

Improved Pilot Selection for Channel Estimation of Polar Codes in Wireless 5G



B Pujitha, K Aruna Kumari

Abstract: Fading channels learning about polar codes is great prominence. Knowledge of polar codes is very important while they are applied to the wireless communication systems. In fading Channels the communication through channel estimation which is an essential step for communication. The structure is constructed by a set of information bits for both systematic polar code and non-systematic polar code and the information set recognized frozen bits. In fading channels uneven pilot selection scheme and even pilot selection scheme are two pilot selection schemes are considered for polar codes. There is an improvement in decoding performance of polar codes using these selection schemes. In this choosing of coded symbols treated as pilots is a replacement of insertion of pilots. Polar codes have poor performance in fixed domain. So the EPS selection scheme can be active for tracing or channel estimation. The structure of polar code encoding is capable structure and pilot selection is grave since whole selections cannot use the existing structure again. By conjoining the above advantages, pilot signals are selected without any addition from outside and insertion of pilot symbols impartial to estimation of the channel. Leveraging this, the DM-BS scheme is applied to multiple input multiple output (MIMO) system in frequency selective fading channel.

I. INTRODUCTION

Basically all channel coding technology works in same way. There are some errors occur in communication links due to random noise device impairments, interference etc. The original data stream is correct at receiving side. So two sets of operations are employed on original data stream in channel coding. Polar codes being used in 5G wireless standard due to provide great error correcting performance with low decoding complexity. When combined with more advanced decoding algorithms. This makes outstanding performance. Frequency Division Multiplexing (FDM) technique is built in this OFDM. Different information streams are plotted in FDM onto discrete frequency channels which are in parallel. Every FDM channel is divided from the others to reduce the interference contiguous channels.

With the increased future smart transportation systems, rapid mobility takes place with variable Doppler shifts with time based phenomena in wireless communication. Peak data rate problems are encountered.

Revised Manuscript Received on December 30, 2019.

* Correspondence Author

B Pujitha*, Department of Electronics and Communication Engineering, P V P Siddhartha Institute of Technology, Vijayawada, India.

K Aruna Kumari, Department of Electronics and Communication Engineering, P V P Siddhartha Institute of Technology, Vijayawada, India.

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So we need efficient encoding and decoding schemes to increase the peak data rate in high velocity environment. Hence, 5G is the better candidate to attain data rates up to 20 Gb/s for eM-BB. So, efficient coding scheme is a challenging task in wireless 5G for high mobility scenario. This project aims to observe that Polar codes are used for capacity improvements. Several researchers are working on this continuously since long back. The current 5G and 3GPP trade off, polar codes are used in uplink and down link as a channel coding in eMBB type of services. Polar codes also used in Ultra low latency and massive machine type communications. Compared to advanced-codes such as Lowdensity-paritycheck (LD-PC) and successive cancellation list (S-CL), therefore the error identification response with finite length systematic polar codes are far better.

II. BACKGROUND OF POLAR CODES

R. Mori, et al [2]: The creators of this paper has given a short clarification about the exhibition of polar codes. These are the principal group of codes-known to accomplish limit of symmetric channels utilizing a low intricacy progressive crossing out decoder. Despite the fact that these codes, joined with progressive wiping out, are ideal in this regard, their limited length execution isn't record breaking.

I. Tal, et al [3]: The creators of this paper has given a short clarification about the strategy for proficiently developing polar codes is displayed and broke down. Albeit polar codes are unequivocally characterized, straight forward development is immovable since the subsequent polar piece channels have a yield letter set that develops exponentially with the code length. In this manner, the center issue that should be explained is that of dependably approximating a bit-channel with an obstinately enormous letters in order by another channel having a reasonable letter set size. They devise two estimate techniques which "sandwich" the first piece channel between a corrupted and an overhauled form thereof. The two approximations can be proficiently figured and end up being amazingly close practically speaking.

