

# Modeling the Design of Plasmonic Biosensor Device by using Abstract Finite State Machine Model and FDTD Based MEEP Tool

Divya Sharma, R.P.Dwivedi

**Abstract:** This paper describes and highlights the usage of Finite State Machine (FSM)  $M'$  model using the Finite Automata sub-systems ( $M'_1, M'_2, M'_3, \dots, M'_n$ ) for a nanoscale biosensor sub-block system design which accepts the languages  $L'_1$  to  $L'_n$  individually or a common language  $L'$ . The biosensor sub-block design and development is a challenging task, as it involves solving complex sub-blocks operations and the Finite Automata design tools provide the different approaches to address the same. Here each sub-system of the biosensor system is individually modeled using Finite Automata and they are simulated by using Massachusetts Institute of Technology Electromagnetic Equation Propagation (MEEP) tool, to model the structure and Plasmonic behavior of the device. The individual sub-system can be mathematically modeled using the MATLAB Simulink as FSM and finally combined to form a target complex biosensor device as well as complete biosensor system. The objective of this paper is to showcase the usage of FSM simulation in the development of biosensor devices as a part of Plasmonic biosensor device design process.

**Index Terms:** Biosensors, Finite State Machine, Massachusetts Institute of Technology Electromagnetic Equation Propagation tool (MEEP), Nanotechnology, Plasmonics.

## I. INTRODUCTION

The nanotechnology finds its application in many key areas like in the design and development of biosensor devices for medical diagnostics [1], [2], fabrication of microprocessor in computing industry, solar panel optimization in renewable energy sector, communication devices [3] etc. It is one of the most expensive area of research under which the cost of translating the design and fabrication from initial requirements to the final end product is very high and time consuming [4], [5]. This high cost can limit the development of new nanotechnology based Plasmonic biosensors devices [6]–[9]. Here the main challenge is to mitigate the complexity of design and development of a biosensor device [10]–[12]. The simplification in the design and development process would significantly help the researchers to accelerate and perform iterative experimental research to re-validate the claims, findings and the research outcomes by using various simulation tools. In this paper,

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Divya Sharma, School of Electrical and Computer Science Engineering, Shoolini University, Solan, 173229, H.P., INDIA.

\*R.P. Dwivedi, School of Electrical and Computer Science Engineering, Shoolini University, Solan, 173229, H.P., INDIA.

the Finite Automata design tools are used in the design and modeling of a nanoscale biosensor device before the actual fabrication takes place. This design approach is significantly different from the existing design process like MEEP [13], [14] or Discrete Dipole Scattering (DDSCAT) simulation tools. Here Finite Automata design tools provide different levels of abstraction and other unique approaches, which would help in modelling of the biosensor device easily.

### A. Biosensor System

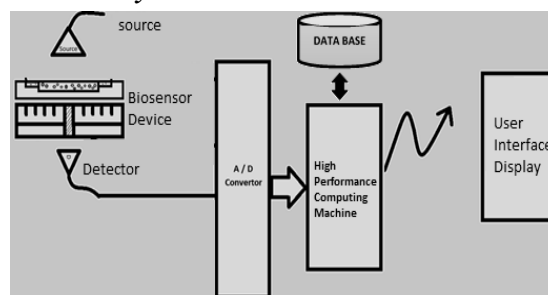
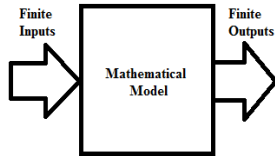


Fig. 1 Biosensor system block diagram.

A biosensor is a device with associated support system which can be used to sense and quantify biological components for example glucometer is used to measure the glucose level [15]. The biosensor device can be designed and developed based on optical, physicochemical, electrochemical and piezoelectric principles. The biosensor device is generally coupled with the complex allied electronic sub-system as shown in the Fig. 1 to enhance, measure and provide the results in user-friendly format. These electronics sub-system includes the light source as the input unit and the detector unit for capturing the changes in the physical parameters of light that attributes to the biosensor device with target specimen. These captured signals are digitized using high precision and high-speed Analog to Digital (A/D) convertor and fed into artificial intelligence based high performance computing machine, which is backed up by the training of database to compute and provide the necessary results. These state-of-art biosensor machines can be easily designed and modelled using Finite State Machine model as a whole unit shown in Fig. 1 or only as the electronics sub-system and the nanoscale biosensor sensor device [16], [17]. Here, the focus is on the nanoscale biosensor's design and modeling.



**B. Finite State Automata System**



**Fig. 2 Finite state automata with finite inputs and finite outputs.**

The Finite State Automata (FSA) Fig. 2 is a Finite State Machine (FSM) which models the computation mathematically. The FSA is an abstract machine which accepts finite set of inputs and provides finite set of outputs with finite set of states. The transition function ‘ $\delta$ ’ is used to make the transition of FSM from one state to another based on the inputs. The Fig. 2 is a mathematical model of any system with finite inputs and finite outputs. The set  $\{ I_1, I_2, \dots, I_q \}$  marks as the finite set of inputs with fixed values and the set  $\{ O_1, O_2, \dots, O_q \}$  as the finite set of outputs with fixed values. This mathematical model can be used to model any kind of system and sub-systems. The finite state machine with output model is formally defined as six tuples machine,

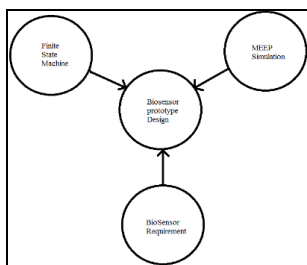
$$M = \{ \Sigma, O, Q, \delta, X, q_0 \} \tag{1}$$

Where,

- $\Sigma$  – Input Alphabet
- $O$  – Output Alphabet
- $Q$  – Finite set of states
- $q_0$ – Initial state
- $\delta$  – Transition Function:  $Q \times \Sigma \rightarrow Q$  the state  $q$  from a finite state set  $Q$  upon an input symbol from the input alphabet  $\Sigma$ , makes a transition into state which is again from the same set  $Q$ .
- $X$  – Transition Function:  $Q \times \Sigma \rightarrow O$  the state  $q$  from a finite state set  $Q$  upon an input symbol from the input alphabet  $\Sigma$ , ejects an output symbol from output alphabet  $O$ .

Here the key aspect is that the input and outputs of the FSM can be easily used to map the biosensor's device input and output as languages. These unique approach opens up to model any kind of system and sub-systems of biosensor devices as described in the Sec. II as Finite State Machines.

