

Fusion of Multi Modal Lumber Spine Scans Using Wavelet and Convolutional Neural Network

Bhakti Palkar, Dharendra Mishra

Abstract: Multiple medical images of different modalities are fused together to generate a new more informative image thereby reducing the treatment planning time of medical practitioners. In recent years, wavelets and deep learning methods have been widely used in various image processing applications. In this study, we present convolutional neural network and wavelet based fusion of MR and CT images of lumber spine to generate a single image which comprises all the important features of MR and CT images. Both CT and MR images are first decomposed into detail and approximate coefficients using wavelets. Then the corresponding detail and approximate coefficients are fused using convolutional neural network framework. Inverse wavelet transform is then used to generate fused image. The experimental results indicate that the proposed approach achieves good performance as compared to conventional methods.

Index Terms: Medical image fusion, Multi-modal image fusion, Wavelets, Deep Learning, Convolutional Neural Network.

I. INTRODUCTION

Spine is one of the most essential parts of human body. Because of spine we can bend and move freely. It is divided into different parts: cervical, thoracic, lumber and sacroiliac and coccyx. Many people today suffer from lower back pain. This pain is associated with lumber region of spine. The number of patients worldwide with lower back disease has increased by 54% from 1990 to 2015 [1]. Because of this, there has been tremendous increase in number of imaging scans of different modalities. Each modality offers its own advantages and disadvantages. Computed Tomography (CT) scan is used to view bony structures like vertebrae of spine. Magnetic resonance (MR) scan is used to view details related to soft tissues. In most of the cases doctors suggest both CT and MR scans to check the structure and shape of lumbar spine. Then based on the scans they decide further treatment on the spine.

In recent times many researchers have come up with different algorithms to fuse multi modal medical images. Fusion algorithms basically fall into three categories: – pixel level fusion, feature level and decision level fusion. In pixel level fusion, original pixels intensities of the source images are fused. In feature level fusion, different objects are fused based on their extracted features. Decision level fusion uses results of multiples algorithms followed by a decision rule to fuse the results. The decision rule could be a statistical method or voting based method or simply a fuzzy logic based

method. Among all the three types, pixel level fusion methods are simple, efficient and they preserve the information content in original images more accurately. Existing pixel level image fusion methods can be divided into three major types: 1) spatial domain techniques, 2) multi-scale decomposition based techniques, 3) sparse representation based techniques

Spatial domain techniques which work on the original pixel intensities of images suffer from low contrast or colour distortion [2]. The most commonly used multi-scale decomposition based techniques are divided into two types: 1) pyramid based fusion and 2) wavelet transform based fusion. Since the input images are different from each other in various aspects such as content, size, shape and noise, these factors greatly affect the performance of pyramid based fusion methods [2]. For brain diagnosis morphological pyramid filtering method has been used [3]. Discrete Cosine Transform can be used in conjunction with Laplacian pyramid to fuse CT and MR images of human brain [7]. It removes the ‘patchy effect’ drawback of pyramid based fusion.

Discrete Wavelet Transform (DWT) based fusion techniques have been used to fuse multi-modal medical images [4]. DWT

based fusion methods give directional information which is not provided by spatial domain and pyramid based fusion methods. Fused images generated by DWT don’t show patchy effect and they have good signal to noise ratio. On the other hand DWT also has some disadvantages like shift variance and lack of phase information which is turn results into inconsistent reconstruction of original image. Dual Tree Complex Wavelet Transform (DT-CWT) which is a variant of DWT offers shift invariance and phase information. It has been used successfully for medical image fusion [5]. Stationary wavelet transform (SWT) is another modified DWT where the ‘shift-invariance’ drawback is removed by completely eliminating the down sampling and up sampling in DWT [6]. Lifting wavelet transform (LWT), a variant of DWT, reduces computation time and memory requirement greatly. LWT has been used to fuse multi modal images of brain [8]. However, all these variants of DWT cannot extract curves and edges of images clearly. Sparse representation based image fusion methods, have been used to fuse multi-modal medical images [9]. With the rapid development in the field of image processing, many people have used deep features of multi-modal images as saliency features to generate fused image. Convolutional sparse representation (CSR) [10] and convolutional neural network (CNN) [11] [12] based methods are used to fuse multi focus and multi-modal images. However, these methods use

Revised Manuscript Received on July 05, 2019.