P. Trifonov [4]: The creator of this paper has given a short clarification about the proficient plan and translating of polar codes of both summed up linked codes and staggered codes. It is demonstrated that the exhibition of a polar code can be improved by speaking to it as a staggered code and applying the multistage disentangling calculation with most extreme probability deciphering of external codes. Extra execution improvement is acquired by supplanting polar external codes with different ones with better blunder adjustment execution. Sometimes this likewise results in multifaceted nature decrease.

It is appeared Gaussian guess for thickness development empowers one to precisely foresee the exhibition of polar codes and connected codes dependent on them.

M. Morelli, et al [5]: The creators of this paper has given a short clarification about the pilot-supported channel estimation technique for OFDM frameworks is tended to for PACE equidistantly dispersed pilot images permit to reproduce the channel reaction by methods for insertion. The ideal least mean squared blunder (MMSE) estimator performs smoothing and introduction together. To lessen the intricacy of the ideal MMSE estimator, and propose to isolate the smoothing and insertion undertakings. The isolated smoothing and introduction estimator (SINE) comprises of a MMSE based smoother which just works at the got pilot images, and an interpolator which is free of the channel measurements. The isolated methodology draws near to the ideal MMSE, while the intricacy is horribly diminished.

Kai Chen, et al [12]: The SC translating calculation of polar codes and its improved variants, in particular, SCL and SCS, are repeated as way search methods on the code tree of polar codes. By joining the standards of SCL and SCS, a conventional ISC deciphering plan called the SCH unraveling is proposed. This proposed plan can give an adaptable setup when the reality complexities are restricted. To maintain a strategic distance from superfluous way looking, a pruning method reasonable for every one of the three ISC interpreting plans is proposed. Execution and multifaceted nature examination dependent on reproductions demonstrates that in the moderate and high SNR routine, the pruned ISC decoders can approach the exhibition of ML deciphering with the reality complexities extremely near those of SC.

Nadine Hussami, et al [13]: Polar codes, presented as of late by Arkan, are the principal group of codes known to accomplish limit of symmetric channels utilizing a low multifaceted nature progressive undoing decoder. In spite of the fact that these codes, com bined with progressive dropping, are ideal in this regard, their limited length execution isn't record breaking. We talk about a few strategies through which their limited length execution can be im demonstrated. We additionally contemplate the presentation of these codes with regards to source coding, both misfortune less and lossy, in the single-client setting just as for appropriated applications.

Tao Wang, et al [14]: The creators have proposed PCC polar codes to sum up the CRC-linked polar codes. With the proposed heuristic development, the PCC polar codes show a capability of blunder execution upgrades over CRC-connected polar codes, particularly when the codeword length is short and code rate is low.

Kai Niu, et al [24]: The creators in this paper propose a system of rate-perfect punctured polar code. A basic semi uniform puncturing strategy is proposed to produce the puncturing table. By the investigation of the line weight property, this calculation can be viewed as an observationally decent puncturing plan. Recreation results in BI-AWGN channel demonstrate that the presentation of RCPP codes can be equivalent to or surpass that of the turbo codes at a similar code length.

III. BASIC STRUCTURE OF POLAR CODES

Another channel coding has thrived known as polar coding and it is a channel coding plan that was designed by Erdal

Arkan at Bilkent University (Ankara, Turkey) in 2009. Polar Codes are said to accomplish direct limit in a given paired discrete memoryless channel. This can be accomplished just when the square size is huge enough. The multifaceted nature of encoding and translating is less and these codes can be effectively decoded. They have been utilized for testing and are in the long run going to be conveyed by Huawei in 5G systems by 2020 [24].

Generally polar code is said to be a LB-error correcting code. Multiple concatenations that is recursive is said to be the basic building block for the polar code and this is the basis for the code construction. Physical transformation of the channel takes place which transforms the physical channels to virtual channels and this transformation is based on multiple concatenation that is recursive. When the multiple channels multiply and accumulate there is a chance that most of the channels either become good or bad and the idea behind polar code is to make use of the good channels and the idea behind this to send the data through the good channels at rate 1 and send data through the bad channels at rate 0. In other words, the channels are said to enter the polarized state from the normal state [25].

