

Effect of Heat Source/Sink on Free Convective MHD Flow past an Exponentially Accelerated Infinite Plate with Mass Diffusion and Chemical Reaction

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Abstract: The effects of heat source/sink and chemical reaction with mass diffusion on free convective incompressible viscous fluid flow past an accelerated vertical plate with magnetic field has been investigated. Laplace transformation method has been applied to solve the system of linear partial differential equations. The result is presented in form of complementary error function and exponential function. The effect of non dimensional parameters such as Schmidt number (Sc), Accelerated parameter (a), Chemical reaction parameter (K), Prandtl number (Pr), Magnetic field parameter (M), Mass Grashof number (Gm), Heat source/sink parameter (H), Thermal Grashof number (Gr) on temperature, concentration, velocity has been discussed with graphs.

Index Terms: Free-convection, Mass transfer, MHD, Heat Source/Sink, Chemical Reaction.

I. INTRODUCTION

The study of free convective flows under different boundary conditions has caught the attention of various researchers and scientists now a days because of its large number of applications in the various fields like science, environment, engineering and technology etc. This study is also important for many industrial and manufacturing processes like designing of apparatus for nuclear power plant, various devices of propulsion for space vehicles, gas turbines, satellites, missiles and aircrafts etc. Chemical reaction effect combined with heat and mass transfer is important in chemical industries. The magnetic field effect on natural convective flows is useful in ionized gases and liquid metals. The study of collective heat and mass transfer effect has applications in fluid boiling and condensing at a solid surface, flow of air in a desert cooler, drying etc. The study of fluid flows with radiations is important for many

industrial and environment processes.

Many researchers have made a contribution to find the exact solution of free convective flow problems with special boundary conditions using various methods. Stokes [1] made the first contribution by solving the flow problem related to the viscous incompressible fluid. The study of chemical reaction and thermal radiation effects can be seen in the work of researchers like Raptis and Massalas [2], Muthucumaraswamy and Ganesan [3].

The researchers such as Soundalgekar et al. [5], Singh and Kumar [6], Muthucumaraswamy and Visalakshi [7] etc. have made contribution in solving flow problems related to the heat and mass transfer effect of free convective flow with different conditions as constant mass flux, with uniform mass diffusion, exponentially accelerated vertical plate, the effect of heat sources, with transverse magnetic field, with vertical stretching surface etc.

Hossain et al. [8], Hady et al. [9], Garg et al. [10] etc have studied the heat generation/absorption effect with different flow conditions.

The present investigation aims to study the combined effect of heat source/sink, mass diffusion and chemical reaction on free convective unsteady fluid flow.

II. MATHEMATICAL ANALYSIS

We are considering viscous incompressible fluid flow past an exponentially accelerated vertical plate. The x' -axis is chosen along the plate in vertically up direction and y' -axis is chosen perpendicular to it. At time $t' \leq 0$, the fluid and plate are kept at equal temperature in fixed condition. At time $t' > 0$, the plate is exponentially accelerated with velocity $u = u_0 e^{at'}$. The temperature and concentration of plate is slightly increased to T_w' and C_w' . The flow field is governed by the following set of equations:

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$$\frac{\partial u'}{\partial t'} = \beta(T' - T_{\infty}') - \frac{\sigma B_0^2 u'}{\rho} + \nu \frac{\partial^2 u'}{\partial y'^2} + \beta^* (C' - C_{\infty}') \quad (1)$$

$$\rho c_p \frac{\partial T'}{\partial t'} = k \frac{\partial^2 T'}{\partial y'^2} + Q^* (T' - T_{\infty}') \quad (2)$$

$$\frac{\partial C'}{\partial t'} = D \frac{\partial^2 C'}{\partial y'^2} + K_1 (C' - C_{\infty}') \quad (3)$$

The boundary conditions are

$$\left. \begin{aligned} u' = 0, T' = T_{\infty}', C' = C_{\infty}' \quad \forall y', t' \leq 0 \\ u' = u_0 e^{at'} \\ T' = T_{\infty}' + (T'_w - T_{\infty}') At' \\ C' = C_{\infty}' + (C'_w - C_{\infty}') At' \end{aligned} \right\} \text{at } y' = 0, t' > 0$$

$$u' \rightarrow 0, T' \rightarrow T_{\infty}', C' \rightarrow C_{\infty}' \text{ as } y' \rightarrow \infty, t' > 0 \quad (4)$$

Where $A = u_0^2/2$

Here u' is velocity in x' direction, t' is time, T' is fluid temperature, T'_w is the plate temperature, C' is species concentration, T_{∞}' is fluid temperature away from plate, β is acceleration due to gravity, C'_w is the species concentration near wall, C_{∞}' is species concentration far away from plate, β is the coefficient of volume expansion, β^* is the thermal expansion coefficient with concentration, σ is electrical conductivity of the fluid, ν is the kinematic viscosity, ρ is the density, B_0 is electromagnetic induction, c_p is specific heat at constant pressure, k is thermal conductivity, K_1 is reaction rate constant, Q^* is heat source/sink and D is chemical molecular diffusivity.

