

Implementation of Twin Precision-Reduced Computation Modified Booth Multiplier in FPGA

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Abstract: Multipliers can be implemented either in ASIC or FPGA. Comparing FPGAs to ASICs, FPGAs are very flexible. Adding to this, a significant advantage of FPGAs over ASICs is reconfigurability and hardware reusability. FPGA is said to be more advantageous than ASIC multipliers because of its internal optimization algorithms. This research is narrowed down to exploit the advantages of FPGA. Multiplication is a complex process and it is hard to be implemented in hardware environments like ASIC. The process of multiplication consumes more hardware resulting in delay and high power dissipation in ASIC, which is a non-reusable hardware. The complexity in multiplication in ASIC is the problem statement which causes increase in metrics like area, power and delay.

I. INTRODUCTION

Multiplication (Series of repeated additions) is an essential function in basic arithmetic operations, especially in signal processing applications, includes graphics and computation system (Mead, C. and Conway, L., 1988). The factorization of a large number checks whether a number is prime. It depends on multiplication. Multiplicand is the number that is added and the result of it is the product. The number of times that the multiplicand is added is called as the multiplier (Meng, T., 1989). In most of the digital systems such as computers, the bitwidths of the given operands will be the same. Generally, when two operands are multiplied, the outcome has a length which is twice that of the input. The multiplier always saves this information (Miller, R.E., 1965).

Merits of implementation of TP in RCMB: TP technique is used to implement two $N/2$ operations. It is executed with the same N bit multiplier. N is termed as the bitwidth of the multiplier. Also, as signed multipliers are in common usage, the unsigned TP technique is implemented in signed multipliers like MB and BW. The optimization is done in the TP application in RCMB (Reduced Computation Modified Booth) with less number of MUXes and the results are simulated using Xilinx in FPGA environment. The greatest merit of this proposed work is that by implementing two $N/2$ multiplications in a single N bit multiplier, double throughput is achieved.

II. LITERATURE REVIEW

Parallel multipliers: M. C. Wen et al., (2005) clarifies a low-power parallel multiplier configuration,

in which a few sections in the multiplier array can be turned off at whatever point their yields are known. This outline keeps up the original structure without presenting additional limit cells, just like the case in past plans. Trial results demonstrate that it spares 10% of power for random inputs. Higher power reduction can be accomplished if the operands contain the greater number of 0's than 1's.

Truncated multipliers: The work done in Muhammad H. Rais (2010) gives the explanation in the advancement cost for ASICs. This exploration displayed the relative investigation of Spartan-3AN, Virtex-4 and Virtex-5 FPGA devices. The execution of standard and truncated multipliers utilizes Very High Speed Integrated Circuit Hardware Description Language (VHDL). A remarkable decrease in FPGA resources, delay, and power was accomplished utilizing truncated multipliers rather than standard parallel multipliers when the full accuracy of the standard multiplier is not required. The three devices indicated a huge change for truncated multipliers when contrasted with standard multipliers. Results demonstrated that the inconsistency in Spartan-3AN average connection and most extreme pin delay had been proficiently diminished in Virtex-4 and Virtex-5 devices. The Virtex-5 FPGA device demonstrated better execution when contrasted with Spartan-3 and Virtex-4 FPGA devices.

Bypassing Multipliers: The work done in Yin-Tsung Hwang et al.,(2007) concentrates on the column bypassing construct multiplier outlines and focuses on power saving and area. Bypassing is the system utilized as a part of the power saving where a customary Complementary Metal Oxide Semiconductor (CMOS) 28T full adder is received as the base configuration. Other outline choices are likewise investigated. One such is to utilize a 28T full adder design which can be partitioned into two segments, one for the carry logic and the other for the sum logic. The carry logic is an AND-OR-INVERT (AOI) gate took after by an inverter. The complemented carry out signal is likewise bolstered to the sum logic as input. The sum logic is another AOI gate additionally taken after by an inverter. To execute row bypassing plan, two systems are required. Signal multiplexing between the bypassing signal, the assessed signal and evaluation suspension of circumventing full adder. In this paper, CMOS hardware is received to fill both needs which consolidate the function of logic assessment and transmission gate into one and requires lesser area.

Revised Manuscript Received on May 22, 2019.

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(a) Twin Precision-Modified Booth Multiplier:

TP is a technique to obtain double output in integer multipliers. With the TP technique, the multipliers adopt to the bitwidth of the operands being computed, which result in reduced power dissipation.

By this technique, computational throughput is also increased because many narrow width operations are computed in parallel.