The code development was at first exhibited by Erdal and later Erdal Arkan created it. It is the principal code with an express development to provably accomplish the channel limit with regards to symmetric double info, discrete, memoryless channels (B-DMC) with polynomial reliance on the hole to limit. One increasingly significant thing to be noted here is that polar codes the encoding and disentangling multifaceted nature with unobtrusive development which renders them to be utilized in a ton of utilizations.

As the demand for various accepted cases in 5G like in eMBB, Massive IOT and URLLC increases, there is a need for stronger channel coding efficiency than Turbo Codes. Also, there is an increase in the capacity i.e. the maximum number of subscribers that a channel can sustain at a given point of time. So, Polar codes have been introduced to support increased channel capacity and improved bit error rate. SCL decoders with CRC achieve about 30% reduction in bit rate when compared to its predecessor Turbo Code at the same given conditions



Fig 1: polar code basic channel

IV. PROPOSED CHANNEL ESTIMATION OF POLAR CODES

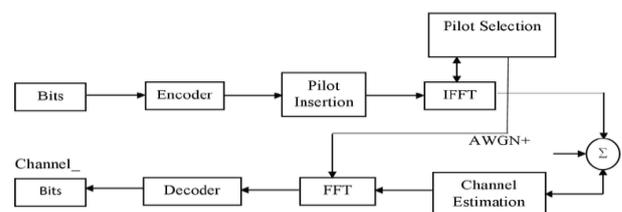


Fig 2: System model

The transmission model is discussed as below. A set of encoded binary bits transmitted through the underlying channel and the elements taken from code word.

The transmitting binary bits are encoded present in the x are through the primary channel $W(y|x)$. Here X is a diagonal matrix. The diagonal matrix given as

$X = \text{diag}\{x_1^N\}$, The corresponding code word signal is give as

$$y_1^N = h_1^N X + z_1^N \quad (1)$$

Where $h_1^N = (h_1, h_2 \dots h_N)$ - channel response for all coded symbols

z_1^N AWGN noise vector.

Every element with zero mean & with variance $N_0/2$. In this ISI(inter-symbol interference) present. The channel h_1^N is expected Rayleigh distribution is followed by Doppler shift f_d . The channel correlation can be defined through Jake's spectrum as below

The Bessel function with zero order is given as:

$$R_{hh}(k) = J_0(2\pi f_d kT) \quad (2)$$

Where R_{hh} - autocorrelation function
T - symbol duration.

4.1 Efficient Selection Criterion

P_f as pilot positions and in P_i as the pilot positions in \bar{A} and in A respectively.

x_{P_f}, x_{P_i} are identified pilot symbols. The encoding through pilot selections of polar codes is comparable to the subsequent problem how to estimate u_A in order to produce $x_A^?$ for every information vector x_A & the building circumstances $\{A, u_A, P_f, P_i\}$ one can instantly detect. The above problem has not any solution meanwhile the linear expression only essential length K vector x_A . There are extra $|P_f|$ well-known values in $x_{\bar{A}}$ in the pilot selection case. Those known pilots x_{P_i} are fixed in the information bits x_A are noted [26].

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$|P_f|$ well-known values in $x_{\bar{A}}$ in the pilot selection case. Those known pilots x_{P_i} are fixed in the information bits x_A are noted.

Now the procedure of encoding can be given as follows

$$(x_c, x_{\bar{c}}) = (u_c G_{cc} + u_{\bar{c}} G_{\bar{c}c}, u_c G_{c\bar{c}} + u_{\bar{c}} G_{\bar{c}\bar{c}}) \quad (3)$$

The set C has not any longer information set as present in the novel encoding. So, the weights of this novel encoding need to be tested. Then the encodable recording requests to be established efficiently. The elements of C and the mapping C could be same. This is the first condition. one-to-one G_{cc} mapping is second condition and it is invertible. The efficient construction depends on the fact $G_{\bar{c}\bar{c}}^{-1} = G_{cc}$. The following is happened when $G_{\bar{c}\bar{c}} = 0$.