**II. GENERIC BIOSENSOR MACHINE OR SYSTEM OR DEVICE BLOCK DESIGN APPROACH**



**Fig. 3 Biosensor prototype design approach using FSM and MEEP simulation model.**

The approach of design and developing generic biosensor

device prototype is shown in the Fig. 3. The MEEP is an open-source command line script programming language based on the FDTD method for simulation of electromagnetic equation propagation [18]. This tool with the aid of allied tools like h5tools, mayavi2 [19] can be used to simulate the structural and behavioral functions of nanoscale biosensor devices. Here the FSM design tools and the MEEP simulation tools are used to translate the biosensor requirements into virtual biosensor device design as described in the Sec 2.1 design process flow.

**A. Algorithm: Design Process Flow**

- Step 1: Start
- Step 2: User specified target biosensor device or system requirement.
- Step 3: Simulation of the biosensor device using MEEP tool.
- Step 4: Simulation of the biosensor device using FSM design tool.
- Step 5: Comprehend the biosensor device behavior using MEEP and FSM simulation model.
- Step 6: If design refining is required: go to step 2 else go to step 7.
- Step 7: Initiate the physical biosensor device fabrication in fab labs.
- Step 8: Stop.

The paper focuses and emphasis on the steps 3, 4 and 5 which forms a crucial stage for the design of biosensor device. A case study of biosensor device block with circular channel waveguide design has been investigated using MEEP and FSM simulations.

**III. EXPERIMENTAL SETUP FOR BIOSENSOR DEVICE WITH CIRCULAR WAVEGUIDE SIMULATION USING MEEP AND FSM**

The MEEP simulation hardware setup includes the machine details: AMD A10-7850K APU processor with 4 CPU cores and 8 GPU cores operating at frequency 4.1GHz, RAM configuration details: 16 Giga bytes with speed 1600MHz. The secondary storage hard disk drives: 500 Gigabytes and one Terabytes and finally the BIOS Settings: Version-A88X-BIOS (2502). Software Setup includes: Ubuntu 14.04.4 LTS AMD64 Operating System with the Linux kernel (3.19.0-49-generic x86\_64). The MEEP simulation tool and allied visualization tools include, MEEP 1.1.1, libctl 3.1, Guile 1.8.8, MPI version 2.1.1, mpirun (Open MPI) 1.6.5, HDF5 utils, h4fromh5, h5fromh4, h5fromtxt, h5math, h5topng, h5totxt, h5tovtk and MayaVi 4.1.0. General system configuration requires system stack size marked as unlimited and swap size ~701 Giga Bytes. For the FSM simulation, the hardware setup is same as MEEP simulation hardware configuration but software setup includes the following details: Windows 10 (64 bit) operating system. The development and simulation tools: Visual studio 2015, MATLAB 9.2 (R2017a) and Simulink.



### A. Biosensor Device Model Specification Details

The sample sensor example with two material types are silver as metal (M) layer and air as insulator (I) layer for the simulation of Metal-Insulator-Metal (MIM) structure. The insulator layer is sandwiched between the metal layers and a central hole runs through all the layers. The two concentric waveguides patterned are formed on the top of silver layer block as shown in Fig. 6.1. The following are the biosensor specification in three-dimension quadrant (x, y, and z) with a central groove,

- Lattice size (x, y, z) = (10,10,10)
- block size (x, y, z) = (5, 0.25, 5)
- MIM structure = Silver – Air – Silver
- Central hole : Radius = 0.15, Height = infinity
- Concentric waveguide pattern:
  - Waveguide 1: Radius = 1.65, Height = 0.25
  - Waveguide 2: Radius = 1.15, Height = 0.25
  - Waveguide 3: Radius = 0.85, Height = 0.25
- Perfectly matched layer = 1.0
- Number of frequencies at which to compute flux : 100
- The following are the run source specification,
  - Source = gaussian-source
  - Pulse center frequency = 0.15
  - Pulse width = 0.1

### B. Circular Waveguide-Based Biosensor Sub-System Machine with and Without Central Grooves

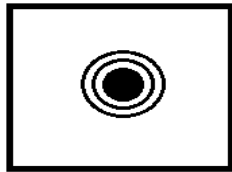


Fig. 4.1 Biosensor block with the central groove and concentric waveguide

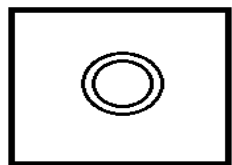


Fig. 4.2 Biosensor block without the central groove and with concentric waveguide

The biosensor device or machine M' is proposed with the central cylinder and two concentric waveguides Fig. 4.1 and structured with layer of Metal-Insulator-Metal (MIM) heterogenous structure. The second biosensor device or machine M'' Fig. 4.2 is proposed without the central cylinder but with the same dimensions of two concentric waveguides as in Fig. 4.1 and structured with layer of the Metal-Insulator-Metal (MIM) heterogenous structure to be simulated using FSM model.

### C. Mathematical Model of FDTD Method

In FDTD method, the transmitted power through custom structure design for the given frequency  $\omega$ , is the integral of the Poynting vector (in the normal  $\hat{n}$  direction) over a plane is given by the equation:

$$P(w) = R_e \hat{n} \int E_w(x)^* H_w(x) d^2 x \quad (2)$$

Similarly, for the reflected power through custom structure design for the given frequency, the reflected power is obtained by subtracting the Fourier-transformed incident fields  $E(0)\omega(x)$  and  $H(0)\omega(x)$  in the below equation:

$$P_r(w) = R_e \hat{n} \int [E_w(x) - E_w^{(0)}(x)][H_w(x) - H_w^{(0)}(x)] d^2 x \quad (3)$$

## IV. DETAILED MEEP SIMULATIONS OF BIOSENSOR SYSTEMS MACHINE WITH CIRCULAR WAVEGUIDE WITH AND WITHOUT CENTRAL GROOVE

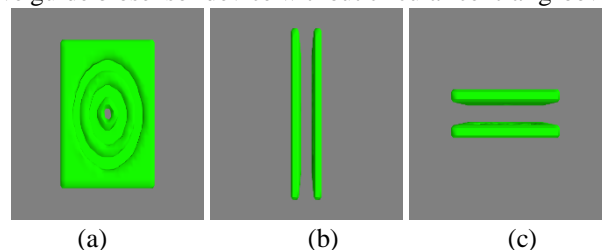
The MEEP provides a set of geometric-object constructs that can be used for building the sensor block structure. The basic geometric structure includes cylinder, block, sphere, cone, ellipsoid, etc. It provides basic constructs to specify the type of material like gold, silver, etc. and finally it also supports various types of source settings to simulate the electromagnetic wave propagation. Here the devices Fig 4.1 and Fig 4.2 are the simulations using MEEP.