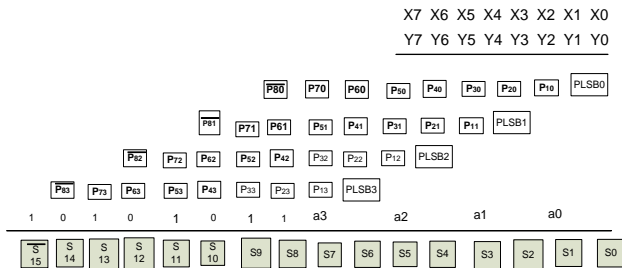


Fig. 1 Signed 8-bit Multiplication using MB Algorithm – An N-bit Multiplication

(M. Sjalander and Per Larsson-Edefors, 2009)

Normally, TP multiplier either performs N bit multiplication or $N/2$ bit multiplication. The output for a N bit multiplication is from S_0 to S_{15} as depicted in Fig.1. Fig.1 illustrates the MB multiplication for 8×8 which uses recoding logic proposed by Yeh, W.C. and Jen, C. W., (2000). Implementation of TP technique varies for BW and

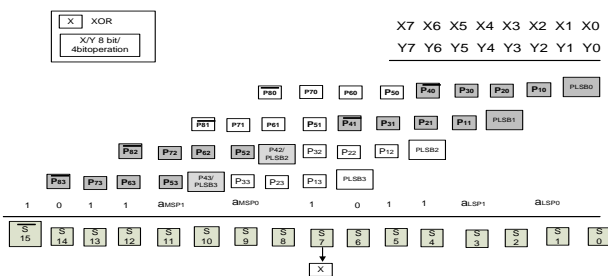


Fig. 2 Implementation of TP in MB Multiplier - N/2 Multiplications

(M. Sjalander and Per Larsson-Edefors, 2009)

MB algorithm. Similarly, S_0 to S_7 and S_8 to S_{15} are the twin outputs for a $N/2$ bit multiplication, shown in Fig.2.

The outcome of the encoding and decoding logic is the generation of PP array in MB multiplication. Therefore double throughput can be achieved only if changes are accommodated in the recoded N -bit PP array. In MB algorithm the last row in the PP array is meant for an inclusion of sign bit pattern i.e. either 1 or 0. This is due to the negative decoding of MBE. Therefore the number of partial products which has to reduce from N number of PP rows to $N/2$ rows becomes $[N/2] + 1$. In this paper (M. Sjalander and Per Larsson-Edefors, 2009) it is explained that the last row in the PP array is due to 1's and 0's and a_i , which is caused by precomputation of P_{LSB} . Implementation in MB multiplication using twin precision technique (M. Sjalander and Per Larsson-Edefors, 2009) is illustrated in Fig.2. It consists of $[N/2] + 1$ rows and results in a double throughput.

By comparing Fig.1 and Fig.2, the changes needed for the TP implementation of 8×8 MB multiplication at each

column are tabulated in Table I. The changes between N or $N/2$ bit multiplication is brought by MUXes. In N -bit multiplication (Fig.1), the S_4 column usually has no sign bit. However, a $N/2$ LSP multiplication requires a sign bit in the same column. Also, there is a need for inversion of MSB bit (P_{40}) in the same place. This is done using MUXes. Similar changes in all the other columns are also done using MUXes.

The following changes are required for the $N/2$ MSP multiplication: sign bit pattern 1's and 0's, precomputed LSB (P_{LSB2} , P_{LSB3}) and the potential carry (a_{MSP0} , a_{MSP1}) which is tabulated in Table I. Totally, for a 16×16 TP MB multiplication, nineteen MUXes are needed. For various bitwidths, the MUX utilization is calculated. From the analysis made, for implementation of TP in MB (M. Sjalander and Per Larsson-Edefors, 2009), it is clear that this method inquires (bitwidth+ 3) MUXes.

Table. 1 Changes needed for Twin Precision in a N bit MB Multiplier

Sum bit	Twin 2009
	PPs selection
S_0	No change
S_1	No change
S_2	No change
S_3	No change
S_4	$1/0$ and $\overline{P_{40}}/P_{40}$
S_5	$1/a_2$
S_6	$\overline{P_{41}}/P_{41}$
S_7	$0/a_3$
S_8	P_{LSB2}/P_{42} and $0/1$
S_9	$a_{MSP0}/1$
S_{10}	P_{LSB3}/P_{43}
S_{11}	$a_{MSP1}/1$
S_{12}	$1/0$
S_{13}	No change
S_{14}	No change
S_{15}	No change

TP implementation to signed multipliers is made in (M.Sjalander and Per Larsson-Edefors, 2009) and further optimization in TP multiplier is not done. There is a generation of $[N/2] + 1$ PP rows in TP implementation; it adopts sign extension scheme presented in (J. Fadavi-Ardekani, 1993). TP implementation in MB (J. Fadavi-Ardekani, 1993) requires that more changes are to be made for $N/2$ bit multiplication as it adopts a sign extension scheme. As many the changes, in a $N/2$ bit multiplication that much is the need for MUXes. They are deployed to select required PPs for N and $N/2$ bit multiplications.

For twin precision implementation in MB algorithm (M. Sjalander and Per Larsson-Edefors, 2009), Booth encoding and decoding is required. Then inclusion of P_{LSB} is done.

