Shortest Route for Waste Transportation in Northern Bandung using Vehicle Routing Problem - Clarke and Wright - Saving Method

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Abstract: Bandung is one of big cities in Indonesia, and like the big city around the world, waste is become the problem to keep the city's clean, and particularly on waste problem is to transporting waste from transfer station (tempat pembuangan sampah – TPS) to intermediate facility (stasiun peralihan antara - SPA) then to a landfill/dump site (tempat pemrosesan akhir -TPA). There are 29 TPS's in Northern Bandung with a difference waste volume for each TPS. The waste will be loaded up and be transferred using stationary container system (SCS) to SPA daily. This paper is discussing waste transportation for 4 trucks of 6 m³ capacity for each from truck pool to many TPS's and to a single SPA to obtain the shortest route. Using modified VRP - Saving method resulting 11 routes with total travel distance is 466,88 km and total service time is 25.51 hours. Method of Nearest Neighbor is also being used to find the alternate shortest route which are also resulting 11 routes and found alternate shortest route with total travel distance is 450, 25 km and total service time is 24.60 hours.

Keywords: VRP; Saving; Clarke and Wright; Nearest Neighbor; Waste Transportation; Routes

I. INTRODUCTION

Bandung is a rapid growing city in Indonesia and as the big cities around the world, waste is a problem, especially collecting waste from TPS's and transporting them to a landfill. Bandung's government has issued a policy that the waste that has been collected from many transfer stations (tempat pembuangan sampah - TPS) will be transported to a site called intermediate facility (stasiun peralihan antara – SPA) then from SPA the waste will be transferred to a landfill (tempat pemrosesan akhir - TPA) that located far from the city. There are 4 service areas in Bandung which are Northern Bandung, Southern Bandung, Western Bandung, and eastern Bandung, and there are at least 29 TPS's on Northern Bandung only. The objective of this paper is to find a shortest route for transporting the waste in Northern Bandung service area from TPS's to a single SPA using VRP – Saving method, while waste transporting from SPA to TPA is not be discussed because there is only a single route from SPA to TPA, the trucks maintenance is also not to be discussed and government policy is to be assumed unchanged.

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II. LITERATURE REVIEW

There are many methods were used to design an effective route in transportation system, including waste transportation. Some methods using GIS [1,2,3], some using dynamic system [4,5], the using time series and statistic analysis [6], development from many algorithms 97,8], integer method [9]. The most common method been used is Vehicle Routing Problem. Son [10] using VRP with multiple research to design waste transportation system, while Bing [11] using VRP to collecting plastic waste. Some VRP was developed to optimize waste transportation system. Teixiera [12] was using periodic-VRP in waste recycle collecting system, and Ramos [13] was using multidepot VRP. Also, VRP was used to minimize gas emission [14].

Vehicle Routing Problem (VRP)

The Vehicle Routing Problem (VRP), introduced by Dantzig and Ramserl in 1959, holds a central position in distribution leadership and has become one of the most commonly researched issues in combinatorial optimization.

The Classical VRP can be officially described as follows. Let G (V, A) be a graph where $V = \{v0, vl, ..., vn\}$ is a vertex set, and $A = \{(vi, vj) : vi, vj \ V, i \neq j\}$ is an arc collection. Vertex v0 reflects a depot, while the remaining vertices correspond to clients. A cost matrix (cij) and a travel time matrix (tij) are connected with A. If these matrices are symmetrical, as is frequently the case, then describe the VRP on an undirected chart G = (V, E), where $E = \{(vi, vj) : vi, vj \ V, i < j\}$ is an edge set. Each client has a non-negative qi requirement and a ti. service time. The depot is based on a fleet of m identical capacity Q vehicles. The number of vehicles is either known in advance or handled as a decision variable. The VRP consists of creating a set of delivery or collection routes at most m such that (1) each route begins and ends at the depot, (2) every customer is visited exactly once by exactly one vehicle, (3) the total demand for every path does not exceed Q, (4) the complete duration of each route (including travel and service times) does not exceed a preset D limit, and (5) the total cost of routing is minimized. A popular version is where a time window [ai, bi] is imposed on each customer's visit. Many other extensions have also been studied; the vehicle fleet may be heterogeneous, vehicles may capture and deliver on the same path, some vehicles may not be able to visit certain locations, some clients may require multiple visits over a



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given period of time, there may be more than one depot, deliveries may be split between multiple vehicles [15].

