> is the overall capacity of x<sup>th</sup> base station.

The efficient model of utility function 5G relay system can be written as

$$\max(U) = \max\left(\sum_{x=1}^M \sum_{y=1}^N U_{xy}(P_{xy})\right)$$

$$\max(U) = \max\left(\sum_{x=1}^M \sum_{y=1}^N (\log_2(1 + \alpha_{xy} P_{xy}) - (\beta_{xy} + \phi_{xy}) P_{xy}) - \sum_{x=1}^M A_x [\log_2(1 + \alpha_{xy} P_{xy})]\right) \text{ for all } x, y \quad \text{--- (7)}$$

The optimized power level can be achieved with maximization of the above optimization problem. The very important resource constraint of BW of every base station is given by equation 6. The total utility level of the entire wireless network is expressed by equation (7).

The utility function can be expressed in terms of mobile users, base stations and also transmission powers of users  $P_{xy}$  as

$$U = U(\{N\}, \{M\}, \{P_{xy}\})$$

where  $N = \{1, 2, \dots, (x) \dots N\}$  represent the mobile users,  $M = \{1, 2, \dots, (y) \dots M\}$  denote the base stations and  $P_{xy} = \{P_{11}, P_{12}, \dots, P_{xy}, \dots, P_{NM}\}$  give the allocated power profile of  $x^{\text{th}}$  mobile user in  $y^{\text{th}}$  base station.

The utility functions are the target of the optimized problem in equation (7).

After careful observation of the expressions of utility function  $U$ , it can be understood that they are not linear, and also is not similar with the exact normal form function.

### III. OBSERVATIONS

The dynamic optimized solution for the proposed model given by equations (6) and (7) will be explained in this section.

**Observation 1:** An optimal solution to the proposed model described by (6) and (7) can be assumed to be a set of control vectors  $\{P_x^*\}$ , suppose for all  $x \in N$ , there exists

$$U(\{P_x^*\}) \geq U(\{P_x\}) \quad \text{--- (8)}$$

The Solution for proposed model denoted by equations (6) and (7)  $\{P_x^*\}$  denotes a set of self organized solution to maximize the utility function. Each user  $x$  will have its own self organized and unique solution. And no individual mobile user can have the best utility value because if individual mobile user changes in its power and bandwidth. All mobile users have the cooperation to get optimum value of utility function to satisfy  $U(\{P_x^*\}) \geq U(\{P_x\})$

$$\Lambda (0 \leq \Lambda \leq 1)$$

$$\begin{aligned} u(\Lambda P1 + (1 - \Lambda)P2) &= \log_2[1 \\ &+ \alpha_{xy}(\Lambda P1 + (1 - \Lambda)P2)] - (\beta_{xy} \\ &+ \varphi_{xy})(\Lambda P1 + (1 - \Lambda)P2) \quad \text{--- (9)} \end{aligned}$$

Substituting for  $P_1$  and  $P_2$  in the above equation for utility function, we will have

$$u\Lambda P1 = \Lambda \log_2(1 + \alpha_{xy}P1) - \Lambda(\beta_{xy} + \varphi_{xy})P1 \quad \text{--- (10)}$$

$$\begin{aligned} (1 - \Lambda)u(P2) &= (1 - \Lambda)\log_2(1 \\ &+ \alpha_{xy}P2 - (1 - \Lambda)(\beta_{xy} + \varphi_{xy})P2) \quad \text{--- (11)} \end{aligned}$$

Adding equations (10) and (11)

$$\begin{aligned} &u\Lambda P1 + (1 - \Lambda)u(P2) \\ &= \Lambda \log_2(1 + \alpha_{xy}P1) \\ &- \Lambda(\beta_{xy} \\ &+ \varphi_{xy})P1 \quad \quad \quad + (1 \\ &- \Lambda)\log_2(1 + \alpha_{xy}P2 - (1 - \Lambda)(\beta_{xy} + \varphi_{xy})P2) \quad \text{--- (12)} \end{aligned}$$