Along with this, there is a need for potential carry (a_{MSP}). These steps are done distinctly for both $N/2$ LSP and MSP multiplications. And also sign extension has to be made separately for the two $N/2$ bit multiplications. In RCMB (FabrizioLamberti et al., 2011), the following steps are performed for a $N/2$ bit multiplication:

- (i) Booth encoding and decoding, (ii) neg bit is added in the LSB of each PP row for two's complement representation, (iii) 1's are added for sign extension.

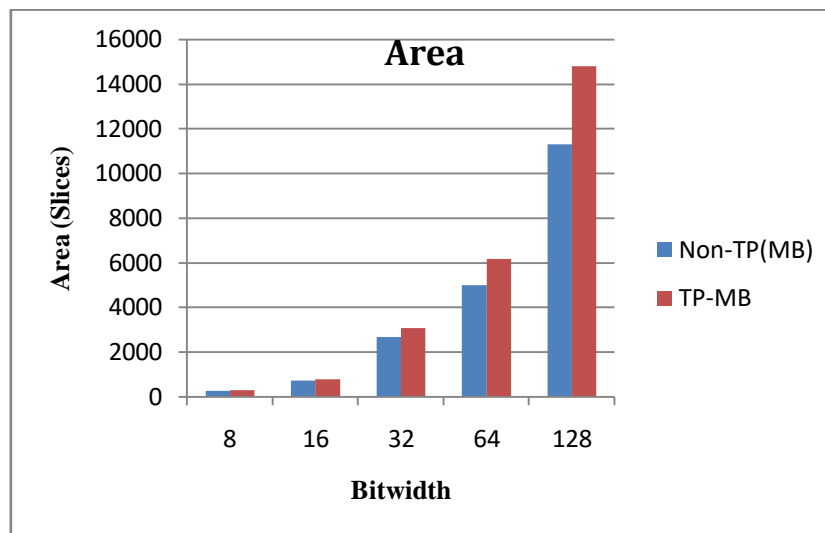
There is no requirement for the inclusion of P_{LSB} and potential carry in RCMB. This reduces the complexity of the system. So this makes it suitable for TP implementation and therefore, utilization of MUXes gets reduced. For an 8×8 TP multiplier, twin 2009 (M. Sjalander and Per Larsson-Edefors, 2009) requires eleven MUXes. Similarly for the implementation of a 16×16 TP multiplier, nineteen MUXes are required which is tabulated in Table II. Therefore the total MUX requirement for TP implementation in MB is formulated as $N+3$. Also, it gives the simulated results of MB and TP-MB using Xilinx software. Fig.3 (a), (b) & (c) illustrates the changes in the area, power, and delay in the implementation of TP in MB multiplier.

TP-MB in ASIC environment was given (M. Sjalander and Per Larsson-Edefors, 2009), whereas Table II gives the same in FPGA environment. This is done for evaluating the performance of the same with TP-RCMB in FPGA. Normally to achieve double throughput (twin output), N bit and $N/2$ bit multipliers are required. However, by implementing TP technique, the same double throughput is achieved not at the cost of twice the area required for N bit and $N/2$ bit multiplications but with a slight increase in area of 7.2% to 23.7%, an increase in delay of 6.5% to 21.6 % and an increase in power of 10% to 36.5 % for varying bit widths of $N=8$ to 128 bits, which is graphically represented in Fig. 3. This is due to the MUX requirement and the logic incorporated to make the unwanted PPs to zero.

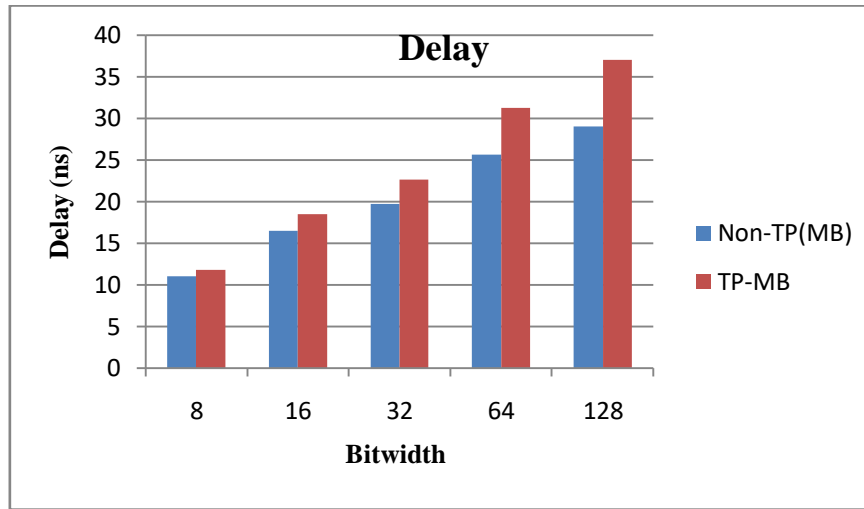
Double throughput in FPGA environment is achieved effectively by implementing TP technique in MB. This chapter also explains the different kinds of MB encoders and decoders. Also, mapping of the PPs to an HPM tree is described in this chapter. This implementation requires less changes in the PP array to acquire TP. Selection of appropriate PPs for N or $N/2$ bit multiplication is satisfied by the MUX utilization. The discussion of implementation of TP-MB formulates the MUX requirement as $N+3$.