Let there be n demand points in a specified region, each requiring a amount of weight Qi (i = 1, 2, ..., n) of products to be supplied to it (products are assumed to be indistinguishable but for their weight). The goods in question are stored at a depot, D, where a fleet of vehicles is also stationed. Vehicles have identical maximum weight capacities and limitations on maximum route time (or distance). At the depot, D, they all have to start and finish their routes. The issue is to get a set of delivery routes from the depot, D, to the different request points to minimize the complete distance covered by the entire fleet. It is assumed that the weights of Qi (i = i, ..., n) of the quantities required are less than the total weight capacity of the vehicles and we require that the entire quantity of Qi required at a given point be delivered by a single vehicle (i.e., we do not allow the possibility that one third, say, of Qi will be delivered by one vehicle and the remaining two thirds by another).

Thus, the VRP applies equally well to collecting solid waste from a specific set of points and delivering parcels to a set of points. For example, a significant current application has been in the routing of newspaper delivery vehicles distributing editions of a well-known newspaper to newsstands in an urban area. Either the maximum weight or the maximum route-time limitations can be relaxed in particular VRP apps. However, both generally play a part. For example, in the newspaper delivery issue just stated, one constraint, in relation to the maximum amount of newspapers a vehicle can carry, was that all deliveries to newsstands must be made within an hour of press time.

If no constraint applies, the VRP reduces to a traveling salesman problem: if the goal is simply to reduce total distance, it is a 1-TSP; if the number of vehicles to be used is specified, it is a *m*-TSP. It can therefore be seen that TSPs can be viewed as special cases of VRPs. As far as optimum solutions are concerned, it can be expected that VRP's will be more difficult than TSP's. Indeed, although several versions of VRP's have been formulated by various investigators as mathematical programming problems, less than 30 delivery points have been reportedly involved in the largest vehicle routing problems of any complexity that have been exactly solved.

In contrast, even with thousands of delivery points, the heuristic approaches we will describe next can be used.

Multi-depot vehicle routing problem with time windows (MDVRPTW) is used to determine the optimum set of fleet routes to meet the delivery requirements of a customer set in multiple depots at different locations under time window constraints. Extending MDVRPTW, a practical and difficult issue in logistics and supply chain management, to a research of service cars used to deliver and install electronics. MDVRPTW findings can be used to minimize fixed depots and vehicle delivery and installation costs as well as travel distance and labor costs. A heuristic and genetic algorithm were created to define a near-optimal solution along with a mixed integer programming model. Computational findings show that the suggested algorithms can be used effectively to fix comparatively big problems [17].

Due to the complexity of the problem, heuristics are usually used to solve waste collection problems with VRP efficiently. A capable clustering-based algorithm is to solve their waste collection vehicle routing issue with time windows considering a solution's path compactness and workload balancing. Generating an initial solution using a method that fully uses a vehicle and improves the initial solution using an interchange procedure. Urban waste collection problem is described as an arc routing problem. Applying a process of transforming the issue into a node routing one and solving it with heuristics of ant colony. A tabu search heuristics was used for the issue of truck and trailer routing and found that the tabu search acquired better alternatives compared to the other building heuristics used [11].