The following conditions are satisfied for selection pilots efficiently

Condition 1:

Let $C \subseteq \{1, 2, \dots, N\}$ When $G_{\bar{c}c} = 0$ then $G_{cc}^{-1} = G_{cc}$.

Condition 2:

Let $C = A \cup P_f$ where $P_f \subset \bar{A}$. Compared with $G_{AA}, G_{\bar{c}\bar{c}}$ all are increased columns from G_{AA}

Insertion of pilots is not traditionally in this project. In its place of pilot insertion, selection of pilots technique is used. The pilots selected which are cannot be distributed evenly between 1 to N bit channels.

Two selection schemes are projected based on the effective encoding condition. they are

- The uneven pilot selection (UEPS) and
- The even pilot selection (EPS).

The new encoding set with selection of pilots from the coded symbols is $C = A \cup P_f$, where P_f is containing a set of selected pilot symbols from the A frozen set. The two UEPS and EPS selections are established to meet the effective encoding condition. The condition is $G_{CC} = G - 1_{CC}$ and C is recognized to domination connecting. The efficiency and performance of decoding are explored. The EPS decoding performance is analyzed and displayed by a simulation which is better than the insertion of traditional method.

4.2. UNEVEN PILOT SELECTION (UEPS):

The invertible matrix G_{AA} is a lower triangular matrix in which ones present at diagonal in field of binary. G_{AA} Reveals some of the columns are everything zeros excluding diagonal elements.

The set S is defined as:

$$G_{AA} \quad S = \{j: j \in \bar{A} \text{ and } w(G_{A,j}) = 1\} \quad (4)$$

Where $G_{A,j}$ is the jth column of the sub matrix G_A, G_A , is a sub matrix formed by taking rows \bar{A} from G_N .

The pilots selected which are cannot be distributed evenly between 1 to N bit channels.

4.3. Even Pilot Selection (EPS)

In this section, A different set D is defined as

$$D = \{4K, 1 \leq K \leq N/2\} \quad (5)$$

The submatrix $G_{\bar{D}D}$ of all-zero matrix G_N is stated below

With D defined in (5), the submatrix $G_{\bar{D}D}$ of all-zero matrix G_N is: $G_{\bar{D}D} = 0$

Generator matrix G_N is equal to F^n

Where $F = \begin{pmatrix} 1 & 0 \\ 1 & 1 \end{pmatrix}$.

The G_N matrix can be disintegrated as:

$$G_N = F^{(n-2)} G_4 \quad (6)$$

The matrix G_4 is given as

$$G_4 = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 1 & 1 & 0 & 0 \\ 1 & 0 & 1 & 0 \\ 1 & 1 & 1 & 1 \end{bmatrix} \quad (7)$$

From the above the element of 4th position of last column is non-zero. Now the specified columns by selecting through the set D removing the submatrix of G_N .

V. CHANNEL ESTIMATION BASED ON DB-MS

Coded symbols are used by the pilot selections. Those coded symbols are known as pilots. The EPS pilot selection and traditional pilot insertion are given below



(a) EPS Pilot Selection



(b) Traditional Pilot Insertion

The block diagram for channel encoder is shown in figure 3

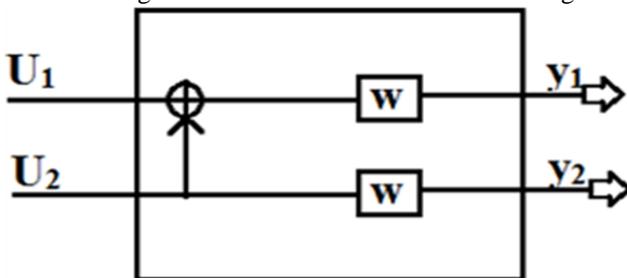


Fig 3: Bipolar code basic channel W_2

Before proceeding with the polar code we construct and specify a channel W_2 which is a Bisymmetric channel and it is to achieve symmetric capacity $I(W)$ which is the highest rate and this is subjected to using the I/P letters of the channel which are equally probable. It is possible to synthesize or create a second set of N binary input channels out of N independent copies of a given B-DMCW channel properties $\{W_N^i \mid 1 \leq i \leq N\}$. One thing to be noted here is that when