Table. 2 Simulated Results of MB and TP-MB using Xilinx

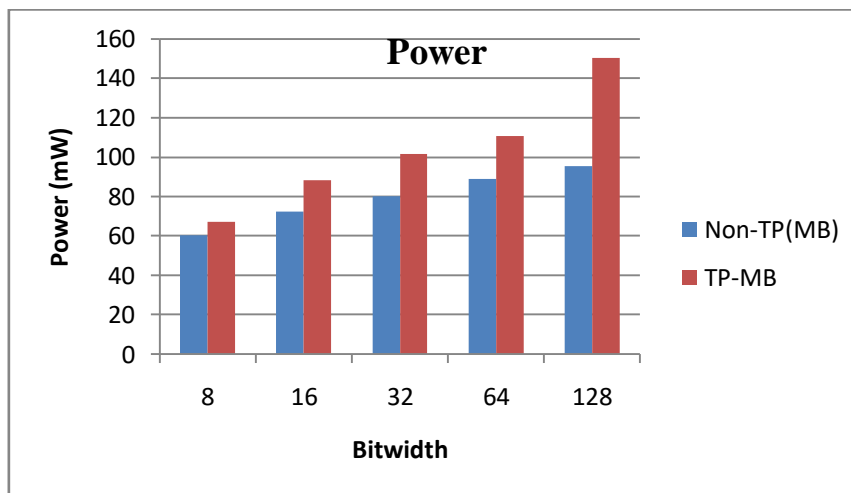
	Non-TP (MB)					TP-MB				
Bitwidth	8	16	32	64	128	8	16	32	64	128
MUX	-	-	-	-	-	11	19	35	67	131
Area (slices)	259	704	2656	5001	11287	279	788	3080	6159	14785
Delay (ns)	11.021	16.50	19.72	25.63	29	11.79	18.48	22.67	31.26	37
Power (mW)	60.34	72.40	80.13	88.95	95.3	67.34	88.32	101.44	110.80	150.11



(a)



(b)



(c)

Fig. 3 (a) Bitwidth vs Area (b) Bitwidthvs Delay (c) Bitwidthvs Power

Twin Precision Reduced Computation Modified Booth Multiplier in FPGA:

Here the performance of a RCMB multiplier with TP technique implemented in FPGA is explained. The multiplier results in double throughput. TP technique is an efficient way to obtain double throughput in the multipliers. The idea of implementing the TP technique to RCMB is done in ASIC (Asirvatham.R. and Ramachandran.S., 2015) environment. The optimization is done by reducing the MUX utilization. But in the case of ASIC, the power consumption increases per unit die size than that in FPGA. Therefore, if optimization is done in FPGA, it is an added advantage.

Algorithm for obtaining TP in RCMB

1. $M_{RC}\{p, q\}$ - Matrix set with reduced complexity

$$p = 1 \text{ to } \frac{N}{2}; q = 1 \text{ to } 2N;$$

N = Bitwidth; M_{RC} consists of equal number of bits in each row.

2. For $N = 8$, upper limit = $U_L\{p_1, p_2\}$; lower limit = $L_L\{p_3, p_4\}$

3. $(PP_{p,q} \in (p, q))$; Partial product is an element of p and q

4. $T_B = N + 3$; T_B = total number of bits per row.

5. Negation and inclusion of sign bit 1s are needed for TP

(i) Negation of bit MSB is done necessarily. It is achieved by performing $N/2$ LSB multiplication which is given as $BT[L_p]$. L_p value gives relative bit position in the p^{th} row so that negation of MSB can be made correctly.

$$\text{for } \begin{cases} p = 1; L = L_p = T_B - U_N \\ p = 2 \text{ to } \frac{N}{4}; L = L_p = L_{(p-1)} + 2 \end{cases} \quad (1)$$

$BT[L_p]$ - Bit (BT) position (L) in the corresponding p row

$$U_N = \frac{N}{2} + 2 \quad (2)$$

U_N - Unchanging value based on N

(ii-a) Inclusion of 1s in subsequent columns (q) are made for following iterations

Iteration (I) = 1 to $(N/4) + 1$

$$\text{for } \begin{cases} I = 1 & q_{uo(I)} = q_{uo(1)} = \left(\frac{N}{2}\right) + 1 \\ I = 2 & q_{uo(I)} = q_{uo(2)} = \left(\frac{N}{2}\right) + 2 \\ I = 3 \text{ to } (N/4) + 1 & q_{uo(I)} = q_{uo(I-1)} + 2 \end{cases} \quad (3)$$

$q_{uo(I)}$ denotes the upper (U) limit in the corresponding column (q) and the ones (O) in it for corresponding iteration (I).