The classical problem of pickup and delivery (PDP) to an embedded routing and three-dimensional loading issue, called PDP with three-dimensional loading limitations (3L-PDP). Suppose you have provided a number of demands and a homogeneous fleet of Vehicles. A set of paths of minimum complete duration must be determined so that each application is transported from a loading site to the respective unloading site. Each request is given as a set of 3D rectangular items (boxes) in the 3L-PDP and the vehicle capacity is replaced by a 3D loading space. Investigation which limitations will guarantee that no reloading effort occurs, i.e. that no box is shifted after loading and before unloading. A spectrum of 3L-PDP varieties is implemented with different features in terms of reloading effort. A hybrid algorithm for solving the 3L-PDP consisting of a routing and packing procedure. A well-known big neighborhood search for the 1D-PDP is modified by the routing procedure. A tree search heuristic is accountable for packing boxes. Computational studies were conducted using 54 newly suggested 3L-PDP benchmark instances [18].

Heuristics for the Single-Depot VRP

Clarke and Wright's "savings" algorithm is by far the best-known strategy to the VRP issue. His fundamental concept is very easy. Consider depot D and n request points as shown in Figure 1a. Suppose the VRP solution initially consists of using n vehicles and dispatching one vehicle to each of the n request points.

Obviously, this solution's complete tour duration is, $2\sum_{i=1}^{n} d(D, i)$, so that

$$s(i,j) = 2d(D,i) + 2d(D,j)$$

If a single vehicle is used to serve two points, say i and j, on a single journey, the complete distance traveled is decreased by the quantity shown in Figure 1b,

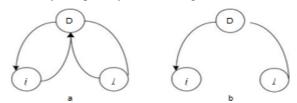


Fig. 1 Single Depot VRP



$$s(i,j) = 2d(D,i) + 2d(D,j) - [d(D,i) + d(i,j) + d(D,j)]$$

= $d(D,i) + d(D,j) - d(i,j)$ (1)

The quantity s(i, j) is known as the "savings" resulting from the combination of points i and j into a single tour. The bigger s(i, j) is, the more desirable it becomes to merge i and j in a single tour. However, I and j cannot be paired if the resulting trip violates one or more of the VRP's constraints [16].

This saving method can be modified in regards of waste transportation. Consider that a truck pool D, while i and j are two TPS's that the waste need to be transported to SPA S, as shown on Figure 2a.

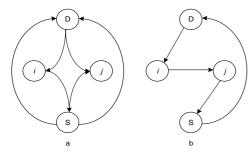


Fig. 2 Modified VRP - Saving Method

If a single vehicle is used to represent two TPS's, say I and j, on a single trip, the total distance traveled will be reduced by the amount shown in Figure 2b.

$$s(D,S) = [d(D,i) + d(i,S) + d(D,j) + d(j,S) + 2d(S,D)] - [d(D,i) + d(i,j) + d(j,S) + d(S,D)]$$

$$= d(i,S) + d(D,j) + d(S,D) - d(i,j)$$
(2)

The difference of this modified is after collecting waste on i, the truck will not travel back to the pool instead of travel to j to collect the waste and transporting the waste to SPA and after unload the waste in SPA, the vehicle will travel back to the truck pool.

III. METHOD

VRP – Clarke and Wright (Saving) and Nearest Neighbor

The modified VRP – Saving is used to solve the waste transportation problem, and the algorithm as follows,

Step 1: construct a distance matrix for pool to every TPS and from every TPS to SPA.

Step 2: calculate the saving based on the distance matrix using formula (2)

Step 3: determining a cluster based on Step 2,

Step 4: within the cluster, assign a truck to load the waste, subject to truck capacity. Truck capacity is $6~\text{m}^3$ with compact factor 12% so that the truck capacity become 7.2 m^3

Step 5: If the truck capacity has been reached, then the truck will travel to SPA, else repeat Step 4

Step 6: assign another truck to do Step 4 for another cluster and stop if all cluster have been served.

The cluster now has become a new shortest route.

To find an alternative shortest route, Nearest Neighbor method is being used, and the algorithm as follows

Step 1: based on cluster that has been created by Saving method, assign a truck to travel to the nearest TPS from the truck pool.

