OFDM-based Massive MIMO Channel Estimation using Gaussian Mixture Learning and Compressed Sensing Methods

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Abstract: Massive MIMO-OFDM system is proved to be an effective and most sustainable technology to forthcoming applications of 5G wireless communications. It furnished significant gains that facilitate a higher number of user connections at high data rates with improved latency and reliability. To achieve accurate channel knowledge, lessen pilot overhead is necessary. To resolve this problem, one of the favorite approaches is compressed sensing. Sparse channel estimation develops the essential sparsity between the communicating channels that can be improved by the channel estimation efficacy with lower pilot overhead. To achieve this, non-zero vector distribution can be taking into consideration the Gaussian mixture accordingly, learn their characteristics towards the expectation-maximization procedure. The results of simulation have proved the performance of proposed estimation approach of channel keeping with minimum pilot overhead and developed exceptional symbol error rate (SER) performance of the system.

Index Terms: Massive MIMO-OFDM, Gaussian Mixture, Approximate message passing, Channel estimation Compressed sensing.

I. INTRODUCTION

The Massive MIMO-OFDM is preeminent and supportive technology to 5G wireless applications that has to maintain excellent data rate and accuracy [1]. To achieve these eminent properties, knowledge of channel information is a most challenging issue in massive MIMO-OFDM systems, therefore, it is necessary to apply relevant estimation techniques to channels between all transmitting and receiving antennas accordingly. In this connection, by the use of proper training sequence design one can acquire accurate channel estimation [6,7]. However, with the help of least square (LS) or minimum mean square error (MMSE) methods to estimate the channel, they are non-supportive for adequate performance due to high computational complexity.

In general, communicating channels are sparse inherently; however, the majority of channels viewed as zero coefficients at channel impulse response (CIR). With a focus on channel sparsity, we implemented the compressed sensing-Aided (CS-Aided) method to characterize the channel properties of the massive MIMO-OFDM model [1]. The key advantage of the proposed approach needs fewer pilots than conventional methods. Many of the researches focused on different Greedy algorithms and Bayesian compressed sensing (BCS) methods [16] which are used to determine the channel estimation onto the concentrated system model. Nonetheless, channel sparsity level is to point out as prior information at the receiving side.

The sparsity adaptive matching pursuit (SAMP) provides high performance at a wide range of practical applications without channel sparsity. However, there is inconsistency between convergence speed and recovery accuracy because SAMP has maintained a constant step size [2, 3]. OFDM is one of the modulating systems that provide to mitigate interference and crosstalk resulting from the conversion of the serial data stream into parallel data stream at different frequencies. OFDM massive MIMO compressed sensing based channel estimation is set as sparse and dense vectors. These vectors are a combination of zero and nonzero vectors respectively. On the perfect sparse recovery, the sparse signal is reconstructed through the support of the LS technique [12].

The expectation-maximization (EM) steps are established to accomplish quantities of estimation following a Gaussian mixture model. Furthermore, the generalized approximate message passing (GAMP) which is an active algorithm in i.i.d distributed random signal [14] is exploiting to develop the expectation step and also mitigate computational complexity. The fast iterative truncation algorithm (FITRA) which is for sparse representation that was elaborated in [8], which found that it has a significant possible convergence rate, provided a regularization parameter to achieve the MUI cancellation and also standardize the functioning of the algorithm. In current work, we established and compared with a renewed compressed sensing aided over Gaussian mixture algorithms for downlink massive MIMO-OFDM systems with a reference of ZF pre-coding technique respectively. To estimate the error performance, the truncated and Bernoulli Gaussian mixture procedures are considered and entrusted to the unknown signal.

Simulated results found that the suggested algorithms provide a substantial improvement in terms of computational difficulties. The remainder part of this work is partitioned as per the following. Second Section discusses downlink and estimation models of noise. The third section covers training sequence design and the principle of estimation to existing technique, the fourth section discusses OMP and Bayesian approaches, fifth section practical issues and finally sixth section concludes.
II. OFDM-BASED MASSIVE MIMO

Let the Base Station (BS) have \( M \) transmitting probes and provide \( K \) independently single element antennae system (\( M \gg 1 \)), and the total OFDM pilot tones \( N \) that are assumed in figure 1. Indeed, the set of accessible pilot tones are separated into data transmission and guard band. Therefore, every pilot tone of the corresponding \( K \times 1 \) signal vector of \( x(n) \), that includes pilot symbols of \( K \) users and of corresponding \( n^{th} \) transmission symbol time with the data vector to satisfy \( E[||x(n)||^2] = 1 \). In accordance with pilot tone is to be set \( \text{as} \{n\} = 0_{K \times 1} \). Consequently, there is no way to exist the signal within the guard band. Now, take into consideration Zero-Force (ZF) pre-coding spatial signal approach for removal of multi-user interference (MUI) at BS because collaborative sensing across the users is much complicated.