Bhakti Palkar, Department of Computer Engineering, MPSTME, NMIMS, Mumbai, India.

Dharendra Mishra, Department of Computer Engineering, MPSTME, NMIMS, Mumbai, India.

the results obtained by last layer and all the important information obtained by middle layers is not considered in deciding final fusion. It is also yet not clear how much deep a network should go. If the network is very deep, it may end up losing all important information.

In this paper, a hybrid method based on wavelet and deep learning is used to fuse CT and MR images of lumber spine. The source images are decomposed into detail content and approximate coefficients by using wavelet. Then VGG-19 deep learning network is used to fuse corresponding parts of the two images. The final fused image is generated by the applying inverse wavelet transform. We have used dataset1 of SpineWeb [16] which has CT and MR scans of lumber spine. This paper is organized as follows: Section two focuses on discrete wavelet transform. Section three is for VGG-19 network. Section four talks about the proposed fusion method. Section five shows results and experiments. Conclusion is presented in section six.

II. DISCRETE WAVELET TRANSFORM

Using wavelet transform any waveform or signal in time domain can be converted into a series of coefficients based on small finite waves called wavelets.

A. 1D Discrete Wavelet Transform

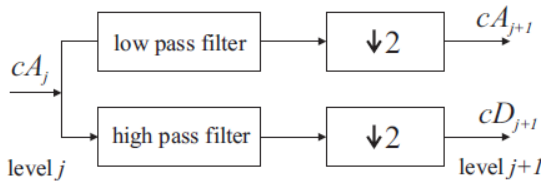


Figure 2: 1D-Discrete Wavelet Transform

Given a signal s of length N , the Discrete Wavelet Transform (DWT) can be computed in at most $\log_2 N$ stages. Original 1D signal (let this be cA_j) is convolved with low pass filter followed by down sampling by 2 to generate approximate coefficients cA_{j+1} . It is also convolved with high pass filter followed by down sampling by 2 to generate detail coefficients cD_{j+1} as shown in Fig.1. This process can be applied recursively on approximation coefficients generated in previous level to generate approximation and detail coefficients at next levels.

B. 2D Discrete Wavelet Transform

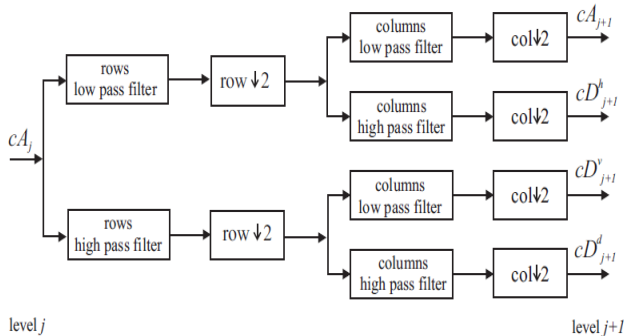


Figure 2: 2D-Discrete Wavelet Transform

2D-DWT is being used efficiently for image processing and computer vision applications. Steps for 2D-DFT are as follows:

Step 1: Apply 1D-DWT on rows to generate approximation coefficients and detail coefficients.

Step 2: Apply 1D-DWT on columns of approximation coefficients obtained in step 1. This generates approximation coefficients cA_{j+1} (LL) and detail coefficients with horizontal orientation cD_{j+1}^h (LH).

Step 3: Apply 1D-DWT on columns of detail coefficients obtained in step 1. This generates detail coefficients with vertical orientation cD_{j+1}^v (LV) and detail coefficients with diagonal orientation cD_{j+1}^d (LD) as shown in Fig. 2.

This completes only one level of decomposition which extracts only highest frequencies. To extract lower frequencies this process can be applied repeatedly on LL band generated in previous level. Like 1D inverse wavelet transform, 2D inverse wave transform is obtained by applying the decomposition step in reverse.