solving equations (9) and (12), we have

$$\begin{aligned} &u(\Lambda P1 + (1 - \Lambda)P2) - [u\Lambda P1 + (1 - \Lambda)u(P2)] \\ &= \log_2[1 + \alpha_{xy}(\Lambda P1 + (1 - \Lambda)P2)] \\ &- (\beta_{xy} + \varphi_{xy})(\Lambda P1 + (1 - \Lambda)P2) \\ &- \Lambda \log_2(1 + \alpha_{xy}P1) \\ &- \Lambda(\beta_{xy} + \varphi_{xy})P1 - (1 - \Lambda)\log_2(1 \\ &+ \alpha_{xy}P2) \quad \quad \quad + (1 - \Lambda)(\beta_{xy} \\ &+ \varphi_{xy})P2 \\ &= \log_2[1 + \alpha_{xy}(\Lambda P1 + (1 - \Lambda)P2)] \\ &- \Lambda \log_2(1 + \alpha_{xy}P1) \\ &- (1 - \Lambda)\log_2(1 + \alpha_{xy}P2) \quad \text{--- (13)} \end{aligned}$$

It can be understood that when the base of logarithmic function is more than 1, logarithmic function is an increasing function, hence we can write

$$\begin{aligned} &u(\Lambda P1 + (1 - \Lambda)P2) - [u\Lambda P1 + (1 - \Lambda)u(P2)] \\ &\geq 0 \quad \text{--- (14)} \end{aligned}$$

From the above equation we can conclude that the utility function leads to a concave function.

**Observation 2:** There exists an optimum solution for A set of control vectors to the power control issue given by equations (6) and (7).

The power control problem of equations (6) and (7) can be explained by using the Lagrange equation technique. The Lagrangian multiplier equation for the optimization issue stated in equation (6) can be expressed as

$$\begin{aligned} F &= \sum_{y=1}^M \sum_{x=1}^N (\log_2(1 + \alpha_{xy}P_{xy}) - (\beta_{xy} + \varphi_{xy})P_{xy}) \\ &- \sum_{y=1}^M \Lambda_y [\log_2(1 + \alpha_{xy}P_{xy}) - C_y] \quad \text{--- (15)} \end{aligned}$$

Differentiate  $F$  with respect to  $P_{xy}$

$$\begin{aligned} dF &= \sum_{x=1}^M \sum_{y=1}^N \left( (1 - \Lambda_x) \frac{1}{\ln 2} \frac{\alpha_{xy}}{1 + \alpha_{xy}P_{xy}} - (\beta_{xy} \right. \\ &\left. + \varphi_{xy}) \right) dP_{xy} \quad \text{--- (16)} \end{aligned}$$

Assume that the partial derivative to be zero then we can write

$$(1 - A_x) \frac{1}{\ln 2} \frac{\alpha_{xy}}{1 + \alpha_{xy} P_{xy}} - (\beta_{xy} + \varphi_{xy}) = 0 \quad \text{--- (17)}$$

If we solve the above equation for getting the optimal power

$$P_{xy} = \frac{(1 - A_y)}{(\beta_{xy} + \varphi_{xy}) \ln 2} - \frac{1}{\alpha_{xy}} \quad \text{--- (18)}$$

After substituting equation (6) in (18) we get the following equation

$$(1 - A_y) \sum_{x \in N} \frac{\alpha_{xy}}{(\beta_{xy} + \varphi_{xy}) \ln 2} = C_y \quad \text{--- (19)}$$

Then we have the value of  $A_y$

$$A_y = 1 - \frac{C_y}{\sum_{x \in N} \frac{\alpha_{xy}}{(\beta_{xy} + \varphi_{xy}) \ln 2}} \quad \text{--- (20)}$$

Substituting equation (20) into (18) we get the optimal power level allocated to each user can be written as

$$P^*_{xy} = \frac{C_y}{(\beta_{xy} + \varphi_{xy}) \ln 2 \sum_{x \in N} \frac{\alpha_{xy}}{(\beta_{xy} + \varphi_{xy}) \ln 2}} - \frac{1}{\alpha_{xy}} \quad \text{--- (21)}$$

Hence there is an efficient solution for power control issue for all users. The solution is achieved with the derivation of the utility function and it can be found easily that solution for each user is unique. In this scenario of optimum condition every user in the system will have mutual coordination and highest utility can be achieved.

#### IV. POWER CONTROL ALGORITHM

The complete detailed steps of proposed heuristic algorithm are shown in table 1 below. And we have already explained as in previous part, the Lagrange multiplier technique gives us many individual solutions for all base stations and all are optimized solutions which satisfy the equations (6) and (7).