### A. Simulation Results for The Circular Waveguide Biosensor with and Without Central Grooves

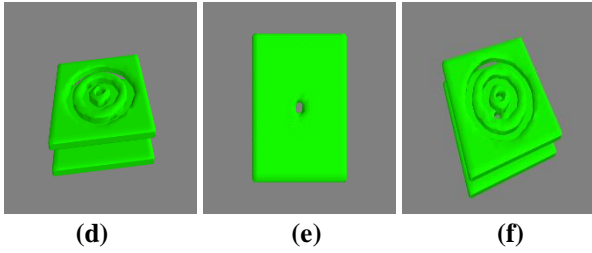
The MEEP provides the simulation output in the form of Hierarchical Data Format 5 (HDF5) [19] files which can be used by the visualization tools like h5utils to extract data and visualize the structures. Here the h5topng and h5tovtk sub tools of h5utils are used to extract and store the information in the form of 'png' image and 3D 'vtk' file format respectively. The 3D visualizing tool MayaVi2 can be used to visualize the sensor block structure in 3D. The sample example of output of MayaVi2 is as shown Fig. 5 and Fig. 6.

### B. Simulation Results for the Circular Waveguide Biosensor with and without Central Groove

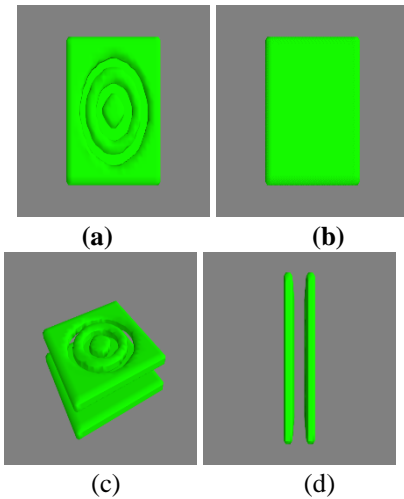
The structural simulation of the circular wave guide biosensor device with circular central groove using MEEP is shown in the Fig. 5 (a) (b) (c) and (d). Similarly, the Fig. 6 (a) (b) (c) and (d) shows the structural simulation of the circular wave guide biosensor device without circular central groove.



# Modeling the Design of Plasmonic Biosensor Device by using Abstract Finite State Machine Model and FDTD Based MEEP Tool



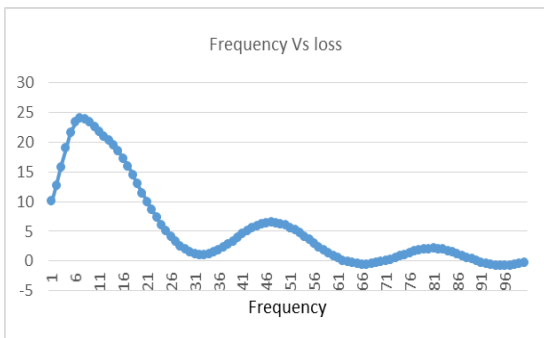
**Fig. 5** Circular waveguide biosensor with central grooves: (a) top view (b) vertical side view (c) horizontal side view (d) angled view1 (e) bottom view and (f) angled view2



**Fig. 6** Circular waveguide biosensor without central grooves: (a) top view (b) bottom view (c) angled view and (d) vertical side view

### C. Simulation Graphs Results for the Circular Waveguide Biosensor with and without Central Groove

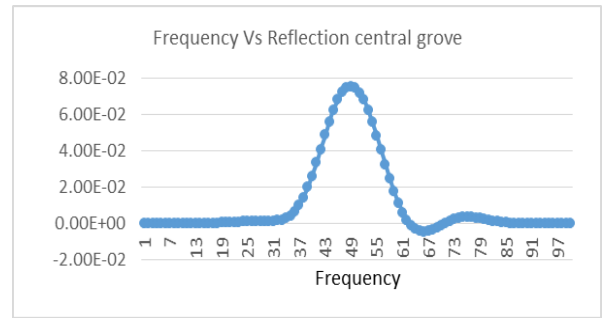
The behavior simulation is performed twice, once with the central groove and the other is without the central groove, the flux spectra is computed by using the runtime specification with source as gaussian-source, Pulse center frequency at 0.15 and Pulse width set to 0.1 as input for transmission, reflection flux and the loss output data points. The output data points are marked in the Appendix I and II with the associated chart plots are marked as in the Fig. 7, Fig. 8, Fig. 9, Fig. 10 and Fig. 11. The Fig.7 shows the circular waveguide frequency Vs loss, the device shows the damping of loss as the frequency increases.



**Fig. 7** MEEP results - Circular waveguide-Frequency Vs Loss

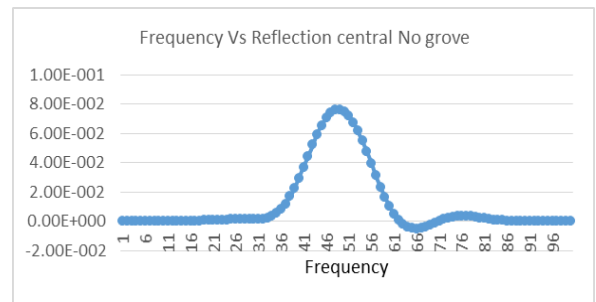
The Fig.8 shows the circular waveguide with cylinder with frequency Vs reflection, the device shows the Gaussian

behavior.



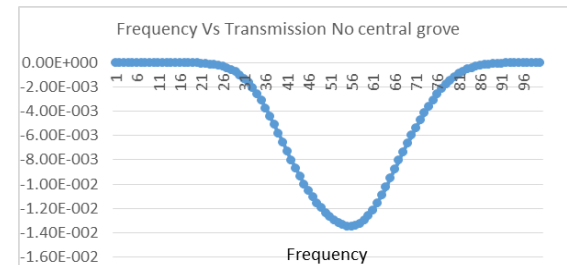
**Fig. 8** MEEP results - Circular waveguide frequency Vs Reflection with Cylinder

The Fig.9 shows the circular waveguide without central groove cylinder with frequency Vs reflection, the device shows the Gaussian behavior.



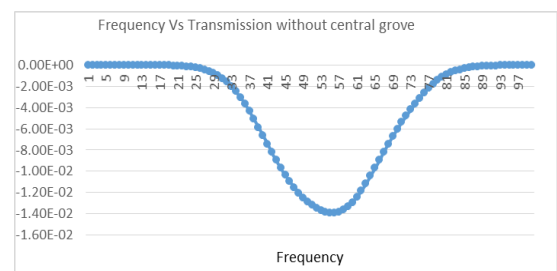
**Fig. 9** MEEP results - Circular waveguide Frequency Vs Reflection without Cylinder

The Fig.10 shows the circular waveguide with central groove cylinder with frequency Vs transmission, the device shows the negative Gaussian behavior.