(ii-b)

$$OL_{L(q)} = \left(\frac{N}{2} + 1 + N\right) \quad (4)$$

$OL_{L(q)}$ denotes the inclusion of 1s in the lower limit in the corresponding column q .

6. Negative bits (negk) are included in the LSB position of each PP row for $N/2$ MSP multiplication. For this, the column (q) on row (p) is to be known. The variation of k is from 0 to $(N/2 - 1)$.

$$\text{for } \begin{cases} \text{negk} \rightarrow q_{(p)} \\ p = \frac{N}{4} + 1, k = \frac{N}{4}, q_{(p)} = N + 1 \\ p = \left(\frac{N}{4} + 2 \text{ to } N/2\right), k = \left(\left(\frac{N}{4} + 1\right) \text{ to } \left(\frac{N}{2} - 1\right)\right), q_{(p)} = q_{(p-1)} + 2 \end{cases} \quad (5)$$

$p = \text{row}, q = \text{column}$

$$T_B = N + 3 \quad (6)$$

T_B denotes the number of bits in a row.

For an 8×8 RCMB multiplier illustrated in Fig. 4, $T_B = 11$ and this is constantly the same for all the rows. When $N/2$ LSP multiplication is performed, the most significant bit in each PP row has to be negated. The bit position (L_p) in the upper limit is given as $BT[L_p]$, given in Equation (1). It is to be known for the inversion step to be processed and BT is the bit and L_p denotes the bit position in the corresponding row (p). The inversion of bits is carried out during an N -bit multiplication. That itself is sufficient for the lower limit $N/2$ MSP multiplication. The bits are negated on the upper limit and it is described in Equation (1).

For rows $p = 1$ to $N/4$, the inversion of bits $BT[L_p]$ is done. For initial conditions $p = 1$, $[L_p]$ is the difference between total bits $T_B(p)$ in a single row and the unchanging value U_N .

$BT[L_p]$ denotes the position of the bit in the subsequent p^{th} row.

U_N is the unchanging value which is based on N value.

For $N = 16$, the inversion of the eleventh, thirteenth and fifteenth bits is required. For $N = 8$, the values of $L_1 = 5$ and $L_2 = 7$. Hence, the inversion of the fifth and seventh bits is done in the upper limit as shown in Fig.4.

For the lower part of the twin multiplication to be done, some changes are made in the upper limit and some in the lower limit for the other part of the twin implementation. For a 2's complement representation, sign extension scheme includes 1s in the suitable column. More changes are required in upper limit. So in this algorithm for obtaining TP, an inclusion of 1s for a 2's complement representation in corresponding column (q) is performed in the upper limit according to Equation (3).

The implementation of TP in RCMB gives better performance compared to the existing Twin (M. Sjalander and Per Larsson-Edefors, 2009) and TP-RCMB implementation in ASIC environment (Asirvatham R. and Ramachandran S., 2015). This implementation yields less MUX utilization. The hardware complexity, latency and power calculation is analyzed. In the existing work, changes made for N and $N/2$ bit multiplications are selected using MUXes, which increase the design complexity of the multiplier. But the same is reduced in TP-RCMB in FPGA. One significant reason is the reduction of PP row height. Other reasons are certainly the optimizations provided by the FPGA.

The sign extension in a 2's complement representation is prevented by the addition of sign bit pattern 1's and 0's. This varies for N and $N/2$ bit multiplication. Bit position is significant for particular column p ; otherwise the sum bit becomes erroneous. But ruling out the particular column q is sufficient in adding 1's. Therefore, it is not necessary to rule out the bit position. $q_{uo(I)}$ denotes the upper (U) limit in the corresponding column (q) and the ones (O) in it for corresponding iteration (I).