Introducing following non-dimensional quantities:

$$u = \frac{u'}{u_0}, \quad y = \frac{y'}{\nu} u_0, \quad t = \frac{t' u_0^2}{\nu}, \quad a = \frac{a' \nu}{u_0^2}$$

$$\theta = \frac{(T' - T_{\infty}')}{(T'_w - T_{\infty}')}, \quad C = \frac{(C' - C_{\infty}')}{(C'_w - C_{\infty}')}$$

$$G_r = \frac{\nu g \beta (T'_w - T_{\infty}')}{u_0^3}, \quad G_m = \frac{\nu g \beta^* (C'_w - C_{\infty}')}{u_0^3}$$

$$M = \frac{\sigma B_0^2 \nu}{\rho u_0^2}, \quad P_r = \frac{\nu \rho c_p}{k}, \quad S_c = \frac{\nu}{D}, \quad K = \frac{\nu K_1}{u_0^2}, \quad H = \frac{Q^* \nu^2}{k u_0^2} \quad (5)$$

Where a , H , M , θ , S_c , P_r , G_r , G_m , and K are Accelerated parameter, Heat source/sink parameter, Magnetic field parameter, dimensionless temperature, Schmidt number, Prandtl number, Thermal Grashof number, Mass Grashof number and Chemical reaction parameter respectively.

Then in view of (5), equations (1), (2) and (3) reduce to

$$\frac{\partial u}{\partial t} = \frac{\partial^2 u}{\partial y^2} + G_r \theta + G_m C - Mu \quad (6)$$

$$P_r \frac{\partial \theta}{\partial t} = \frac{\partial^2 \theta}{\partial y^2} - H \theta \quad (7)$$

$$S_c \frac{\partial C}{\partial t} = \frac{\partial^2 C}{\partial y^2} - KC \quad (8)$$

The corresponding boundary conditions becomes

$$u(y, t) = 0, \theta(y, t) = 0, C(y, t) = 0 \quad \forall y \text{ and } t \leq 0$$

$$u(y, t) = e^{at}, \theta(y, t) = t, C(y, t) = t$$

for $y = 0$ and $t > 0$

$$u(y, t) \rightarrow 0, \theta(y, t) \rightarrow 0, C(y, t) \rightarrow 0 \text{ as } y \rightarrow \infty \text{ and } t > 0 \quad (9)$$

The system of equations (6)-(8), under the boundary conditions (9) represents the proposed flow problem.

III. SOLUTION OF THE PROBLEM

We have used Laplace Transformation method to find the solution of the equations of flow (6)-(8), under the boundary conditions (9). The solution of given problem for temperature, concentration and velocity are given by

$$\theta(y, t) = C_2 \exp(\alpha_5) \operatorname{erfc}(\beta_5) + C_4 \exp(-\alpha_5) \operatorname{erfc}(\beta_{10}) \quad (10)$$

$$C(y, t) = C_5 \exp(\alpha_7) \operatorname{erfc}(\beta_{13}) + C_6 \exp(-\alpha_7) \operatorname{erfc}(\beta_{14}) \quad (11)$$