Step 2: loading the waste to the truck subject to truck capacity

Step 3: if the truck capacity has not been reached then assign the truck to travel to the second nearest TPS.

Step 4: if the truck capacity has been reached, assign the truck to travel to SPA, else repeat Step 3.

Step 5: assign another truck to do Step 1-4 for another cluster and stop if all cluster have been served.

The alternative shortest route has been found.

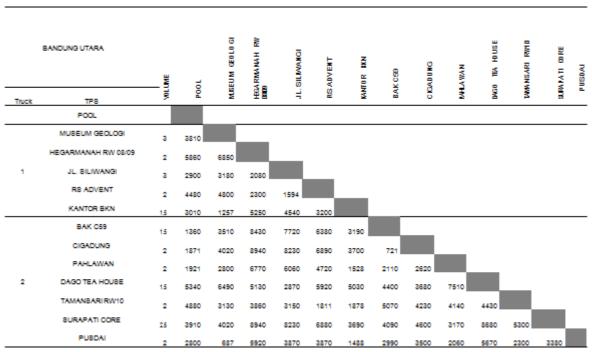
Comparing the Saving method result to Nearest Neighbor result, then the shortest route has been created

Data collection

A survey conducted on Northern Bandung region to collect the data regarding the distance from truck pool to every TPS, the distance among TPS, and the distance from every TPS to SPA, waste volume in every TPS, time to load the waste to the truck, as follows



Table. 1 Distance, Volume of Waste



This table is shown a quarter for the entire table, due to large table.

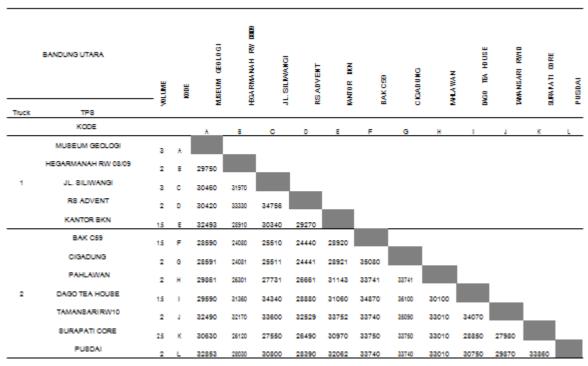
IV. RESULT

Saving Matrix

Based on distance matrix that has been constructed, the saving value can be obtained using formula 2, for example, obtaining saving value from pool (D) – TPS Bak Samami (BS) – TPS Dago Tea House (DTH) – SPA – pool, as follows, SDTH,BS = d(DTH,SPA) + d(SPA,D) + d(D,BS) - d(DTH,BS)

= 1680 + 16760 + 1113 - 3550 = 31183 By the same calculation, saving matrix as follows

Table. 2 Saving Matrix



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This table is shown a quarter for the entire table, due to large table.



Clustering

After saving matrix is formed, then cluster is determined by sorting the saving value from the biggest to the smallest.

Table. 3 Sorting Saving Value

No.	Saving	N. Saving	No.	Saving	N. Saving
1	Z-AB	48456	50 O-V 35327		35327
2	AA-AB	47307	51 M-V 353		35324
3	Z-AA	47306	52	S-V	35321
4	AB-AC	46369	53	U-V	35319
5	Z-AC	46366	54	B-N	35240
6	AA-AC	46285	55	G-J	35090
7	W-Z	45229	56	F-G	35080
8	W-AC	45226	57	A-M	35068
9	W-AA	45223	58	F-I	34870
10	W-AB	45220	59	C-Y	34770
11	B-AC	38690	60	C-N	34770
12	B-Z	38690	61	C-D	34756
13	B-W	38680	62	G-Q	34737
14	B-AA	38680	63	A-U	34674
15	B-AB	38680	64	M-X	34628
16	Y-Z	38500	65	U-X	34622
17	Y-AA	38500	66	G-Y	34450
18	Y-AC	38500	67	G-M	34440
19	Y-AB	38490	68	G-0	34440
20	N-Z	38120	69	G-S	34440
21	N-AC	38120	70	G-T	34440
22	N-W	38110	71	G-U	34440
23	N-AA	38110	72	G-V	34440
24	N-AB	38110	73	C-I	34340
25	C-Z	37880	74	T-X	34329
26	C-W	37870	75	O-X	34328
27	C-AA	37870	76	S-X	34323
28	C-AB	37870	77	A-S	34311
29	C-AC	37870	78	A-O	34310
30	G-W	37540	79	C-R	34130