III. VISUAL GEOMETRY GROUP (VGG)-19

Size:	Image
224×224	Conv1_1, Depth-64 Conv1_2, Depth-64
	Max-Pool
112×112	Conv2_1, Depth-128 Conv2_2, Depth-128
	Max-Pool
56×56	Conv3_1, Depth-256 Conv3_2, Depth-256 Conv3_3, Depth-256 Conv3_4, Depth-256
	Max-Pool
28×28	Conv4_1, Depth-512 Conv4_2, Depth-512 Conv4_3, Depth-512 Conv4_4, Depth-512
	Max-Pool
14×14	Conv5_1, Depth-512 Conv5_2, Depth-512 Conv5_3, Depth-512 Conv5_4, Depth-512
	Max-Pool
7×7	FC-4098 FC-4098 FC-4098

Figure 3: VGG-19 Network

The VGG-19 is 19 layer deep convolutional neural network that is trained on more than a million images from the ImageNet database [13][14]. It can classify images into 1000 object categories. As a result, the network has learned rich feature representations for a wide range of images. Two important characteristics of VGG-19 are 'simple' and 'deep'. The VGG-19 has fairly straightforward architecture. The network has an image input size of 224×224. The image is passed through a stack of convolutional layers, where 3 × 3 filters are used. All convolutional layers are equipped with the rectification (ReLU) non-linearity. Spatial pooling is carried out after five convolutional layers by max-pooling layers over a 2×2 pixel window, with stride 2. The stack of convolutional layers is followed by three Fully-Connected (FC) layers: the first two have 4096 channels each, the third performs 1000 classifications and thus

contains 1000 channels (one for each class).

IV. PROPOSED FUSION METHOD

This section discusses how to fuse CT and MR images of lumbar spine using wavelets and VGG-19 convolutional neural network. We have used wavelets to decompose MR and CT scans into approximation and detail coefficients separately. Then VGG-19 network based fusion method is used to fuse corresponding coefficients of the two input images. Finally inverse wavelet transform is used to obtain fused image.

A. Fusion Algorithm

Fig. 4 demonstrates the overall fusion method. It is summarized as below:

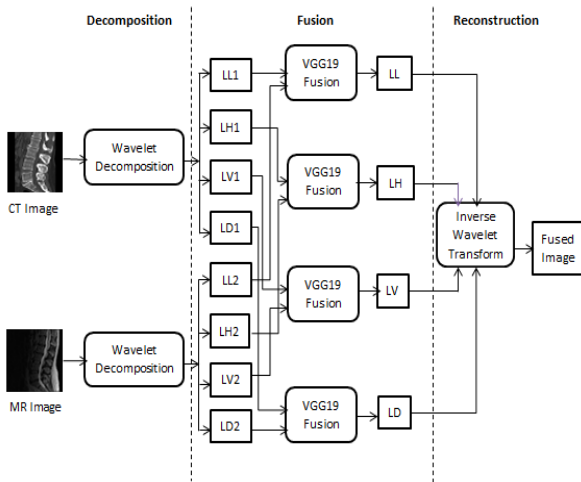


Figure 4: Medical image fusion using wavelets and VGG-19 network

Step1: Apply wavelet decomposition on CT image to generate approximate coefficient LL1 and three detail coefficients: LH1(horizontal), LV1 (vertical), LD1(diagonal)
Step2: Apply wavelet decomposition on MR image to generate approximate coefficient LL2 and three detail coefficients: LH2(horizontal), LV2 (vertical), LD2(diagonal)
Step3: Apply fusion based on VGG-19 network on four pairs: (LL1 and LL2), (LH1 and LH2), (LV1 and LV2) and (LD1 and LD2), to generate LL band, LH band, LV band and LD band.
Step4: Apply inverse wavelet transform on the four bands generated in step 3 to obtain fused image.

B. VGG-19 Fusion

We have used VGG-19 convolutional neural network to extract deep features. This section

describes the fusion strategy designed using pre-trained VGG-19 model. The algorithm for VGG-19 fusion is as follows:

Input: Source images I_k where $k=\{1,2\}$.

Output: Fused coefficients

Steps:

1. For each image I_k , generate $\phi_k^{i,m}$ feature maps where 'i' is layer number and 'm' is the channel number of the i^{th} layer where $k=\{1,2\}$ and $i=\{1,2,3,4\}$, $m \in \{1,2, \dots, M\}$, $M = 64 \times 2^{i-1}$.

2. Calculate initial activity level map C_k^i L1-norm as shown in equation 1:

$$C_k^i = \|\phi_k^{i,1:M}(x, y)\|_1 \quad (1)$$

Calculate final activity level map \hat{C}_k^i using block based average operator as shown in equation 2:

$$\hat{C}_k^i(x, y) = \frac{\sum_{\beta=-r}^r \sum_{\theta=-r}^r C_k^i(x+\beta, y+\theta)}{(2r+1)^2} \quad (2)$$

where r is 1.