**Fig. 10** MEEP results - Circular waveguide Frequency Vs Transmission with Cylinder

The Fig.11 shows the circular waveguide without cylinder with frequency Vs transmission, the device shows the inverse Gaussian behavior.



**Fig. 11** MEEP results - Circular Waveguide - Frequency Vs Transmission without Cylinder



### V. FINITE STATE MACHINE MODEL OF BIOSENSOR DEVICE M'

The generic biosensor system and sub-systems can be modelled as FSA machine M'. The biosensor system as a finite state machine M' would accept the input formal language L<sub>i</sub>' and produce the output language L<sub>o</sub>' respectively. The input language L<sub>i</sub>' is generally defined based on the quantities in Eq. 2 and the output language L<sub>o</sub>' is generally defined based on the quantities in Eq. 3,

$$\text{Input Language } L_i' = \{ \text{frequency}_i, \text{wavelength}_i, \text{intensity}_i, \text{phase}_i, \text{angle}_i, \text{SourceType} \} \quad (2)$$

Where,

- Frequency<sub>i</sub> : It is the operating input frequency range.
- Amplitude<sub>i</sub> : It is the operating input amplitude range.
- Wavelength<sub>i</sub> : It is the operating input wavelength range.
- Phase<sub>i</sub> : It is the input phase value.
- Angle<sub>i</sub> : It is the input angle value.
- SourceType : It is the input continuous or Gaussian source type.

$$\text{Output Language } L_o' = \{ \text{frequency}_o, \text{wavelength}_o, \text{intensity}_o, \text{phase}_o, \text{angle}_o, \text{SourceType} \} \quad (3)$$

Where,

- Frequency<sub>o</sub>: It is the operating output frequency range.
- Amplitude<sub>o</sub>: It is the operating output amplitude range.
- Wavelength<sub>o</sub>: It is the operating output wavelength range.
- Phase<sub>o</sub>: It is the output phase value.
- Angle<sub>o</sub>: It is the output angle value.

The biosensor sub-systems are modelled as an individual Finite State Machine M<sub>1</sub>', M<sub>2</sub>', M<sub>3</sub>', M<sub>4</sub>', M<sub>5</sub>',...M<sub>n</sub>' which accepts the input language L<sub>i1</sub>', L<sub>i2</sub>', L<sub>i3</sub>', L<sub>i4</sub>', L<sub>i5</sub>',... L<sub>in</sub>' and releases the output languages as L<sub>o1</sub>', L<sub>o2</sub>', L<sub>o3</sub>', L<sub>o4</sub>', L<sub>o5</sub>',...L<sub>on</sub>' respectively. This biosensor machine sub-system blocks would also require an interfacing sub-block if there are two or more sub-blocks, which has a disjoint language L<sub>ix</sub>' acceptance. These languages would be treated as the interfacing languages or mapper languages which are accepted by the interfacing sub-blocks.

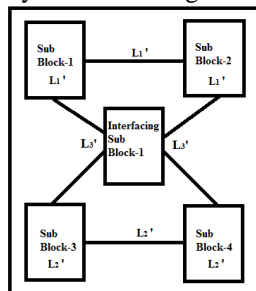


Fig. 12 Generic model M of Biosensor with M<sub>1</sub>', M<sub>2</sub>', M<sub>3</sub>', and M<sub>4</sub>' sub-blocks with the M<sub>5</sub>' interfacing sub-block

The Fig. 12 machine M has the sub-blocks 1, 2, 3, 4 and an

interfacing sub-block 1. The sub-blocks 1 and 2 accept the input language L<sub>1</sub>' Eq. 4, the interfacing block accept L<sub>3</sub>' Eq. 5, and the sub-blocks 3 and 4 accept the input language L<sub>2</sub>' Eq. 4. The interfacing sub-block accepts the interfacing language L<sub>3</sub>' Eq. 5, which acts as the interfacing or mapping language between sub-blocks 1, 2 and 3, 4.

$$\text{Input/output Language } L_1' \text{ and } L_2' = \{ \text{frequency}_{i_o}, \text{wavelength}_{i_o}, \text{intensity}_{i_o}, \text{phase}_{i_o}, \text{angle}_{i_o}, \text{Gaussian mode}_i \text{ or continuous model}_i \} \quad (4)$$

$$\text{Interfacing Language } L_3' = \{ \text{frequency}_{\text{interface}}, \text{wavelength}_{\text{interface}}, \text{intensity}_{\text{interface}}, \text{phase}_{\text{interface}}, \text{angle}_{\text{interface}}, \text{Gaussian model}_{\text{interface}} \text{ or continuous model}_{\text{interface}} \} \quad (5)$$

#### A. Biosensor Device M' Design using Finite State Machine

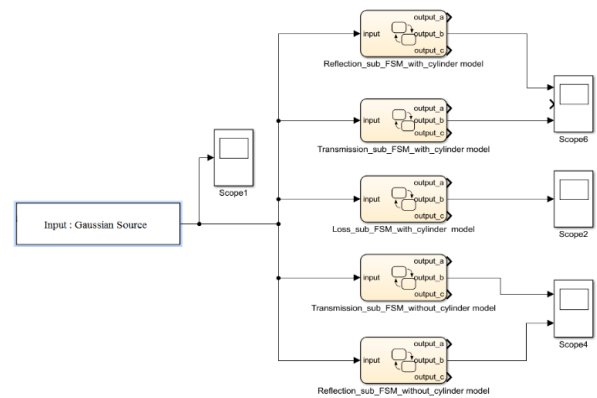


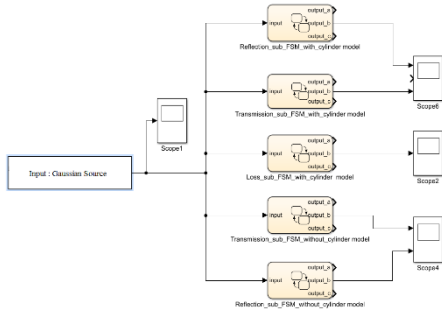
Fig. 13 Generic Plasmonic Biosensor using Finite State Machine M' by Integrating C-Code in State flow using Simulink

The Fig. 13 describes the generic biosensor block and sub-blocks which models the mathematical transformation equations accepting or rejecting the formal language L'. The Fig.13 describes the following details of sub-blocks of the Finite State System.