N becomes bigger, 2 things tend to happen i.e. some of the fraction of channels for the indices I for $I(W_N^{(i)})$ is near 0 approaches $1 - I(w)$ and rest of the fraction of channels for indices I for $I(W_N^{(i)})$ is near 1 approaches $I(w)$. These polarized channels $\{W_N^{(i)}\}$ are in good condition for channel coding.

So, one should make sure that the channels which are almost near 1 are 1 h avetobesentdatathrough rate of 1 and some of the channels for which capacity is 0 needs to send data at rate 0 i.e. the channels with capacity 0 are said to be junk channels. Therefore, Codes implemented on this Idea are called polar codes. We are trying to prove a fact that the real ways exists a sequence of polar codes $\{C_n; n-1\}$ given any binary discrete memory less channel with $I(W) > 0$ and any target rate $R < I(W)$. The sequence of polar codes are such that C_n has block length $N=2n$ and the bounding for the successive cancellation

decoder is bounded as $P_e(N, R) \leq O\left(N^{\left(\frac{1}{4}\right)}\right)$ which is

said to be independent of the code rate for the probability of block error under successive cancellation decoding. The complexity of the decoders and encoders that achieve this performance are having a complexity of $O(N \log N)$.

For a Bisymmetric channel W, there are basically two channel parameters of interest. One is the symmetric capacity (W) and the second one is the Bhattacharyya parameter.

$$I(W) = \sum_{y \in Y} \sum_{x \in X} \frac{1}{2} W\left(\frac{y}{x}\right) \log \frac{W\left(\frac{y}{x}\right)}{\frac{1}{2} W(y/0) + \frac{1}{2} W(y/1)} \quad (11)$$

and the Bhattacharyya parameter is given by

$$Z(W) = \sum_{y \in Y} \sqrt{W\left(\frac{y}{0}\right) W\left(\frac{y}{1}\right)} \quad (12)$$

The symmetric capacity parameter is used as a measure of rate and the Bhattacharyya parameter is used as a parameter of reliability, respectively. Symmetric capacity is the highest rate at which any reliable communication will take place across the channel W. This will be done using the inputs for the channel W with equal frequency. Bhattacharyya parameter is $Z(W)$ is said to be an upper bound on the probability of maximum-likelihood (ML) decision error when W is used only once to transmit either of the two i.e. 0 or 1.

The performance of channel estimation analyzed by mean square error (MSE). There are two estimators like least square (LS) and minimum mean square error (MMSE) are used in this estimation. To estimate the channel response the technique linear interpolation is used at non-pilot locations.

Let \mathcal{P} be set of pilot locations then

In the LS estimator, the channel response estimation through the pilot locations are given as

$$\tilde{h}_p = y_p X_p^{-1} \quad (13)$$

The mean square error of LS estimator is given as

$$MSE_{LS} = \frac{1}{RE_b/N_0} \quad (14)$$

Even though for the MMSE estimation, the channel response estimation at the pilot locations are:

$$(\hat{h}_p = R_{h_p} \tilde{h}_p \left(R_{h_p} \tilde{h}_p + \frac{1}{RE_b/N_0} I \right)^{-1} \tilde{h}_p \quad (15)$$

Where is a matrix in which the cross correlation of a and b vectors.

Here $R_{ab} = E \{ ab^H \}$ and I is identity matrix. The MSE of \hat{h}_1^N estimation does not in common yield a form of closed expression without any approximations and simplifications. The performance of MMSE is better compared to LS in small E_b/N_0 regions.

The Numerical results of EPS through MSE and UEPS through MMSE & LS are informed. The channel estimation performance of pilot selection schemes EPS or UEPS should have same as the traditional pilot insertion. The channel estimation performance of UEPS should be worse than the EPS due to the pilots have uneven nature.