$$u(y, t) = \frac{1}{2} \exp(\gamma_1) [\exp(\alpha_1) \operatorname{erfc}(\beta_1) + \exp(-\alpha_1) \operatorname{erfc}(\beta_2)] - (U_1 + U_2) [\exp(\alpha_2) \operatorname{erfc}(\beta_2) + \exp(-\alpha_2) \operatorname{erfc}(\beta_4)] - (U_3 + U_4) [C_1 \exp(\alpha_2) \operatorname{erfc}(\beta_2) + C_2 \exp(-\alpha_2) \operatorname{erfc}(\beta_4)] + U_1 \exp(\gamma_2) [\exp(\alpha_2) \operatorname{erfc}(\beta_5) + \exp(-\alpha_2) \operatorname{erfc}(\beta_6)] + U_2 \exp(\gamma_2) [\exp(\alpha_4) \operatorname{erfc}(\beta_7) + \exp(-\alpha_4) \operatorname{erfc}(\beta_8)] + U_1 [\exp(\alpha_5) \operatorname{erfc}(\beta_9) + \exp(-\alpha_5) \operatorname{erfc}(\beta_{10})] + U_3 [C_3 \exp(\alpha_5) \operatorname{erfc}(\beta_9) + C_4 \exp(-\alpha_5) \operatorname{erfc}(\beta_{10})] - U_1 \exp(\gamma_2) [\exp(\alpha_6) \operatorname{erfc}(\beta_{11}) + \exp(-\alpha_6) \operatorname{erfc}(\beta_{12})] + U_4 [C_5 \exp(\alpha_7) \operatorname{erfc}(\beta_{13}) + C_6 \exp(-\alpha_7) \operatorname{erfc}(\beta_{14})] + U_2 [\exp(\alpha_7) \operatorname{erfc}(\beta_{13}) + \exp(-\alpha_7) \operatorname{erfc}(\beta_{14})] - U_2 [\exp(\alpha_9) \operatorname{erfc}(\beta_{15}) + \exp(-\alpha_9) \operatorname{erfc}(\beta_{16})] \quad (12)$$

IV. NUSSELT NUMBER

Nusselt number is given by

$$N_u = - \left(\frac{\partial \theta(y, t)}{\partial t} \right)_{y=0}$$

$$= (t\sqrt{H} + \frac{P_r}{2\sqrt{H}}) \operatorname{erf} \sqrt{\frac{H}{P_r}} t + \sqrt{\frac{t P_r}{\pi}} \exp \left(-\frac{H}{P_r} t \right) \quad (13)$$

V. SHERWOOD NUMBER

Sherwood number is given by

$$S_h = - \left(\frac{\partial C(y, t)}{\partial t} \right)_{y=0}$$

$$= \frac{1}{2} \sqrt{\frac{S_c}{K}} \operatorname{erf} \sqrt{Kt} + t \sqrt{K S_c} \operatorname{erf} \sqrt{Kt} + \sqrt{\frac{t S_c}{\pi}} \exp(-kt) \quad (14)$$

VI. SKIN-FRICTION

Skin-Friction is given by

$$\tau = - \left(\frac{\partial u(y, t)}{\partial t} \right)_{y=0}$$

$$\begin{aligned}
 &= \exp(at) \sqrt{M+a} \operatorname{erf} \sqrt{(M+a)t} + [1 - \\
 &(U_3 + U_4)t] \sqrt{\frac{1}{\pi t}} \exp(-Mt) + \\
 &U_3 \left[\sqrt{\frac{tP_r}{\pi}} \exp\left(-\frac{H}{P_r}t\right) + \left(t\sqrt{H} + \frac{P_r}{2\sqrt{H}}\right) \operatorname{erf} \sqrt{\frac{H}{P_r}t} - \right. \\
 &\left. \left(\frac{1}{2\sqrt{M}} + t\sqrt{M}\right) \operatorname{erf} \sqrt{Mt} \right] + U_4 \left[\frac{1}{2} \sqrt{\frac{S_c}{K}} \operatorname{erf} \sqrt{Kt} + \right. \\
 &t\sqrt{KS_c} \operatorname{erf} \sqrt{Kt} + \sqrt{\frac{tS_c}{\pi}} \exp(-kt) - \left(\frac{1}{2\sqrt{M}} + \right. \\
 &t\sqrt{M}\left.) \operatorname{erf} \sqrt{Mt} \right] + \\
 &2U_1 \left[\exp(lt) \sqrt{M+l} \operatorname{erf} \sqrt{(M+l)t} + \sqrt{H} \operatorname{erf} \sqrt{\frac{H}{P_r}t} - \right. \\
 &\left. \exp(lt) \sqrt{H+lP_r} \operatorname{erf} \sqrt{(H+lP_r)t} - \sqrt{M} \operatorname{erf} \sqrt{Mt} \right] + \\
 &2U_2 \left[\exp(mt) \sqrt{M+m} \operatorname{erf} \sqrt{(M+m)t} + \right. \\
 &\left. \sqrt{KS_c} \operatorname{erf} \sqrt{Kt} - \sqrt{(K+m)S_c} \operatorname{erf} \sqrt{(K+m)t} + \right. \\
 &\left. \sqrt{KS_c} \operatorname{erf} \sqrt{Kt} - \sqrt{\frac{S_c}{\pi t}} \exp(-(k+m)t) - \sqrt{M} \operatorname{erf} \sqrt{Mt} \right]
 \end{aligned}
 \tag{15}$$