- Input: Gaussian source.
- 5 Sub-blocks of FSM
  - Transmission sub-blocks FSM
  - Reflection sub-block FSM
  - Loss sub-block FSM
- Input and Output scopes to monitor the behavior (scope<sub>1</sub>, scope<sub>2</sub>, scope<sub>4</sub> and scope<sub>6</sub>).

#### B. Biosensor Sub-systems Machine with Central Groove FSM based Model M'

# Modeling the Design of Plasmonic Biosensor Device by using Abstract Finite State Machine Model and FDTD Based MEEP Tool



**Fig. 14 Circular waveguide Plasmonic Biosensor with and without central cylinder using Finite State Machine by Integrating C-Code in State flow using Simulink**

The Fig. 14 describes the generic biosensor block and sub-blocks which models the mathematical transformation equations accepting or rejecting the formal language  $L'$ . It is modelled for both the with and without central groove,

- Input: Gaussian source.
- Sub-blocks of FSM
- Here transmission sub-block FSM, the transmission Vs input frequency is modelled.
- Here the reflection sub-block FSM, the transmission Vs input frequency is modelled.

The loss is modelled based on with and without central groove Loss sub-block FSM. The input and output scopes monitor the behavior.

### C. Mathematical Model and the Chart Plot of the FSM based Biosensor Device Behavior

The sub-section D to sub-section H describes the circular waveguide with and without central groove for biosensor sub-system's mathematical model equations. These equations are extracted using the curve fitting of the chart plots Fig. 7, Fig. 8, Fig. 9, Fig. 10, Fig. 11 and these equations are then injected into the FSM by integrating C-code into state flow machine, using Simulink for both circular waveguide with and without central cylinder groove for Plasmonic biosensor device behaviour. The significance of these equations is that they fundamentally model the same biosensor device's reflection, transmission and loss properties which can be easily integrated into FSM computing model as part of the design process of the biosensor device. The simulation results of the circular waveguide-based biosensor sub-system's FSM model. The measured fluxes for transmission, reflection fluxes and the losses with the Gaussian source as the input are shown in the chart plot Fig. 15, Fig. 16, Fig. 17, Fig. 18 and Fig. 19.

### D. Circular Waveguide: Frequency Vs Loss Equation

The polynomial Eq. 6 is obtained by the curve fitting in MATLAB using the data points of frequency Vs Loss chart plot. It shows the damping behavior as the frequency increases.

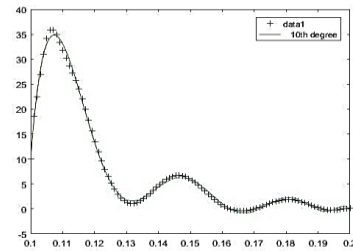
$$y = P_1(x^{10}) + P_2(x^9) + P_3(x^8) + P_4(x^7) + P_5(x^6) + P_6(x^5) + P_7(x^4) + P_8(x^3) + P_9(x^2) + P_{10}(x) + P_{11} \quad (6)$$

Where,

- Coefficients:  $P_1 = -3.5698e+15$ ,  $P_2 = 5.2519e+15$ ,  $P_3 = -3.451 + 2e+15$ ,  $P_4 = -1.334e+15$ ,

$$P_5 = -3.3586e+14, P_6 = 5.7565e+13, P_7 = -6.8034e+12, P_8 = 5.4768e+11, P_9 = -2.8753e+10, P_{10} = 8.8948e+08, P_{11} = -1.2321e+07$$

- Norm of residuals = 4.9934



**Fig. 15 Circular waveguide-Frequency Vs Loss**

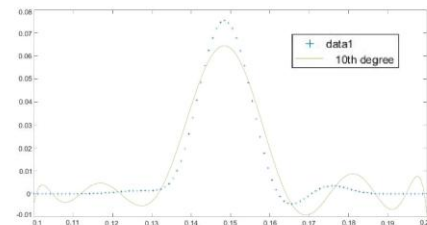
### E. Circular Waveguide with Cylinder: Frequency Vs Reflection Equation

The polynomial Eq. 7 is obtained by the curve fitting in MATLAB using the data points of frequency Vs reflection chart plot of circular waveguide with central cylinder. It shows the positive Gaussian behavior.

$$y = P_1(x^{10}) + P_2(x^9) + P_3(x^8) + P_4(x^7) + P_5(x^6) + P_6(x^5) + P_7(x^4) + P_8(x^3) + P_9(x^2) + P_{10}(x) + P_{11} \quad (7)$$

Where,

- Coefficients:  $P_1 = -4.9434e+13$ ,  $P_2 = 7.3703e+13$ ,  $P_3 = -4.9111e+13$ ,  $P_4 = 1.9257e+13$ ,  $P_5 = -4.9202e+12$ ,  $P_6 = 8.5584e+11$ ,  $P_7 = -1.0264e+11$ ,  $P_8 = 8.3788e+09$ ,  $P_9 = -4.4563e+08$ ,  $P_{10} = 1.3943e+07$ ,  $P_{11} = -1.9491e+05$
- Norm of residuals = 0.057416



**Fig. 16 Circular waveguide Frequency Vs Reflection with cylinder**

### F. Circular Waveguide with Cylinder: Frequency Vs Reflection Equation

The polynomial Eq. 8 is obtained by the curve fitting in MATLAB using the data points of frequency Vs Reflection chart plot of circular waveguide without central cylinder. It shows the positive Gaussian behavior.

$$y = P_1(x^{10}) + P_2(x^9) + P_3(x^8) + P_4(x^7) + P_5(x^6) + P_6(x^5) + P_7(x^4) + P_8(x^3) + P_9(x^2) + P_{10}(x) + P_{11} \quad (8)$$

Where,

- Coefficients:  $P_1 = -4.9297e+13$ ,  $P_2 = 7.3406e+13$ ,  
 $P_3 = -4.8849e+13$ ,  $P_4 = 1.9128e+13$ ,  
 $P_5 = -4.8804e+12$ ,  $P_6 = 8.4771e+11$ ,  
 $P_7 = -1.0151e+11$ ,  $P_8 = 8.2743e+09$ ,  
 $P_9 = -4.3939e+08$ ,  $P_{10} = 1.3726e+07$ ,  
 $P_{11} = -1.9157e+05$
- Norm of residuals = 0.057459