VI. RESULTS

From fig 4: The expected channel is to be the Rayleigh fading channel. Both LS and MMSE channel estimators are compared. The technique linear interpolation is used to channel estimation at non-pilot locations. $N = 256$ is block length of simulated polar code. The encoded symbols through the scheme BPSK are modulated. In the process of decoding SC decoding is applied. The following setup is selected as a test case: 900 MHz taken as carrier frequency and 256 Ksps as symbol rate. 10 Hz and 50 Hz are Two Doppler frequencies tested & 12 km/h and 60 km/h are the corresponding velocities of dipolar respectively.

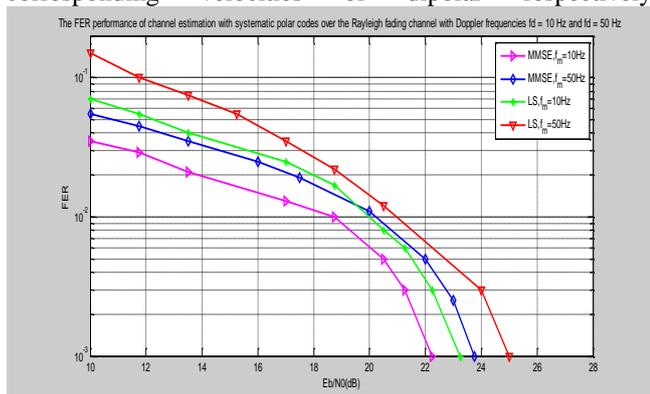


Figure 4: The FER performance of channel estimation over the Rayleigh fading channel $N=256$ and $R=0.5$.

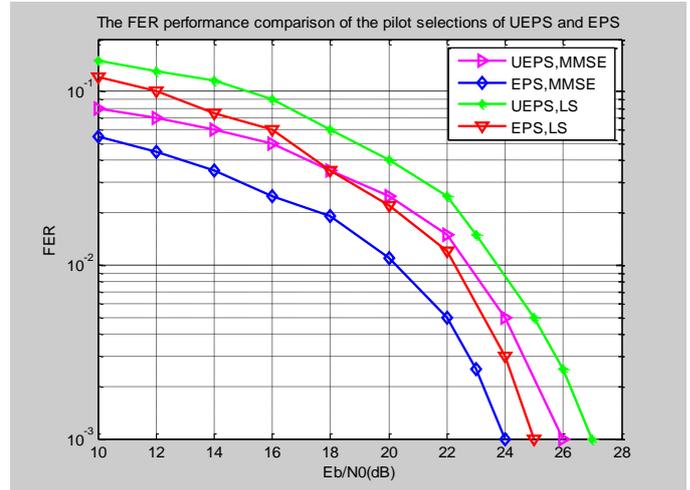


Figure 5: The FER performance comparison of U-EPS and E-PS in the Rayleigh fading channel $N=256$ and $R=0.5$.

From fig 5 The performance of frame-error-rate (FER) for EPS is shown in below graph. The selected pilots are \tilde{h}_p and \tilde{h}_p . $R = 0.5$ is the initial code rate of the polar code. \tilde{h}_p and \tilde{h}_p are the elements in the frozen and information set, respectively. The FER performance of MMSE technique with $\tilde{h}_p = 10$ Hz is enhanced when compared to the LS with the equivalent Doppler shift. When goes up to 50 Hz the MMSE and LS performs worse FER performance than the consistent performance at 10Hz.