VII. RESULTS AND DISCUSSIONS

To identify with the physical properties of the problem, algebraic calculations are carried out to demonstrate the effect of various parameters upon the characteristics of flow. The algebraic values of temperature, concentration, velocity are calculated at flow parameters like Prandtl number (Pr), Accelerated parameter (a), Chemical reaction parameter (K), Thermal Grashof number (Gr), Schmidt number (Sc), Mass Grashof number (Gm), Heat source/sink parameter (H), Magnetic field parameter (M) and Time (t). These results are shown graphically by Figs. (1) – (11).

Effects of H, Pr and t on temperature profile are shown in Fig.1. Here different values of H are chosen 2, 4 and 6 to show the effect of it on temperature. The value of Pr=0.71 and t=0.2 are taken as constant. It is observed that higher values of H decrease the fluid temperature. The cause of t on temperature is shown by taking values of t as 0.2, 0.4 and 0.6 with fixed values of H = 2 and Pr = 0.71. The graph depicts that temperature rises with time.

Different values of Pr are taken as 0.21, 0.71 and 7 with fixed values of H = 2 and t = 0.2. From the graph, it is observed that temperature reduces when Prandtl number increases. It is also noticed that temperature for air is high as compared to temperature for water .

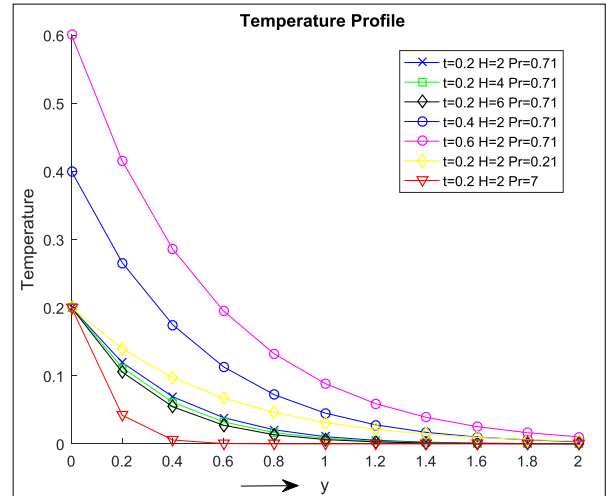


Fig.1 Temperature profile for values of H, t and Pr
Fig. 2 illustrates the concentration profile at t, K and Sc. The values of K are taken as 3, 5 and 7 keeping t=0.2 and Sc=2.01 as constants. The

effect of Schmidt number is presented by taking values as 2.01, 3 and 4 keeping t=0.2 and K=3 fixed. The graph of concentration shows that concentration of plate decreases slightly with higher value of Chemical reaction parameter and Schmidt number. Effect of t is shown by taking values of t as 0.1, 0.2 0.3 and 0.4 keeping K = 3 and Sc = 2.01 fixed. The graph of concentration shows that concentration of plate increases when time is increased.

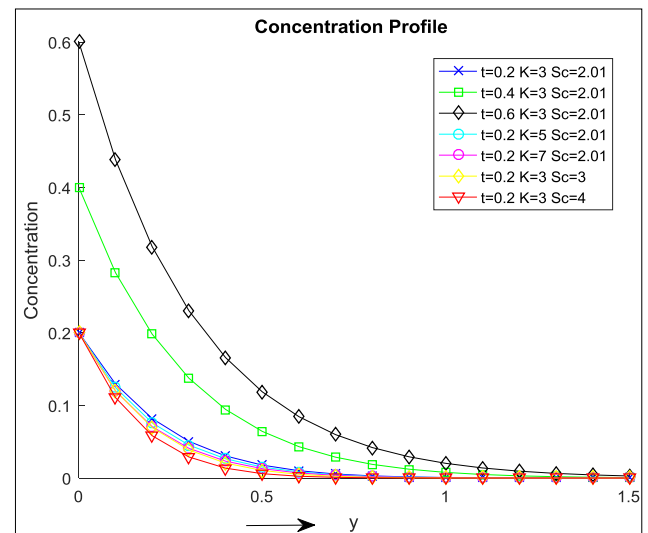


Fig.2 Concentration profile for different values of t, K and Sc

EFFECT OF HEAT SOURCE/SINK ON OF MHD FREE CONVECTIVE FLOW PAST AN EXPONENTIALLY ACCELERATED INFINITE VERTICAL PLATE WITH MASS DIFFUSION AND CHEMICAL REACTION