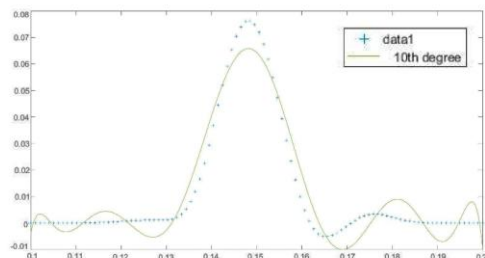


Fig. 17 Circular Waveguide - Frequency Vs Reflection without Cylinder

### G. Circular Waveguide with Cylinder: Frequency Vs Transmission Equation

The polynomial Eq. 9 is obtained by the curve fitting in MATLAB using the data points of frequency Vs transmission chart plot of circular waveguide with central cylinder. It shows the negative Gaussian behavior.

$$y = P_1(x^{10}) + P_2(x^9) + P_3(x^8) + P_4(x^7) + P_5(x^6) + P_6(x^5) + P_7(x^4) + P_8(x^3) + P_9(x^2) + P_{10}(x) + P_{11} \quad (9)$$

Where,

- Coefficients:  $P_1 = 1.1265e+12$ ,  $P_2 = -1.7304e+12$ ,  
 $P_3 = 1.1862e+12$ ,  $P_4 = -4.7771e+11$ ,  
 $P_5 = 1.2515e+11$ ,  $P_6 = 2.2284e+10$ ,  
 $P_7 = 2.7307e+09$ ,  $P_8 = -2.274e+08$ ,  
 $P_9 = 1.2316e+07$ ,  $P_{10} = -3.9174e+05$ ,  
 $P_{11} = 5558.3$
- Norm of residuals = 0.0009477

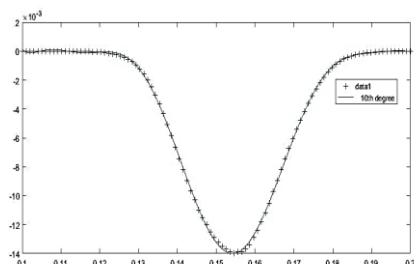


Fig. 18 Circular Waveguide - Frequency Vs Transmission with Cylinder

### H. Circular Waveguide without Cylinder: Frequency Vs Transmission Equation

The polynomial Eq. 10 is obtained by the curve fitting in MATLAB using the data points of frequency Vs transmission chart plot of circular waveguide without central cylinder. It shows the positive Gaussian behavior.

$$y = P_1(x^{10}) + P_2(x^9) + P_3(x^8) + P_4(x^7) + P_5(x^6) + P_6(x^5) + P_7(x^4) + P_8(x^3) + P_9(x^2) + P_{10}(x) + P_{11} \quad (10)$$

Where,

- Coefficients:  $P_1 = 8.5306e+11$ ,  $P_2 = -1.3169e+12$ ,  
 $P_3 = 9.0668e+11$ ,  $P_4 = -3.6657e+11$ ,  
 $P_5 = 9.6358e+10$ ,  $P_6 = -1.7205e+10$ ,  
 $P_7 = 2.1133e+09$ ,  $P_8 = -1.7631e+08$ ,  
 $P_9 = 9.5624e+06$ ,  $P_{10} = -3.0448e+05$ ,  
 $P_{11} = 4323$
- Norm of residuals = 0.00097021

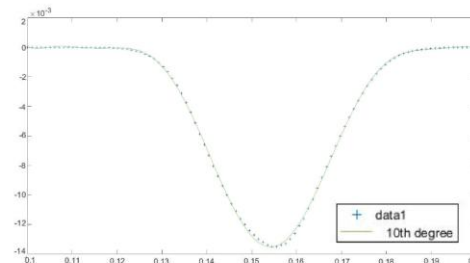


Fig. 19 Circular Waveguide - Frequency Vs Transmission without Cylinder

## VI. MEASUREMENT INFERENCE: FSM Vs MEEP MODELS SIMULATION

This paper develops the simulation model of biosensor using the two different approaches, one using the FSM and the another using MEEP based on FDTD model, for the transmission, reflection and the losses over the circular waveguide with or without the central cylinder groove. The two models using two different approaches for solving the design of the biosensor shows the similar pattern chart plots for both FSM and MEEP models. The circular waveguide's frequency Vs transmission with and without cylinder chart plot shows negative Gaussian. The circular waveguide's frequency Vs reflection with and without cylinder chart plot shows positive Gaussian. The model chart plot of circular waveguide losses follows the damping property. The importance of both the simulation models is that both can be used as a tool to understand the important parameters of transmission, reflection and loss for the given biosensor device. The measured results show similar behavior using both the MEEP and FSM simulation model, hence it can be seen that the FSM model can also be used as a simulation approach to design the biosensor device on the same lines of MEEP simulation model.

**VII. CONCLUSION**

The biosensor device and complete system design and development is very complex approach and exploring the legacy of powerful FSM as the abstract machine model, would help in reducing the complexity, simulation and design steps there by accelerating the different types of biosensor device development. The FSM design model applied to the biosensor device design and development process would help in the quick verification of the target biosensor device specification and its behaviour related to transmission, reflection and losses. Since it follows the machine abstraction, this approach can be applied to model other biosensor devices based on electrochemical, MEMS, piezoelectric principles to quantify other physical properties also. The FSM simulation model can be further expanded and explored to any of the biosensor device with different nanoscale patterns like Nano wells, Nano pyramids and others. Furthermore, future work exploration can be done on the FSM simulation of biosensor device which can also be integrated with the entire FSM of Artificial Intelligence based biosensor system model prototype.

**APPENDIX**

| APPENDIX -I   |           |              |            |
|---|-----------|--------------|------------|
| MEEP simulation: circular waveguide without central groove or cylinder flux as languages l' for the FSM |           |              |            |
|   | Frequency | Transmission | Reflection |
| flux1:  | 0.1       | -4.23E-08    | 4.05E-07   |
| flux1:  | 0.10101   | -6.33E-08    | 7.63E-07   |
| flux1:  | 0.10202   | -9.20E-08    | 1.40E-06   |
| flux1:  | 0.10303   | -1.33E-07    | 2.48E-06   |
| flux1:  | 0.10404   | -1.94E-07    | 4.18E-06   |
| flux1:  | 0.105051  | -2.88E-07    | 6.76E-06   |
| flux1:  | 0.106061  | -4.36E-07    | 1.05E-05   |
| flux1:  | 0.107071  | -6.66E-07    | 1.59E-05   |
| flux1:  | 0.108081  | -1.01E-06    | 2.34E-05   |
| flux1:  | 0.109091  | -1.53E-06    | 3.38E-05   |
| flux1:  | 0.110101  | -2.26E-06    | 4.81E-05   |
| flux1:  | 0.111111  | -3.30E-06    | 6.76E-05   |
| flux1:  | 0.112121  | -4.76E-06    | 9.38E-05   |
| flux1:  | 0.113131  | -6.79E-06    | 1.28E-04   |
| flux1:  | 0.114141  | -9.62E-06    | 1.72E-04   |
| flux1:  | 0.115152  | -1.36E-05    | 2.27E-04   |
| flux1:  | 0.116162  | -1.92E-05    | 2.95E-04   |
| flux1:  | 0.117172  | -2.71E-05    | 3.74E-04   |
| flux1:  | 0.118182  | -3.81E-05    | 4.67E-04   |
| flux1:  | 0.119192  | -5.32E-05    | 5.70E-04   |
| flux1:  | 0.120202  | -7.40E-05    | 6.83E-04   |
| flux1:  | 0.121212  | -1.02E-04    | 8.01E-04   |
| flux1:  | 0.122222  | -1.40E-04    | 9.19E-04   |