Calculate initial weight map W_k^i using soft-max operator as shown in equation 3:

$$W_k^i(x, y) = \frac{\hat{C}_k^i(x, y)}{\sum_{n=1}^K \hat{C}_n^i(x, y)} \quad (3)$$

5. Calculate modified weight map \bar{W}_k^i as shown in equation 4. by applying up-sampling operator to resize the weight map to that of the size of input image.

$$\bar{W}_k^i(x + p, y + q) = W_k^i(x, y), \quad (4)$$

$$p, q \in \{0, 1, \dots, (2^{i-1} - 1)\}$$

This generates four pairs of weight maps \bar{W}_k^i , $k \in \{1, 2\}$ and $i \in \{1, 2, 3, 4\}$

6. For each pair \bar{W}_k^i , calculate the initial fused coefficients using equation 5.

$$F^i(x, y) = \sum_{n=1}^K W_n^i(x, y) \times I_n(x, y), \quad k = 2 \quad (5)$$

7. Obtain final fused content using max operator

$$F(x, y) = \max[F^i(x, y) | i \in \{1, 2, 3, 4\}] \quad (6)$$

Once the fused coefficients are obtained for four pairs (one pair of approximation coefficients and three pairs of detail confidents) we use inverse wavelet transform on the four coefficients to obtain fused image.

V. RESULTS AND DISCUSSIONS

The aim of this section is to validate and compare the proposed method with conventional methods using quantitative and qualitative criteria.

A. Dataset

In our experiment the proposed fusion method is applied on T2 weighted MR images and CT images of ten patients suffering from various lumbar spine diseases. The MR and CT scans are taken from publically available dataset1 of SpineWeb [16]. All pairs of CT and MR images have been registered with each other using landmark based registration technique in MATLAB.

B. Fusion

T2 weighted MR and registered CT images of ten patients are used for experimentation. Fused images obtained using VGG-Fusion methods are compared with DWT [4], SWT [5], DT-CWT [6] and DCT-LP [7]. We have presented results in visual form for one case and in tabular form for ten cases.

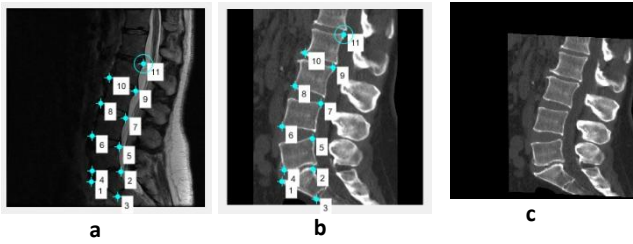


Figure 4: Case 1 Registration process
a) Fixed Image(MR)-landmark points selection
b) Moving Image(CT)- landmark points selection
c) Registered CT

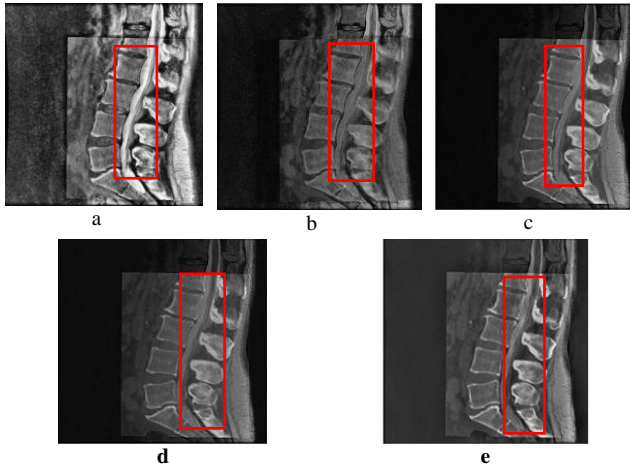


Figure 5: Case 1- Fusion Results
a) VGG-Fusion b) SWT
c) DCT-LP d) DWT
e) DT-CWT

Fig. 4 shows original MR (a) and CT (b) images of case 1. User selects 11 matching control points from the two images, and then the geometrical transformations are inferred to register CT with MR image. Figure 'c' is the registered CT image. Once the registered CT image is obtained, fusion is performed on original MR(a) and registered CT (c) images. Fig. 5 shows the fused images obtained using different methods for case 1.