**Table I Optimal Power control algorithm**

<b>1. Assign the initial values and find maximum utility</b>
$\max(U)$ $= \max \left( \sum_{x=1}^M \sum_{y=1}^N U_{xy}(P_{xy}) \right) \text{ find max utility}$ <p style="text-align: right;"><i>for all x, y in network</i></p>
<b>2. Power control mechanism</b>
<p>a. For all the values of y Reset Lagrange multiplier</p> <p>b. Find out resource constraint problem</p> <p>c. Calculate the Lagrangian equation</p> <p>d. Compute the optimal power level to get maximum utility</p> $P^*_{xy} = \frac{C_y}{(\beta_{xy} + \varphi_{xy}) \ln 2 \sum_{x \in N} \frac{\alpha_{xy}}{(\beta_{xy} + \varphi_{xy}) \ln 2}} - \frac{1}{\alpha_{xy}}$ <p style="text-align: right;"><i>for all x, y</i></p>

e. Assign the values to users

**3. Stop**

#### V. SIMULATION RESULTS

This section explains the simulation on a network with three base stations as the servicing stations. The number of active users N in the network is taken as 60 and it is assumed that mobile users are distributed uniformly in the entire network. It is also assumed that all the cells experience same communication environment, equal capacity, traffic loads and also with same propagation loss  $L_{xy} = |h_{xy}|^{-\delta}$ . The capacity of every cell is assumed to same which is given by  $C_y$ . Table II and Table III shows simulation parameters. The maximum utility level of different mobile users with optimized power in all base stations is simulated and shown in Figure.2. The optimized power level of different users is illustrated in figure.3 The variation of Signal to Interference plus Noise Ratio (SINR) is shown in figure.4. it is clearly seen that SINR increases with power and figure.5 illustrates total utility of each base station. From the result it is also found that utility of the base station 1 is more than base station 3 as base station 1 is nearer to mobile user when compared to base station 3. It is also obvious that the utility level of base station 1 is the highest among other base stations because congestion cost parameter is small.

The base station 2 has got a higher utility level when compared to base station 3, because of its smaller congestion cost parameter than base station 3. It is understood that the system overall performance is significantly affected by the congestion cost parameter.

**Table II Simulation Parameters**

Parameter	Value
Number of Cells M	3
Number of users N	60
Number of users in each cell	20
Propagation Path Loss	0.8
AWGN power	-83 DBM
Neighbour cell Interference power	-10.3 DBM
Capacity of cell M	$10^5$ BPS
Positive Parameter	$\beta_{xy}$
Probability parameter	$\varphi_{xy}$

**Table III Parameters of  $\beta_{xy}$  and  $\varphi_{xy}$**

$\beta_{xy}$	y=1	y=2	y=3	y=4	y=5
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$x=1$	0.2	0.3	0.4	0.5	0.6
$x=2$	0.25	0.35	0.45	0.55	0.65
$x=3$	0.3	0.4	0.5	0.6	0.7
$\varphi_{xy}$	$y=1$	$y=2$	$y=3$	$y=4$	$y=5$
$x=1$	0.65	0.72	0.75	0.81	0.85
$x=2$	0.7	0.73	0.82	0.85	0.89
$x=3$	0.75	0.79	0.85	0.91	.94