|        |          |            |          |
|--------|----------|------------|----------|
| flux1: | 0.123232 | -1.90E-04  | 0.001029 |
| flux1: | 0.124242 | -2.56E-04  | 0.001119 |
| flux1: | 0.125253 | -3.42E-04  | 0.00118  |
| flux1: | 0.126263 | -4.55E-04  | 0.001205 |
| flux1: | 0.127273 | -6.01E-04  | 0.001193 |
| flux1: | 0.128283 | -7.87E-04  | 0.001164 |
| flux1: | 0.129293 | -0.0010206 | 0.001157 |
| flux1: | 0.130303 | -0.0013108 | 0.001247 |
| flux1: | 0.131313 | -0.0016636 | 0.001546 |
| flux1: | 0.132323 | -0.0020838 | 0.002201 |
| flux1: | 0.133333 | -0.002573  | 0.003385 |
| flux1: | 0.134343 | -0.0031292 | 0.005286 |
| flux1: | 0.135354 | -0.0037466 | 0.008072 |
| flux1: | 0.136364 | -0.0044158 | 0.011872 |
| flux1: | 0.137374 | -0.005124  | 0.016739 |
| flux1: | 0.138384 | -0.0058567 | 0.022632 |
| flux1: | 0.139394 | -0.0065986 | 0.029403 |
| flux1: | 0.140404 | -0.0073349 | 0.036801 |
| flux1: | 0.141414 | -0.0080526 | 0.044489 |
| flux1: | 0.142424 | -0.0087411 | 0.05208  |
| flux1: | 0.143434 | -0.0093923 | 0.059173 |
| flux1: | 0.144444 | -0.0100013 | 0.065388 |
| flux1: | 0.145455 | -0.0105651 | 0.070407 |
| flux1: | 0.146465 | -0.0110827 | 0.073984 |
| flux1: | 0.147475 | -0.011554  | 0.075962 |
| flux1: | 0.148485 | -0.0119795 | 0.076264 |
| flux1: | 0.149495 | -0.012359  | 0.07489  |
| flux1: | 0.150505 | -0.0126916 | 0.071906 |
| flux1: | 0.151515 | -0.0129748 | 0.06744  |
| flux1: | 0.152525 | -0.0132038 | 0.061676 |
| flux1: | 0.153535 | -0.013372  | 0.054855 |
| flux1: | 0.154545 | -0.0134707 | 0.047272 |
| flux1: | 0.155556 | -0.0134901 | 0.039264 |
| flux1: | 0.156566 | -0.0134201 | 0.031194 |
| flux1: | 0.157576 | -0.0132524 | 0.023421 |
| flux1: | 0.158586 | -0.0129819 | 0.016269 |
| flux1: | 0.159596 | -0.012608  | 0.010004 |
| flux1: | 0.160606 | -0.0121359 | 0.004803 |
| flux1: | 0.161616 | -0.0115763 | 7.53E-04 |
| flux1: | 0.162626 | -0.0109448 | -0.00215 |
| flux1: | 0.163636 | -0.0102603 | -0.00399 |
| flux1: | 0.164646 | -0.0095427 | -0.0049  |
| flux1: | 0.165657 | -0.0088109 | -0.00505 |
| flux1: | 0.166667 | -0.0080811 | -0.00459 |
| flux1: | 0.167677 | -0.0073652 | -0.00372 |
| flux1: | 0.168687 | -0.0066713 | -0.00258 |
| flux1: | 0.169697 | -0.0060035 | -0.00131 |





|        |          |            |           |
|--------|----------|------------|-----------|
| flux1: | 0.170707 | -0.0053635 | -4.50E-05 |
| flux1: | 0.171717 | -0.004752  | 0.001117  |
| flux1: | 0.172727 | -0.0041699 | 0.002092  |

|        |            |            |          |
|--------|------------|------------|----------|
| flux1: | 0.13636364 | -0.004338  | 0.010081 |
| flux1: | 0.13737374 | -0.0050748 | 0.014388 |
| flux1: | 0.13838384 | -0.0058475 | 0.019763 |
| flux1: | 0.13939394 | -0.0066396 | 0.026111 |
| flux1: | 0.14040404 | -0.0074343 | 0.033225 |
| flux1: | 0.14141414 | -0.0082153 | 0.040798 |
| flux1: | 0.14242424 | -0.0089686 | 0.048451 |
| flux1: | 0.14343434 | -0.0096827 | 0.055772 |
| flux1: | 0.14444444 | -0.0103492 | 0.062354 |
| flux1: | 0.14545455 | -0.0109633 | 0.067837 |
| flux1: | 0.14646465 | -0.0115216 | 0.071936 |
| flux1: | 0.14747475 | -0.0120245 | 0.074453 |
| flux1: | 0.14848485 | -0.0124723 | 0.075282 |
| flux1: | 0.14949495 | -0.0128663 | 0.0744   |
| flux1: | 0.15050505 | -0.0132053 | 0.071859 |
| flux1: | 0.15151515 | -0.0134887 | 0.067779 |
| flux1: | 0.15252525 | -0.0137123 | 0.062342 |
| flux1: | 0.15353535 | -0.0138691 | 0.055786 |
| flux1: | 0.15454545 | -0.0139513 | 0.048407 |
| flux1: | 0.15555556 | -0.0139493 | 0.040542 |
| flux1: | 0.15656566 | -0.0138527 | 0.032556 |
| flux1: | 0.15757576 | -0.0136547 | 0.024815 |
| flux1: | 0.15858586 | -0.0133507 | 0.017651 |
| flux1: | 0.15959596 | -0.0129414 | 0.011336 |
| flux1: | 0.16060606 | -0.0124333 | 0.006061 |
| flux1: | 0.16161616 | -0.0118376 | 0.001918 |
| flux1: | 0.16262626 | -0.0111716 | -0.00109 |
| flux1: | 0.16363636 | -0.0104544 | -0.00304 |
| flux1: | 0.16464646 | -0.0097065 | -0.00406 |
| flux1: | 0.16565657 | -0.0089468 | -0.00431 |
| flux1: | 0.16666667 | -0.0081916 | -0.00396 |