C. Quantitative assessment of fused images

Tables 1, 2, 3 and 4 show the quantitative assessment of fused images using four quality parameters: entropy, standard deviation, spatial frequency [2] and universal quality index[15] respectively. Entropy (E) indicates the amount of information contained in the image. The higher value of entropy implies that the fused image has more information than any of the input images. Standard Deviation (SD) measures the contrast in the fused image. So it should be high. Image with high spatial frequency (SF) offers better quality. Universal image quality index (UQI) models any distortion in the image using three different factors: loss of correlation, luminance distortion and contrast distortion. The higher the UQI value better is the quality of the image. Colour codes are used to indicate the algorithm that has showed best value of the quality parameter. Table cells with dark red background shows the best value as opposed to light background which shows worst value.

As we can observe in table I that VGG-fusion method showed highest (best) value for 8 out of 10 patients. DT-CWT is another method which could show entropy values near to VGG-Fusion entropy values. SWT and DCT-LP fusion methods do not show good entropy values. DWT method is worst as it has shown lowest entropy values

for 9 out 10 cases which mean that DWT fused images do not carry much information. DT-CWT and VGG-Fused images are more informative than SWT and DCT-LP fused images.

Table -I: Quantitative Assessment-Entropy

Case	VGG-Fusion	SWT	DT-CWT	DCT-LP	DWT
1	7.8219	7.0563	7.3104	7.1009	7.0092
2	7.8225	7.7465	7.7801	7.7638	7.7436
3	7.6481	7.6188	7.6343	7.6439	7.6030
4	7.4500	7.2499	7.6075	7.2842	7.2244
5	7.6107	7.5319	7.8304	7.5496	7.5418
6	7.4312	7.0763	7.3688	7.0913	7.0741
7	7.7159	7.5529	7.4140	7.5725	7.5341
8	7.8027	7.2755	7.4366	7.2855	7.2870
9	7.8540	7.5770	7.7843	7.5991	7.5526
10	7.7437	7.3090	7.5206	7.3388	7.2759

Table II shows standard deviation values which should be high to indicate good contrast. DT-CWT has shown highest SD values for 9 out of 10 cases. VGG-Fusion method has shown SD values very near to DT-CWT values. DWT could show highest SD values for any of the cases which indicate that the fused images obtained using DWT are of low contrast. Contrast of DT-CWT and VGG-Fused images is better than SWT and DCT-LP.

Table -II: Quantitative Assessment-Standard Deviation

Case	VGG-Fused	SWT	DT-CWT	DCT-LP	DWT
1	62.8561	43.6251	56.4697	44.0244	42.9024
2	60.1074	56.6511	71.5696	57.1373	56.5296
3	57.0075	54.5636	70.6445	54.9777	54.2845
4	49.1442	43.2058	54.9181	43.7830	41.9642
5	48.8266	45.9384	64.5806	46.4274	46.2874
6	46.9885	36.0115	47.0770	36.2756	35.5292
7	71.2319	58.8815	72.4750	59.1172	59.0526
8	60.6287	42.3452	54.1153	42.3834	42.5562
9	59.2885	47.5669	62.0904	48.2776	46.8118
10	59.5328	50.4212	62.0333	50.5876	50.0371

Table III shows spatial frequency (SF) values which indicate quality of the fused image. Again we can observe that the quality of VGG-Fused images is remarkably better than the fused images obtained using other three methods. DWT has always shown least values of spatial frequency for all ten cases.

Table -IIIIV: Quantitative Assessment-Spatial Frequency

Case	VGG-Fused	SWT	DT-CWT	DCT-LP	DWT
1	10.5606	7.8878	8.5463	8.8059	3.9119
2	13.6450	9.4554	9.8815	10.2033	6.7283
3	11.5609	9.0088	8.9245	9.7461	5.7287
4	9.8641	8.9289	7.5440	9.7604	4.7077
5	12.3010	9.5563	9.8970	10.3995	6.0516
6	7.5253	6.0957	5.6927	6.5617	3.3869
7	11.6245	6.0287	7.6433	6.6340	4.8485
8	9.7115	2.9435	4.8602	3.0977	2.8693
9	14.3514	11.1519	10.8626	12.3099	6.4893
10	9.9550	5.2405	5.8770	5.5487	3.5586

Table IV shows values of universal image quality index which is based on contrast, luminance and correlation. According to this parameter quality of DT-CWT fused images do not possess good

quality. VGG-fused images show best quality fused images for 8 out of 10 cases.