Effects of various parameters on velocity profile are shown by Figs. (3) - (6). Fig. 3 shows the effect H and a on velocity Profile. The different values of a are chosen as 0.2, 0.4, 0.6 and 0.8. Other parameters ($t=0.2, H=2, Sc=0.60, K=3, Gr=5, M=0.5, Gm=5, Pr=0.71$) are kept constant. The different values of H are chosen as 2, 4, 6 and 8. Other parameters ($a=0.2, t=0.2, Sc=0.60, K=3, Gr=5, M=0.5, Gm=5, Pr=0.71$) are kept constant. The graph depicts that increasing value of accelerated parameter accelerate the fluid flow and increasing values of H retards the fluid flow.

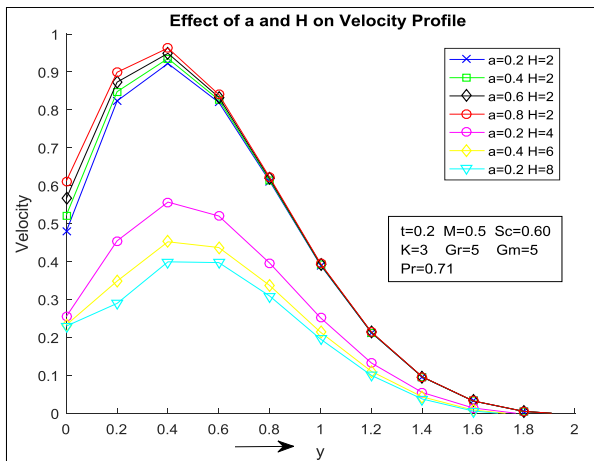


Fig.3 Velocity profile for different values of H and a

The effect of Pr and Sc are shown graphically by Fig. 4. The different values of Pr are chosen as 0.16, 0.21 and 0.71. Other parameters ($t=0.2, a=0.2, H=4, M=0.5, Sc=0.60, K=5, Gr=5, Gm=5$) are kept constant. The values of Sc are chosen as 0.60 (for Water), 0.75 (for Oxygen) and 0.78 (for Ammonia). Other parameters ($t=0.2, a=0.2, H=4, M=0.5, K=5, Gr=5, Gm=5, Pr=0.71$) are kept constant. It is noticed motion of fluid slow down with increasing values of Pr or Sc . It means thermal diffusion and mass diffusion accelerate the fluid flow.

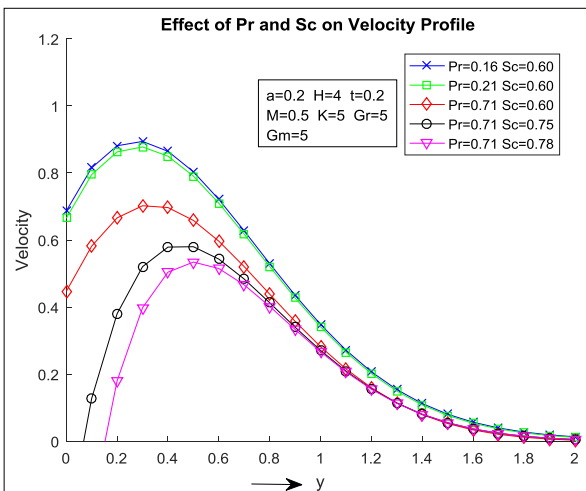


Fig.4 Velocity profile for different values Pr and Sc

Fig. 5 shows the effect M and K on velocity Profile. The different values of M are chosen as 0.5, 0.7 and 1 keeping other parameters ($a=0.2, t=0.2, H=4, Sc=0.60, K=5, Gr=5, Gm=5, Pr=0.71$) as constant. It is observed that motion of fluid slow down with increasing values of M . It means induced magnetic field retards the fluid flow. The different values of K are chosen as 5, 7 and 9. Other parameters ($a=0.2, t=0.2, H=4, Sc=0.60, Gr=5, M=0.5, Gm=5, Pr=0.71$) are kept constant. The graph depicts that increasing values of K results in decreasing value of velocity. It means chemical reaction rate slow down the fluid flow.