| APPENDIX -II  |            |               |            |
|---|------------|---------------|------------|
| MEEP simulation: circular waveguide with central groove or cylinder flux as languages l'' for the FSM |            |               |            |
|   | Frequency  | Transmissi on | Reflection |
| flux1:  | 0.1        | -4.11E-08     | 4.22E-07   |
| flux1:  | 0.1010101  | -6.26E-08     | 8.02E-07   |
| flux1:  | 0.1020202  | -9.19E-08     | 1.45E-06   |
| flux1:  | 0.1030303  | -1.33E-07     | 2.51E-06   |
| flux1:  | 0.1040404  | -1.92E-07     | 4.18E-06   |
| flux1:  | 0.10505051 | -2.82E-07     | 6.71E-06   |
| flux1:  | 0.10606061 | -4.23E-07     | 1.05E-05   |
| flux1:  | 0.10707071 | -6.40E-07     | 1.59E-05   |
| flux1:  | 0.10808081 | -9.71E-07     | 2.35E-05   |
| flux1:  | 0.10909091 | -1.46E-06     | 3.43E-05   |
| flux1:  | 0.11010101 | -2.17E-06     | 4.91E-05   |
| flux1:  | 0.11111111 | -3.18E-06     | 6.92E-05   |
| flux1:  | 0.11212121 | -4.58E-06     | 9.61E-05   |
| flux1:  | 0.11313131 | -6.54E-06     | 1.31E-04   |
| flux1:  | 0.11414141 | -9.26E-06     | 1.77E-04   |
| flux1:  | 0.11515152 | -1.31E-05     | 2.34E-04   |
| flux1:  | 0.11616162 | -1.84E-05     | 3.05E-04   |
| flux1:  | 0.11717172 | -2.58E-05     | 3.91E-04   |
| flux1:  | 0.11818182 | -3.62E-05     | 4.91E-04   |
| flux1:  | 0.11919192 | -5.05E-05     | 6.06E-04   |
| flux1:  | 0.12020202 | -7.01E-05     | 7.34E-04   |
| flux1:  | 0.12121212 | -9.67E-05     | 8.72E-04   |
| flux1:  | 0.12222222 | -1.32E-04     | 0.001013   |
| flux1:  | 0.12323232 | -1.79E-04     | 0.001151   |
| flux1:  | 0.12424242 | -2.42E-04     | 0.001276   |
| flux1:  | 0.12525253 | -3.23E-04     | 0.001377   |
| flux1:  | 0.12626263 | -4.29E-04     | 0.001444   |
| flux1:  | 0.12727273 | -5.66E-04     | 0.001472   |
| flux1:  | 0.12828283 | -7.42E-04     | 0.001471   |
| flux1:  | 0.12929293 | -9.64E-04     | 0.001465   |
| flux1:  | 0.13030303 | -0.0012412    | 0.00151    |
| flux1:  | 0.13131313 | -0.0015811    | 0.001696   |
| flux1:  | 0.13232323 | -0.0019901    | 0.00215    |
| flux1:  | 0.13333333 | -0.002472     | 0.003034   |
| flux1:  | 0.13434343 | -0.003027     | 0.004532   |
| flux1:  | 0.13535354 | -0.0036515    | 0.006828   |



# Modeling the Design of Plasmonic Biosensor Device by using Abstract Finite State Machine Model and FDTD Based MEEP Tool

|        |            |            |           |
|--------|------------|------------|-----------|
| flux1: | 0.16767677 | -0.0074528 | -0.00319  |
| flux1: | 0.16868687 | -0.0067383 | -0.00214  |
| flux1: | 0.16969697 | -0.0060524 | -9.57E-04 |
| flux1: | 0.17070707 | -0.0053968 | 2.38E-04  |
| flux1: | 0.17171717 | -0.0047722 | 0.001341  |
| flux1: | 0.17272727 | -0.0041794 | 0.002269  |
| flux1: | 0.17373737 | -0.0036201 | 0.002964  |
| flux1: | 0.17474747 | -0.0030972 | 0.003397  |
| flux1: | 0.17575758 | -0.0026144 | 0.003568  |
| flux1: | 0.17676768 | -0.0021759 | 0.003502  |
| flux1: | 0.17777778 | -0.0017854 | 0.003246  |
| flux1: | 0.17878788 | -0.0014438 | 0.002859  |
| flux1: | 0.17979798 | -0.0011526 | 0.0024    |
| flux1: | 0.18080808 | -9.10E-04  | 0.001925  |
| flux1: | 0.18181818 | -7.11E-04  | 0.001475  |
| flux1: | 0.18282828 | -5.52E-04  | 0.001081  |
| flux1: | 0.18383838 | -4.26E-04  | 7.55E-04  |
| flux1: | 0.18484848 | -3.28E-04  | 5.00E-04  |
| flux1: | 0.18585859 | -2.52E-04  | 3.10E-04  |
| flux1: | 0.18686869 | -1.93E-04  | 1.77E-04  |
| flux1: | 0.18787879 | -1.47E-04  | 8.77E-05  |
| flux1: | 0.18888889 | -1.12E-04  | 3.19E-05  |
| flux1: | 0.18989899 | -8.37E-05  | -8.93E-08 |
| flux1: | 0.19090909 | -6.21E-05  | -1.58E-05 |
| flux1: | 0.19191919 | -4.53E-05  | -2.11E-05 |
| flux1: | 0.19292929 | -3.25E-05  | -2.04E-05 |
| flux1: | 0.19393939 | -2.29E-05  | -1.67E-05 |
| flux1: | 0.19494949 | -1.59E-05  | -1.20E-05 |
| flux1: | 0.1959596  | -1.08E-05  | -7.78E-06 |
| flux1: | 0.1969697  | -7.28E-06  | -4.46E-06 |
| flux1: | 0.1979798  | -4.85E-06  | -2.21E-06 |
| flux1: | 0.1989899  | -3.21E-06  | -9.08E-07 |
| flux1: | 0.2        | -2.11E-06  | -2.72E-07 |

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