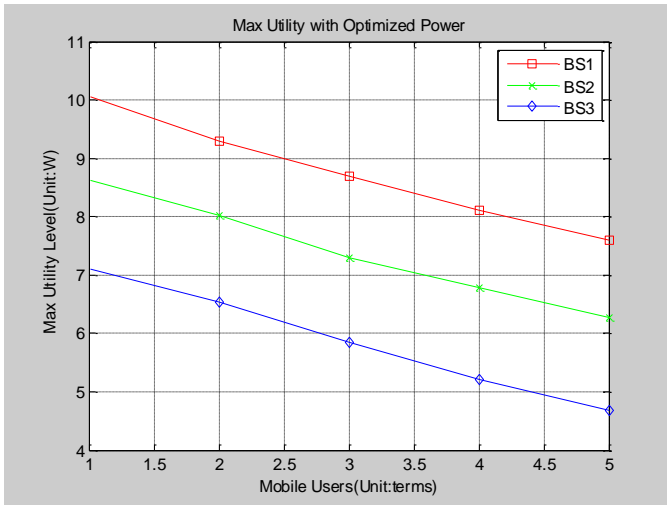


Figure 2 Maximum utility level with optimized power

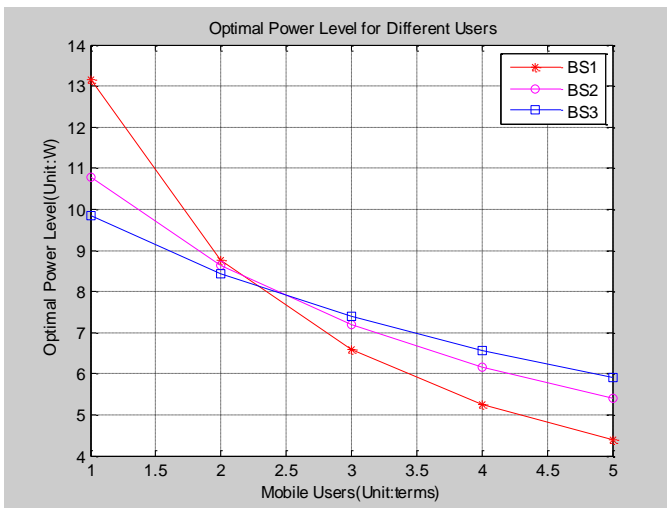


Figure 3 Optimal power levels for different users

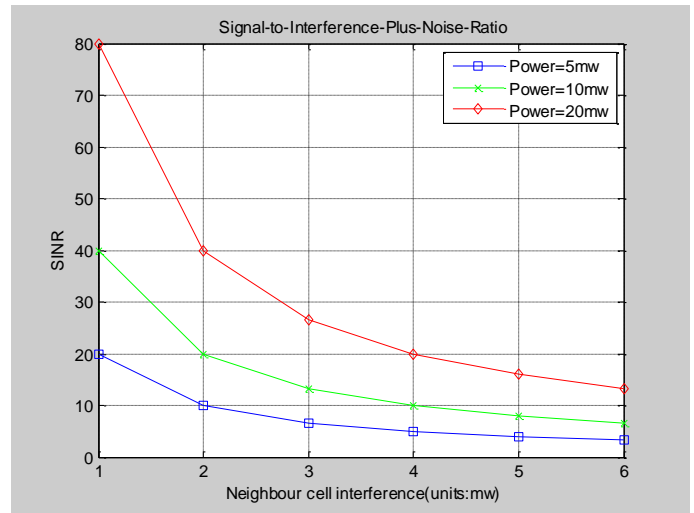


Figure 4 SINR versus interference of neighbor cell

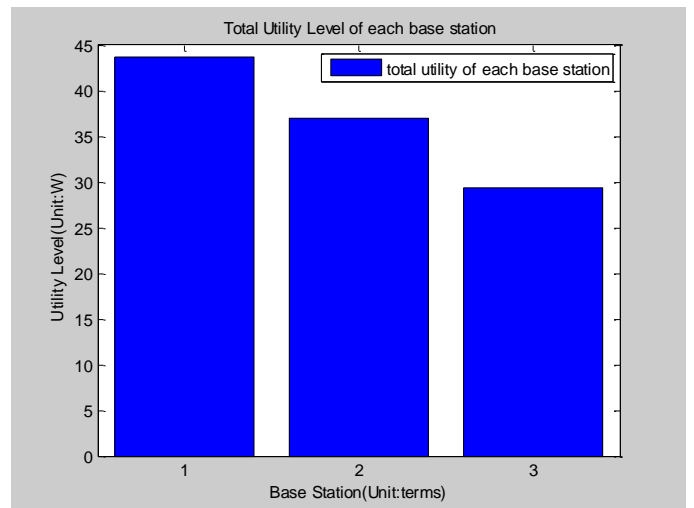


Figure 5 Base station Total Utility levels

## VI. CONCLUSIONS

In this research paper the uplink power control approach based on utility function is proposed in 5G wireless networks. The important contributions of this research work are modeling a utility function based optimal power control technique and utility function itself works as self-organizing scheme in 5G wireless networks. From the mathematical derivation it is proved that utility function is a concave function and the energy cost occurred by the congestion is a self-organized scheme with further reduction in Operational Expenditure. By using Lagrangian multiplier technique the optimum uplink power of every mobile user is calculated and it is also found that this is a unique optimal solution by this scheme. Several numerical simulations proved that our scheme achieved the optimal power and maximum utility.

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