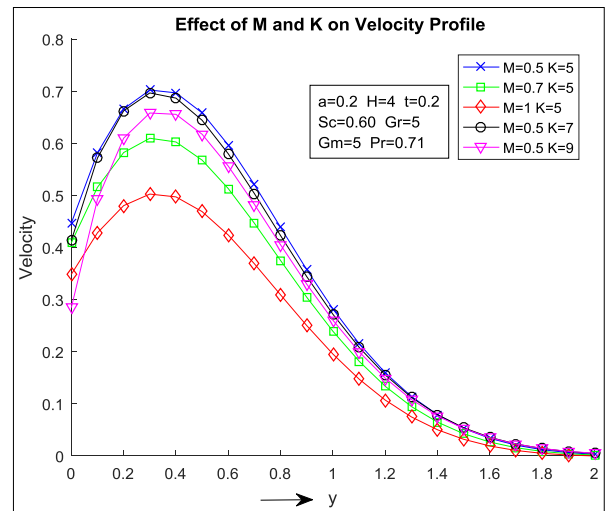


Fig.5 Velocity profile at various values of M and K

Fig. 6 represents the velocity variations at values of Gr and Gm . The values of Gr are chosen as 5, 10 and 15. Other parameters ($a=0.2, t=0.2, H=4, M=0.5, Sc=0.60, K=5, Gm=5, Pr=0.71$) are kept constant. It is observed that increasing values of Gr increases the fluid flow. The different values of Gm are chosen as 5, 10 and 15. Other parameters ($a=0.2, t=0.2, H=4, M=0.5, Sc=0.60, K=5, Gr=5, Pr=0.71$) are kept constant. It is noticed that velocity decreases by increasing values of Gr but after some distance it starts arising.

The effect of t, H and Pr on Nusselt number is depicted by Fig. 7. The graph indicates that heat transfer rate is higher by increasing values of t, H and Pr .

The effect of t, K and Sc on Sherwood number is by Fig. 8. The graph clearly shows that mass transfer rate is higher by increasing values of t, K and Sc .

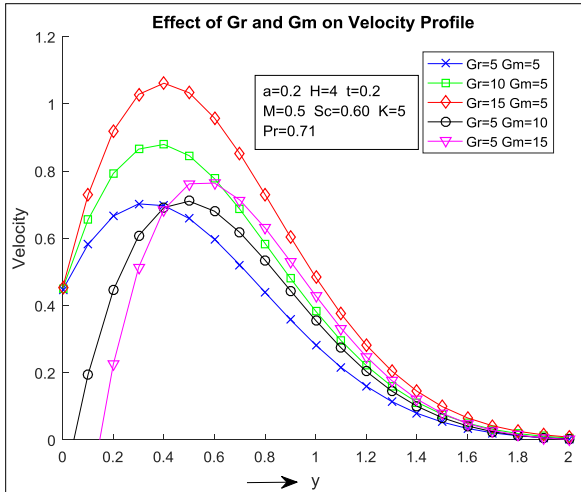


Fig.6 Velocity profile for different values Gr and Gm

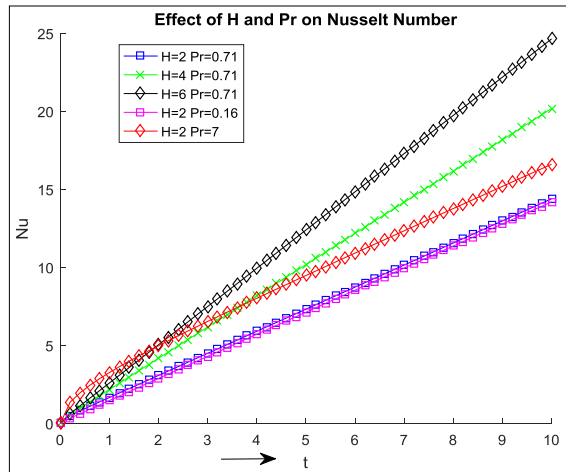


Fig.7 Effect of H and Pr on Nusselt Number

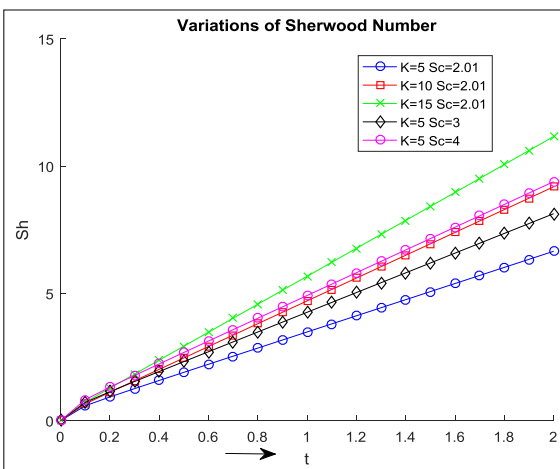


Fig.8 Effect of K and Sc on Sherwood Number

Skin-Friction variations at different parameters are shown by Figs. (9) – (11).