This table is shown a quarter for the entire table, due to large table.

For instance, if the largest saving in at node i and j, then node i and j are grouped into the same cluster, then find the

second largest in terms of waste quantity until truck capability is achieved. This will be called as the first cluster.

The same algorithm is applied to obtain the next cluster, then the cluster as follows,



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Table. 4 Cluster

Cluster	TPS	Total	Route
1	PL-Z-AB-Y-Spa-PL	6.8	POOL - A.PERMAI - ELDORADO - LIPPI - SPA - POOL
2	PL-AA-AC-W-Spa-PL	7	POOL - LGI - P. SETIABUDHI - ABADI ASRI - SPA - POOL
3	PL-M-U-S-Spa-PL	6	POOL - GD. WANITA - TARBAK - POS GIRO - SPA - POOL
4	PL-O-T-X-Spa-PL	7	POOL - SAPARUA - RIUNGSARI - TOTAL BUAH - SPA - POOL
5	PL-G-I-J-F-Spa-PL	7	POOL - CIGADUNG - DAGO T.HOUSE - RW 10 TAMSAR - C59 - SPA - POOL POOL - SILIWANGI - ADVENT - RW16 LINGGAWASTU - SAPA -
6	PL-C-D-R-Spa-PL	6.5	POOL
7	PL-K-L-P-Spa-PL	7	POOL - SURAPATI - PUSDAI - PU BINAMARGA - SPA - POOL
8	PL-E-V-Q-Spa-PL	7	POOL - BKN - SARININGSIH - SAMAMI - SPA - POOL POOL - GEOLOGI - PAHLAWAN - RW 08/09 HEGARMANAH - SPA -
9	PL-A-H-B-Spa-PL	7	POOL
10	PL-Y-Spa-PL	7.2	POOL - LIPPI - SPA - POOL
11	PL-N-Spa-PL	6	POOL - KARANG SETRA - SPA - POOL

From 11 routes, the total travel distance is 466,88 km and total service time is 25.51 hours

V. DISCUSSION

The inherent nature of municipal solid waste collection is related to the growth of efficient vehicle routing (VR) models that optimize complete vehicle travel distances, environmental emissions and investment charges. VR is a planned method that enables vehicles to load waste at collection locations (a.k.a. sites) and dump it at a landfill with a single or multiple goal. Waste generation and collection cannot be evaluated in detail, allowing further assessment of disposal practices, modifications and trends so that MSW collection modeling is of specific significance.

Several VR models were described in the literature with multiple goals such as minimum fuel consumption, minimum travel distances and environmental emissions [11]. VRP – Clarke and Wright (saving) method works by clustering the nodes and routes are formed, these routes can be modified by finding alternative shortest route which is possible to obtain a shortest route. In this paper alternative shortest route is calculated using Nearest Neighbor method. Comparing to saving method, routes that are formed by Nearest Neighbor has the shortest total distance (km) and fastest travel time (hours), as follows

Table. 6 Comparison of Clarke and Wright method and Nearest Neighbor method within clusters