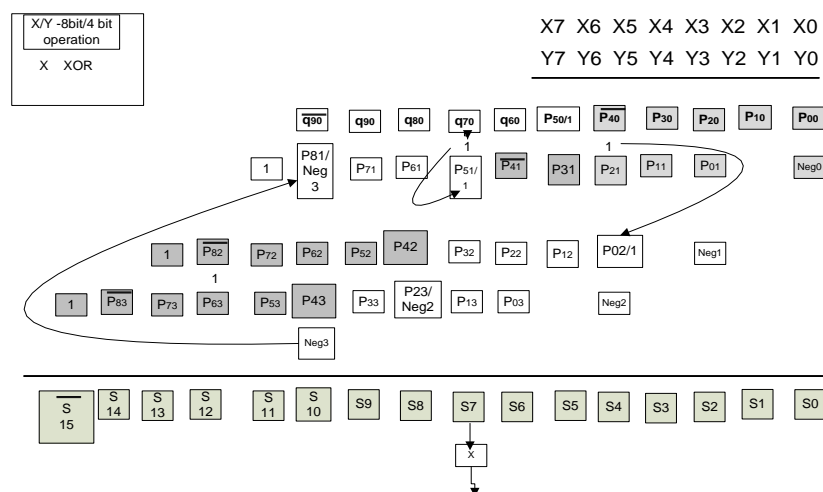


Fig. 4 Implementation of TP-RCMB to Obtain Twin Output

So in the ninth, tenth and twelfth and fourteenth columns, the 1s are inserted. Similarly for $N=8$, the iterations are from 1 to 3. Insertion of 1s is done in the fifth, sixth and eighth columns. The variation of each iteration ranges from the first PP row to one-fourth of the full bit

width plus one. A '1' is added in the columns $\left(\frac{N}{2}\right) + 1$ and $\left(\frac{N}{2}\right) + 2$ for iteration I=1 and 2. The consecutive values of I is the total of previous iteration value and a two. In Fig.4, the '1' that is inserted in the fifth column is joined with PP, P02 and is represented as P02/1 for a Full/Twin in the Least Significant Part. MUXes are used for selection between signals.

A combination of P50 and 1 is put up in the 6th column. To prevent the N/2 MSP multiplication from the carry of the previous LSP multiplication affecting the second half, a '1' is inserted in the eighth column which passes through a XOR gate. Hence the S(N-1) gets negated. A '1' is added in the 13th column in the lower limit for the TP implementation as per Equation (4) for a value of N=8. It is not necessary to put extra effort to insert 1s in the lower limit for N/2 MSP multiplication. The sign bits allotted for a full precision multiplication of RCMB can be very well used.

The 8×8 RCMB multiplier is chosen to explain the proposed idea. From the consolidated changes, it is revealed that $[N/2]+3$ MUXes are entailed for TP-RCMB and verified for various bitwidths, as charted in Table III. Nearly 41% to 47% (for $N = 8$ to 128) of less MUXes utilized compared to the previous work (M. Sjalander and Per Larsson-Edefors, 2009). The concept of optimization is not done (M. Sjalander and Per Larsson-Edefors, 2009) in TP implementation. Though the work of TP optimization is extended to signed multipliers in ASIC environment (Asirvatham R. and Ramachandran S., 2015), the parameters influencing the design are less appreciable. Compared to the prior work (M. Sjalander and Per Larsson-Edefors, 2009), the method of implementation requires fewer changes for performing $aN/2$ operation. These changes in PPs are typically selected using MUXes. The proposed TP in RCMB method decreases the area and delay as the design and project cycle in FPGA are smaller than those in ASIC.

Table. 3 Changes to be made to Implement TP in RCMB

SUM BIT	FULL PRECISION RCMB	TP RCMB	SIGNAL SELECTION (Change/No Change)
S ₁₅	1	1	No Change
S ₁₄	$\overline{P83}$	$\overline{P83}$	No Change
S ₁₃	P73,1	P73,1	No Change
S ₁₂	$\overline{P82}$, p63	$\overline{P82}$, p63,1	No Change
S ₁₁	1, p72, p53	1, p72, p53	No Change
S ₁₀	$\overline{q90}$, $\overline{P81}$, p62, p43	$\overline{q90}$, p81/neg3, p62, p43	One Change
S ₉	q90, p71, p52, p33	q90, p71, p52, p33	No Change
S ₈	q80, p61, p42, p23	q80, p61, p42, p23/neg2	One Change
S ₇	q70, p51/1, p32, p13	q70, p51, p32, p13	One Change
S ₆	q60, p41, p22, p03	q60, $\overline{P41}$, p22, p03	One Change
S ₅	P50, p31, p12	P50/1, p31, p12	One Change
S ₄	P40, p21, p02, neg2	P40/ $\overline{P40}$, p21, p02/1, neg2	Two Changes
S ₃	P30, p11	P30, p11	No Change
S ₂	P20, p01 neg1	P20, p01 neg1	No Change
S ₁	P10	P10	No Change
S ₀	P00, neg0	P00, neg0	No Change

From Table IV, it is inferred that the TP implementation in RCMB achieves a reduction in delay of about 5% to 22%, area ranges from 5% to 26% and the power reduction is from 8% to 34% in FPGA environment. This is more appreciable compared to 5% to 20% reduction in delay, 5% to 18% of the reduction in area and a power reduction of 8% to 32% in ASIC (Asirvatham R. and Ramachandran S., 2015) environment. It is due to the following reasons. (i) In Xilinx FPGAs, a CLB has been any divided into many slices. A slice in most of the Xilinx devices consists

of 2 LUTs and two flip-flops. There is additionally a special logic in the slice which changes the usually performed operations like combining two LUTs into a bigger LUT and making economical adders. (ii) To improve the performance of arithmetic operations, the special connections obtainable that permits LUT to operate as an economical full adder (Andreas Ehliar, 2009). This can be noted as a carry chain. It is additionally connected to adjacent slices to permit for larger adders to be created.