Fig. 9 represents graphically the effect of M, a and Sc on Skin-Friction. The graph clearly depicts that accelerated parameter and magnetic field parameter increases the shear stress whereas mass diffusion has a reverse effect on it.

Fig. 10 represents graphically the effect of K and Pr on Skin-Friction. It is depicted that shear stress decreases with increase in K but it increases slightly Pr.

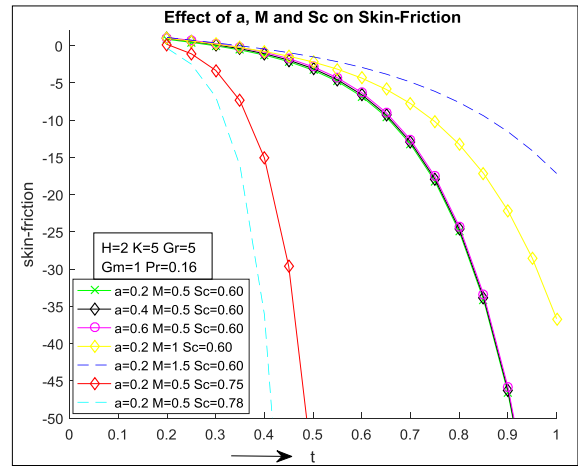


Fig.9 Effect of M, a and Sc on Skin-Friction

The effect of H, Gr and Gm on Skin-Friction is represented in Fig. 11. It is evident from the graph that heat absorption parameter tend to increase the shear stress whereas thermal buoyancy forces and mass buoyancy forces have opposite effect on it.

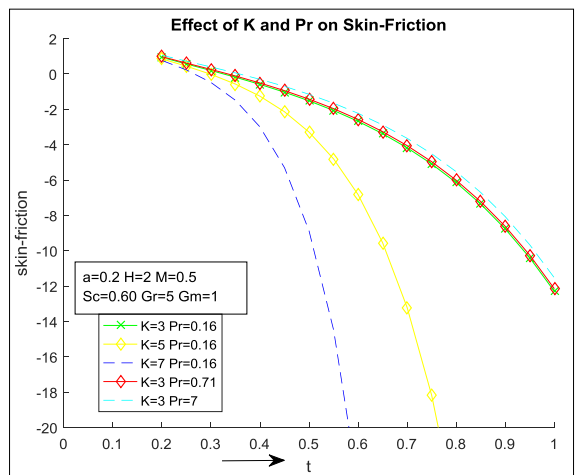


Fig.10 Effect of K and Pr on Skin Friction

EFFECT OF HEAT SOURCE/SINK ON OF MHD FREE CONVECTIVE FLOW PAST AN EXPONENTIALLY ACCELERATED INFINITE VERTICAL PLATE WITH MASS DIFFUSION AND CHEMICAL REACTION

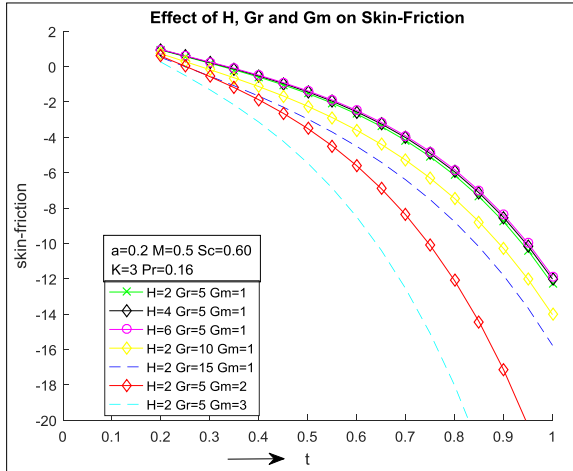


Fig.11 Effect of H, Gr and Gm on Skin Friction

VIII. CONCLUSIONS

The Present study can be concluded as:

-Heat absorption parameter and thermal diffusion reduces the fluid temperature while progression in time arises the temperature of the fluid.