Table -IVV: Quantitative Assessment-Universal Quality Index

Case	VGG-Fused	SWT	DT-CWT	DCT-LP	DWT
1	0.6900	0.5955	0.5523	0.5976	0.6388
2	0.7404	0.7152	0.6575	0.7152	0.6979
3	0.8045	0.7329	0.6959	0.7589	0.7585
4	0.7965	0.7823	0.7360	0.7822	0.7728
5	0.7865	0.7631	0.7173	0.7632	0.7569
6	0.8152	0.7988	0.7598	0.8010	0.7933
7	0.6610	0.5981	0.5385	0.6004	0.5964
8	0.6782	0.7505	0.7172	0.7685	0.7420
9	0.7600	0.7795	0.7468	0.7794	0.7725
10	0.6671	0.6533	0.6245	0.6538	0.6425

The MR and CT input images are completely different from each other because they show different details of human body. All four quality parameters: entropy, standard deviation, spatial frequency and universal image quality index help us in making the decision that fused image generated using VGG-Fusion method is of good quality. It integrates important features from both input images, shows good amount of information content and good contrast.

D. Qualitative analysis by orthopedic surgeon

Qualitative analysis is done by getting the source images and fused image verified and tested by renowned orthopedic surgeon. He has observed that all the images cover lumbar spine diseases such as degenerative disc disease, spinal stenosis, disc herniation, spondylolisthesis and bone Spurs (Osteophytes). Case wise details of the disease are as follows:

- 1) Case 1: Prolapse Disk, Disk thinning, Bulging Disk
- 2) Case2: Spondylolisthesis, Degenerative disk and osteophyte
- 3) Case3: Spinal stenosis, disk thinning, herniation, osteophyte formation
- 4) Case 4: Spondylolisthesis
- 5) Case 5: Disk Herniation
- 6) Case 6: Degenerative disk, Osteophyte
- 7) Case 7: Spinal stenosis, Disk Herniation
- 8) Case 8: Disk thinning, Disk Herniation
- 9) Case 9: Disk thinning, Disk Herniation
- 10) Case 10: Disk thinning, Disk Herniation

To assess quality of fused images, the orthopedic surgeon has used four parameters namely: bone visibility, soft tissue visibility, contrast and quality. Table no.5 shows the parameters used by the surgeon to assess quality of fused images. All the fused images show both bony and soft tissues which are otherwise visible only in one input image either CT or MR image. Fused images generated using VGG-Fusion are of very good quality and contrast as compared to other four methods. So, fused image which is generated using VGG-Fusion can be used for further treatment planning.

Table 5: Parameters for Qualitative Assessment

Parameters				
Methods	Bone Visibility	Soft Tissue visibility	Contrast	Quality
VGG-Fusion	√	√	Very Good	Very High
SWT	√	√	Good	Medium
DT-CWT	√	√	Good	Low
DCT-LP	√	√	Good	Medium

DWT	√	√	Low	Low
-----	---	---	-----	-----

VI. CONCLUSION

In this paper, we present a very simple yet effective hybrid fusion method using wavelet and VGG-19 deep learning framework for MR and CT images of lumbar spine. The source images –MR and registered CT are decomposed into approximation (LL) and detail (LH, LV, LD) coefficients separately using wavelets. Fusion based on VGG-19 is performed separately on the four pairs of coefficients (LL1, LL2), (LH1, LH2), (LV1, LV2) and (LD1, LD2). Finally, the fused image is reconstructed by applying inverse wavelet transform on the four coefficients generated by deep learning framework. We use both quantitative and qualitative methods to evaluate the proposed method. As per quantitative evaluation, fused images generated using DT-CWT and VGG-Fused are better than SWT, DWT and DCT-LP in terms of content and contrast. But the quality of VGG-Fusion method is remarkably better than other fused images. So, fused image which is generated using VGG-Fusion can be used for further treatment planning. The same approach can be tested on fusion of other human organs as well as other multiple modalities. VGG-Fusion can also be combined with other variants of wavelet transforms.