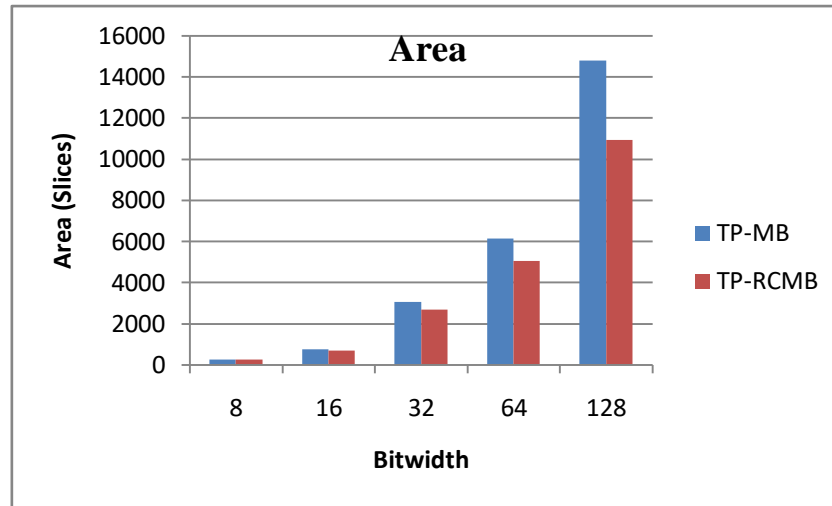
Table. 4 Comparison of TP-MB and TP-RCMB using Xilinx

	TP-MB					TP-RCMB				
Bitwidth	8	16	32	64	128	8	16	32	64	128
Mux	11	19	35	67	131	7	11	19	35	67
Area (Slices)	279	788	3080	6159	14785	265	717	2710	5050	10941
Delay (ns)	11.79	18.48	22.67	31.26	37	11.25	16.81	19.96	25.01	29.01
Power (mW)	67.34	88.32	101.44	110.80	150.11	61.95	72.65	84.30	89.81	99.2

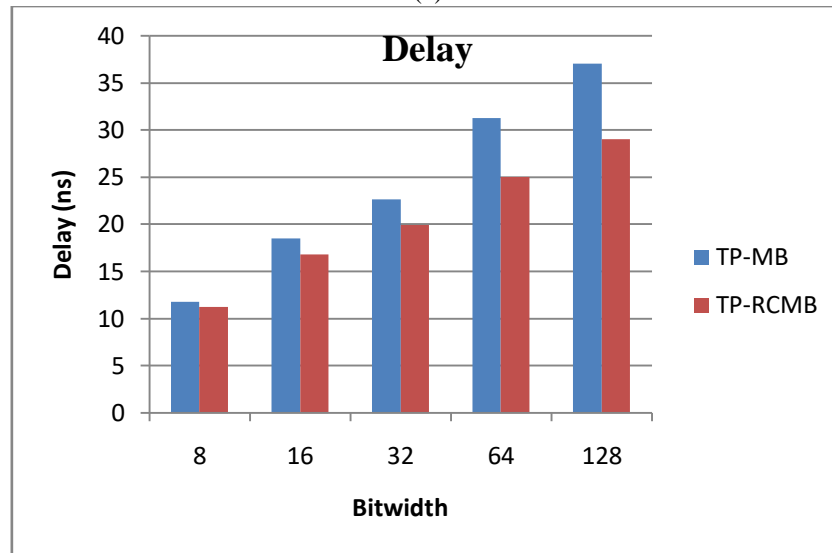


Fig. 4 is a typical representation of area, power and delay tabulated in Table III. It gives the performance evaluation of TP in MB by M. Sjalander and Per Larsson-Edefors, 2009

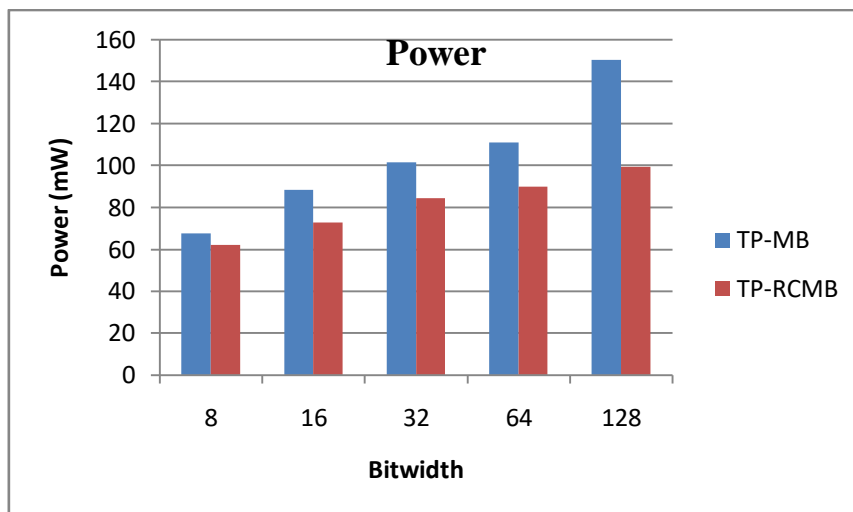
and TP implementation in RCMB. Illustration of area, delay and power for TP-MB and the proposed TP-RCMB in FPGA is depicted in Fig. 4 (a), (b) & (c).