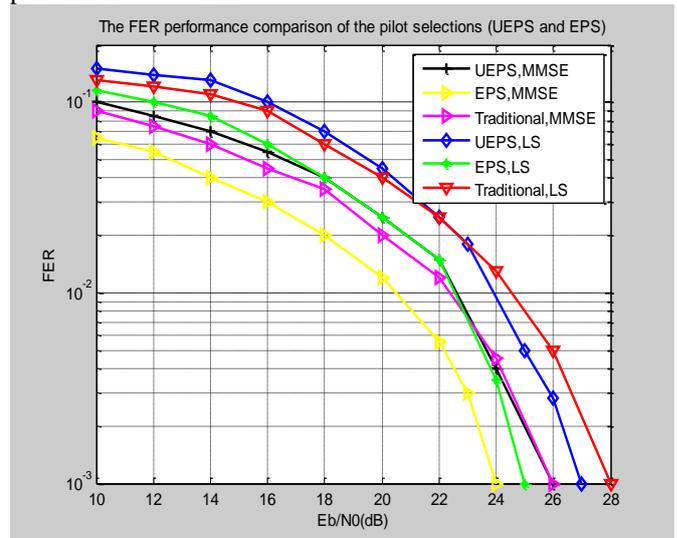


Figure 6: FER performance comparison among pilot selections and traditional pilot insertion method

From fig 6 A comparison between the UEPS and EPS pilot selections and the insertion of pilot traditionally shown in the following graphs. Where $\tilde{h}_p = 50$ Hz is the Doppler shift. In this pilot insertion scheme, pilots are injected evenly. For each four coded symbols one pilot is inserted. The polar code with block length $N = 256$ is used for the pilot insertion and 0.5 is the initial code rate. The numbers of pilots in these three systems are equal. The total number of pilots employed here is 64. In the traditional pilot insertion the overall throughput is $= 128/(256 + 64)$ that equal to 0.4. The same throughput is maintained by UEPS and EPS as that of the insertion of pilot in traditional method, the initial code rate is adjusted as $R = 147/256 = 0.574$.

For both UEPS and EPS schemes, 45 pilots are from among 64 pilot symbols, the final throughput of $\eta = (147 - 45)/256 = 0.4$. When MMSE is applied to UEPS and the traditional method has nearly the equal FER performance and the FER performance of EPS is better when compared to UEPS and traditional insertion. Thus benefit of EPS than UEPS at FER applies at 2dB to the traditional selection of pilots. But, this benefit of EPS terminated the traditional insertion comes that all pilots injected serve only as the elements of channel estimation.

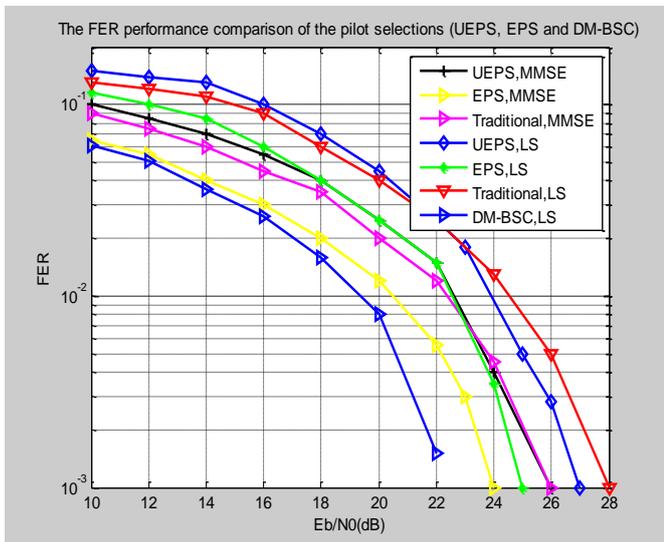


Figure 7: Bisymmetrical channel estimation Vs EPS and UEPS

VII. CONCLUSIONS

Two pilot selection systems, uneven pilot selection (UEPS) and even pilot selection (EPS) are considered for polar codes along with new DM-BSC in fading channels. Instead of pilot insertion, the decoding performance of polar codes is really improved by choosing the pilots. Considering the insufficient performance of polar codes in the fixed domain, the projected pilot selection system EPS can be hired in real systems for channel estimation or tracing. Simulation results display that the projected EPS system beats both UEPS and traditional insertion of pilot systems. So, the polar code performance is improved in wireless communication systems.

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