-Progression in time increases the species concentration whereas Chemical reaction and mass diffusivity has reverse effect on it.

-Accelerated parameter and mass buoyancy forces accelerate the fluid motion whereas chemical reaction, thermal buoyancy forces, heat absorption parameter, magnetic field, , viscosity and mass diffusivity tends to retard the fluid motion.

-The heat transfer rate is increased with progression in time, thermal diffusion and heat absorption parameter.

-Rate of mass transfer increases with time, chemical reaction, and mass diffusivity.

-Shear stress increases with increment in accelerated parameter, thermal diffusion, heat absorption parameter and magnetic field parameter whereas heat time, mass diffusivity, chemical reaction parameter, thermal buoyancy forces and mass buoyancy forces decrease it.

APPENDIX

$$l = \frac{M-H}{Pr-1} \quad m = \frac{M-KSc}{Sc-1} \quad n = \frac{Gr}{Pr-1} \quad p = \frac{Gm}{Sc-1}$$

$$U_1 = \frac{n}{2l^2} \quad U_2 = \frac{p}{2m^2} \quad U_3 = \frac{n}{l} \quad U_4 = \frac{p}{m}$$

$$\gamma_1 = at \quad \gamma_2 = lt \quad \gamma_3 = mt$$

$$\alpha_1 = y\sqrt{M+a} \quad \alpha_2 = y\sqrt{M} \quad \alpha_3 = y\sqrt{M+l}$$

$$\alpha_4 = y\sqrt{M+m}$$

$$\alpha_5 = y\sqrt{H} \quad \alpha_6 = y\sqrt{H+lPr} \quad \alpha_7 = y\sqrt{KSc}$$

$$\alpha_8 = y\sqrt{(K+m)Sc}$$

$$C_1 = \frac{t}{2} + \frac{y}{4\sqrt{M}} \quad C_2 = \frac{t}{2} - \frac{y}{4\sqrt{M}} \quad C_3 = \frac{t}{2} + \frac{yPr}{4\sqrt{H}}$$

$$C_4 = \frac{t}{2} - \frac{yPr}{4\sqrt{H}} \quad C_5 = \frac{t}{2} + \frac{y\sqrt{Sc}}{4\sqrt{K}} \quad C_6 = \frac{t}{2} - \frac{y\sqrt{Sc}}{4\sqrt{K}}$$

$$\beta_1 = \frac{y}{2\sqrt{t}} + \sqrt{(M+a)t} \quad \beta_2 = \frac{y}{2\sqrt{t}} - \sqrt{(M+a)t}$$

$$\beta_3 = \frac{y}{2\sqrt{t}} + \sqrt{Mt} \quad \beta_4 = \frac{y}{2\sqrt{t}} - \sqrt{Mt}$$

$$\beta_5 = \frac{y}{2\sqrt{t}} + \sqrt{(M+l)t} \quad \beta_6 = \frac{y}{2\sqrt{t}} - \sqrt{(M+l)t}$$

$$\beta_7 = \frac{y}{2\sqrt{t}} + \sqrt{(M+m)t} \quad \beta_8 = \frac{y}{2\sqrt{t}} - \sqrt{(M+m)t}$$

$$\beta_9 = \frac{y}{2\sqrt{t}}\sqrt{Pr} + \sqrt{\frac{H}{Pr}t} \quad \beta_{10} = \frac{y}{2\sqrt{t}}\sqrt{Pr} - \sqrt{\frac{H}{Pr}t}$$

$$\beta_{11} = \frac{y}{2\sqrt{t}}\sqrt{Pr} + \sqrt{\left(\frac{H}{Pr}+1\right)t} \quad \beta_{12} = \frac{y}{2\sqrt{t}}\sqrt{Pr} - \sqrt{\left(\frac{H}{Pr}+1\right)t}$$

$$\beta_{13} = \frac{y}{2\sqrt{t}}\sqrt{Sc} + \sqrt{Kt} \quad \beta_{14} = \frac{y}{2\sqrt{t}}\sqrt{Sc} - \sqrt{Kt}$$

$$\beta_{15} = \frac{y}{2\sqrt{t}}\sqrt{Sc} + \sqrt{(K+m)t}$$

$$\beta_{16} = \frac{y}{2\sqrt{t}}\sqrt{Sc} - \sqrt{(K+m)t}$$

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