(a)



(b)



(c)

Fig. 4 (a) Bitwidth Vs Area (b) Bitwidth Vs Delay (c) Bitwidth Vs Power

III. CONCLUSION

Double throughput is achieved effectively by implementing TP technique in RCMB in the FPGA environment. The proposed approach of implementation requires fewer changes in the PP array to acquire TP. As per the multiplication requirement, i.e. for an N or $N/2$ bit operation, MUXes do the selection of specific PPs in TP multiplier. The overall delay, area and power get reduced when the results are compared with TP-RCMB in an ASIC environment.

REFERENCES

1. Abdelgawad, A., and Bayoumi, M., "High Speed and Area-Efficient Multiply Accumulate (MAC) Unit for Digital Signal Processing Applications", IEEE International Symposium on Circuits and Systems, pp. 3199-3202, 2007.
2. About ASIC & FPGA. <http://www.altera.com>
3. Albert, D. and Dimitri, T., "Architecture and Implementation of a Vector /SIMD Multiply-Accumulate Unit", IEEE Trans. on Computers, Vol.54, No.3, pp.284-293, 2005.
4. Altera DE1 Board. <http://www.terasic.com.tw/cgi-bin/page/archive.pl?No=83>.
5. Amaricai, A., Vladutiu, M. and Boncalo, O., "Design Issues and Implementations for Floating-Point Divide-Add Fused", IEEE Trans. Circuits Syst. II-Exp. Briefs, Vol. 57, No. 4, pp. 295-299, 2010.
6. Amora, A.D., Nannarelli, A., Re,M. and Cardarilli, G.C., "Reducing Power Dissipation in Complex Digital Filters by using the Quadratic Residue Number System", Proc. of 34th Asilomar Conference on Signals, Systems and Computers, pp. 879-883, 2000.
7. Anitha,R., Alekhya, N., Jesima,L. W. and Bagyaveereswaran,V., "Comparative Study of High Performance Braun's Multiplier using FPGAs", IOSR Journal of Electronics and Communication Engineering, Vol. 1, No. 4, pp. 33-37, 2012.
8. Ardekani, J.F., "MxN Booth Encoded Multiplier Generator Using Optimized Wallace Trees", Proceedings IEEE International Conference on Computer Design: VLSI in Computers and Processors, ICCD '92, pp.1-4, 1992.
9. Ashour, M.A. and Saleh, H.I., "An FPGA implementation guide for some different types of Serial - Parallel Multiplier Structures", Microelectronics Journal, Vol.31, No.3, pp.161-168, 2000.
10. Asirvatham, R. and Ramachandran, S., "An Optimised Twin Precision Multiplier for ASIC Environment", EURASIP Journal on Advances in Signal Processing, pp. 1-18, 2015.
11. Bala, P.S. and Raghavendra, S., "A New VLSI Architecture of Parallel Multiplier - Accumulator Based on Radix-2 Modified Booth Algorithm", IEEE Trans. on Very Large Scale Integration (VLSI) Systems, Vol.18, No. 2, pp. 91-97, 2011.
12. Baugh, C. R. and Wooley, B. A., "A Two's Complement Parallel Array Multiplication Algorithm", IEEE Trans. Computers, Vol. 22, No. 12, pp. 1045-1047, 1973.
13. Bhardwaj, M., Min, R. and Chandrakasan, A.P., "Quantifying and Enhancing Power Awareness of VLSI Systems", IEEE Trans. on Very Large Scale Integration (VLSI) Systems, Vol. 9, No. 6, pp.757-772, 2001.
14. Booth, A.D., "A signed binary multiplication technique", The Quarterly Journal of Mechanics and Applied Mathematics Vol. 4, No. 2, pp. 236-240, 1950.
15. Brooks, D. and Martonosi, M., "Dynamically Exploiting Narrow Width Operands to Improve Processor Power and Performance", IEEE Proceedings Fifth International Symposium on High-Performance Computer Architecture, pp. 13 - 22, 1999.
16. Bruguera, J. D. and Lang, T., "Implementation of the FFT Butterfly with Redundant Arithmetic", IEEE Trans. Circuits Syst. II, Analog Digital Signal Process, Vol. 43, No. 10, pp. 717-723, 1996.