REFERENCES

1. Hartvigsen J. et al., "Low Back Pain Series: What Low Back Pain Is and Why We Need to Pay Attention.", Lancet, June 2018; Volume 391, Issue 10137; p2356-2367.
2. Dhirendra Mishra and Bhakti Palkar, "Image Fusion Techniques: A Review", International Journal of Computer Applications 130(9):7-13, November 2015. Published by Foundation of Computer Science (FCS), NY, USA.
3. K. Mikoajczyk, J. Owczarczyk, W. Recko, "A test-bed for computer-assisted fusion of multi-modality medical images", in: Computer Analysis of Images and Patterns, Springer, 1993, pp. 664-668.
4. Yong Yang, Dong Sun Park, and Shuying Huang, Nini Rao, "Medical Image Fusion via an Effective Wavelet Based Approach", published in EURASIP Journal on Advances in signal processing, Volume 2010, February 2010, Article No:44, Hindawi Publishing corp., New York, united states.
5. Tao J., Li S., Yang B. (2010) Multimodal Image Fusion Algorithm Using Dual-Tree Complex Wavelet Transform and Particle Swarm Optimization. In: Huang DS., McGinnity M., Heutte L., Zhang XP. (eds) Advanced Intelligent Computing Theories and Applications. ICIC 2010. Communications in Computer and Information Science, vol 93. Springer, Berlin, Heidelberg
6. R.Asokan1 , T.C.Kalaiselvi2 and M.Tamilarasi3 , "Medical Image Fusion Using Stationary Wavelet Transform With Different Wavelet Families", Pak. J. Biotechnol. Vol. 13 (special issue on Innovations in information Embedded and Communication Systems) Pp. 10 - 14 (2016)
7. Akanksha Sahu, Vikrant Bhateja, Abhinav Krishn, Himanshi, "Medical Image Fusion with Laplacian Pyramids", 2014 International Conference on Medical Imaging, m-Health and Emerging Communication Systems (MedCom) 2014.
8. Himanshi, Vikrant Bhateja, Abhinav Krishn and Akanksha Sahu, "Medical Image Fusion in Curvelet Domain Employing PCA and Maximum Selection Rule", Proceedings of the Second International Conference on Computer and Communication Technologies, Advances in Intelligent Systems and Computing 379, DOI 10.1007/978-81-322-2517-1_1, Springer, India 2016
9. S. Li, H. Yin, and L. Fang, "Group-sparse representation with dictionary learning for medical image denoising and fusion," IEEE Transactions on Biomedical Engineering, vol. 59, pp. 3450–3459, 2012.

10. Liu Y, Chen X, Ward R K, et al. Image fusion with convolutional sparse representation. IEEE signal processing letters, 2016, 23(12): 1882-1886.
11. Liu Y, Chen X, Peng H, et al. Multi-focus image fusion with a deep convolutional neural network. Information Fusion, 2017, 36: 191-207.
12. Hui Li, Xiao-Jun Wu, Josef Kittler, "Infrared and Visible Image Fusion using a Deep Learning Framework", International Conference on Pattern Recognition 2018
13. ImageNet. <http://www.image-net.org>
14. Simonyan, Karen, and Andrew Zisserman. "Very deep convolutional networks for large-scale image recognition.", arXiv preprint arXiv:1409.1556 (2014).
15. Zhou Wang, Alan C. Bovik, "A Universal Image Quality Index", IEEE Signal Processing Letters, vol. 9, no. 3, pp. 81-84, March 2002
16. Spineweb dataset <http://spineweb.digitalimaginggroup.ca/>

AUTHORS PROFILE



Mrs. Bhakti Palkar has received B.E (Computer science and engineering) in 2001, M.E (Computer) from Mumbai University in 2008. She has more than 16 years of experience in teaching. Currently working as associate professor in Department of Computer Engineering at K.J. Somaiya College of engineering, Mumbai. Her areas of interest are Image processing,, Database management systems, Compiler construction.



Dr. Dhirendra Mishra has received his BE (Computer Engg) degree from University of Mumbai. He completed his M.E. (Computer Engg) from Thadomal Shahani Engg. College, Mumbai, University of Mumbai. He received PhD from NMIMS university. He currently works as Professor in Computer Engineering department of Mukesh Patel School of Technology Management and Engineering, SVKM's NMIMS University, Mumbai, INDIA. His areas of interests are Image Processing, Operating systems, Information Storage and Management.