Cluster	Route (Saving)	Distance (km)
1	POOL - A.PERMAI - ELDORADO - LIPPI - SPA - POOL	57.3
2	POOL - LGI - P. SETIABUDHI - ABADI ASRI - SPA - POOL	47.61
3	POOL - GD. WANITA - TARBAK - POS GIRO - SPA - POOL	38.28
4	POOL - SAPARUA - RIUNGSARI - TOTAL BUAH - SPA - POOL POOL - CIGADUNG - DAGO T.HOUSE - RW 10 TAMSAR - C59 - SPA	37.05 A
5	- POOL POOL - SILIWANGI - ADVENT - RW16 LINGGAWASTU - SAPA -	48.98
6	POOL	35.95
7	POOL - SURAPATI - PUSDAI - PU BINAMARGA - SPA - POOL	40.09
8	POOL - BKN - SARININGSIH - SAMAMI - SPA - POOL POOL - GEOLOGI - PAHLAWAN - RW 08/09 HEGARMANAH - SPA	41.48
9	- POOL	44.53
10	POOL - LIPPI - SPA - POOL	40.05
11	POOL - KARANG SETRA - SPA - POOL	35.56
	Total Distance (km)	466.88
	Total Travel Time (hours)	25.51

Cluster	Route (Nearest Neighbor)	Distance (km)
1	POOL-LIPPI-ELDORADO-ALAM PERMAI-SPA-POOL	50.5
2	POOL-ABADI ASRI-P.SETIABUDHI-LGI-SPA-POOL	47.61
3	POOL-POS GIRO-TARUNA BAKTI-GD. WANITA-SPA-POOL	38.28
4	POOL-TOTAL BUAH-RIUNGSARI-SAPARUA-SPA-POOL POOL-C59-CIGADUNG-DAGO T.HOUSE-RW10 TAMSAR-SPA-	37.5
5	POOL	43.81
6	POOL-SILIWANGI-ADVENT-RW16 L.WASTU-SPA-POOL	35.95
7	POOL-PU BINAMARGA-PUSDAI-SURAPATI-SPA-POOL	40.49
8	POOL-SAMAMI-BKN-SARININGSIH-SPA-POOL	37.78
9	POOL-PAHLAWAN-GEOLOGI-RW08/09 H.MANAH-SPA-POOL	42.72
10	POOL-LIPPI-SPA-POOL	40.05
11	POOL-KARANG SETRA-SPA-POOL	35.56
	Total Distance (km	450.25
	Total Travel Time (hours	24.6

As the routes have been formed, there are 11 routes to be served by 6 m³ truck, then the schedule of all trucks can be built as follows,

Table 7. Truck Schedule

	Route to be served on day number						
Truck No	1	2		34	5		6
1	Route 1	Route 2	Route 3	Route 1	Route 2	Route 3	
2	Route 4	Route 5	Route 6	Route 4	Route 5	Route 6	
3	Route 7	Route 8	Route 9	Route 7	Route 8	Route 9	
4	Route 10	Route 11		Route 10	Route 11		

From Table 7, it can be seen that there are routes to be served two times in a week, so that all routes have been scheduled.

The operational cost for trucks and operators can be calculated as,

Fixed Cost = Driver Cost + Assistant Cost, one driver and 4 assistants for every truck, Variable Cost = Fuel Cost (Diesel) x Distance

Table 8. Operational Cost

Route	Operational Cost (Rp)
1	494,807
2	488,844
3	469,634
4	468,019
5	481,020
6	464,816
7	474,178
8	468,602
9	478,774
10	473,270
11	464,023

Table 8 resulting average of operational cost is Rp. 470,590

VI. CONCLUSION

This paper obtaining the result using modified VRP – Clarke and Wright which is never been used, and the conclusions are as follows,

1. There are 11 clusters/routes to serve 29 TPSs regarding waste transportation from every TPS to SPA in Northern Bandung with total travel distance is 450,25 km and total service time is 24.60 hours.

- 2. There are 4 trucks to serve all the clusters 2 times a week
- 3. The average operational cost is Rp. 470,590.

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