The pre-coding sparse signal vector on the \( n^{th} \) pilot tone can be expressed as

\[
s(n) = P(n)x(n) \tag{1}
\]

Where \( x(n) \in \mathbb{C}^{M \times 1} \) and \( P(n) \in \mathbb{C}^{M \times K} \) are precoded vector of \( n^{th} \) sub-carrier of \( M \) antennas and pre-coding channel matrix of \( n^{th} \) OFDM pilot tone respectively. In view of the fact that \( K << M \), the ZF pre-coding spatial channel vector matrix is expressed by

\[
P^Z_F = \begin{bmatrix} X_1^H \quad \cdots \quad X_M^H \end{bmatrix}^{-1} \tag{2}
\]

here \( P^Z_F \) provides the inverse and of pseudo-inverse of \( P(n) \) of \( n^{th} \) pilot tone in MIMO channel vector matrix. Then after pre-coding, every pre-coded vector \( h(n) \) is rearranged by \( M \) antennas to the downlink OFDM conversion such as

\[
[a_1 \ldots a_M] = \begin{bmatrix} h_1 \ldots h_M \end{bmatrix}^T \tag{3}
\]

Here \( h_m \in \mathbb{C}^{N \times 1} \) denotes the frequency-domain samples at the \( m^{th} \) antenna. Signals of time-domain can be achieved by the result of inverse discrete Fourier transform (IDFT). Thereafter, overcome the inter symbol interference (ISI) by inserting cyclic prefix (CP) to the corresponding time-domain signals of respective antennas. Finally these time varying quantity signals are changed as analog signals for channel transmission.

After eliminating the CPs, the Discrete Fourier Transform (DFT) serves to achieve the frequency-domain signals. The transformed received vector of N-point DFT inclusive of \( K \) user signals are represented by

\[
F(n) = \frac{1}{\sqrt{N}} \exp \left( \frac{j2\pi n}{N} \right) \quad 0 \leq n \leq N - 1 \tag{4}
\]

The signal corresponds to \( K \) user symbols expressed as

\[
y(n) = X(n)h(n) + z(n) \tag{5}
\]

Where \( X(n) \) and \( h(n) \) are the vectors for channel belongs to \( \mathbb{C}^{N \times 1} \) and \( z(n) \) is the receiver noise corresponding to \( n^{th} \) transmitted symbol.

The received signal vector appears error free MUI signal as

\[
y(n) = h(n) + z(n), \quad \text{while adding of equation (1),(2) and (4) which is to be involved ZF pre-coding scheme [17].}
\]

The transmitted pilots of \( n^{th} \) antenna can be expressed as

\[
Y_p = X_{P_1}, \ldots, X_{P_K}, \ldots, X_{P_1}^T \in \mathbb{C}^{N \times 1}, \quad \text{where } [P_1, P_2, \ldots, P_K] \text{ representation of a pilot location. The signal received at the } n^{th} \text{ antenna can be denoted as}
\]

\[
y(n) = \sum_{i=1}^{L} \text{diag} F(n) s(n) + z(n) \tag{6}
\]

In this system model we consider 256 Base station antennas operates with 128 antenna users and 16-QAM constellation is used with 32 OFDM pilot tones. Due to hundreds of transmit antennas at BS, explicitly degrades their channels performance, and also causes high pilot overhead to estimatethe channels. Accordingly, it is necessary to mitigate the high pilot overhead in employing system towards higher datarates.

III. CS-BASED CHANNEL ESTIMATION

Consider generated DFT signal (Frequency domain) matrix and additive noise of massive MIMO-OFDM model of \( n^{th} \) antenna that is denoted as

\[
y_p = \sum_{i=1}^{L} \text{diag}(X_p)F_p h_n + z_p \tag{7}
\]

To estimate unknown vector \( h_n \) of massive MIMO-OFDM system, the proposed CS recovery algorithm is employed. For channel estimation in OFDM, the Greedy iteration reconstruction schemes [4, 7-9] have delivered potential performance.

Nonetheless, in many conventional greedy algorithms requires priori information at receiver side. Moreover, the greedy iteration schemes suffer with inaccuracy and more computational complexity [12, 15]. Either of these two schemes has been successfully detected the fading channel information [14]. However, the proposed CS recovery algorithm need not consider the channel level as a priori information. This iteration is in accordance with the Partial common support information (PCSI) and depending on an iteration threshold. The PCSI of the \( n^{th} \) receive antenna is expressed by

\[
I_n = \sum_{n=1}^{L} I_n + (n - 1)L \tag{8}
\]

In the CS based channel estimation algorithm the following notations are involved. Updated measurement matrix, Observation vector, column index, iteration threshold, updated index, estimated channel vector, and residual are expressed by \( A_{n}, Y_{n}, \lambda_{n}, \epsilon, \Lambda_{n}, r_{n}, h_{n,t} \) respectively [5].
There are two major challenges with applying OMP to massive data [13, 15]. Firstly, the computation complexity and an iteration storage cost are relatively large and secondly, the single coefficient selection simultaneously requires the corresponding k iterationsto estimate with coefficient \( \mu_q \). whenever, the k iterations are increases that leads impractical slow down its performance. To estimate the channel to the CS-based massive MIMO-OFDM, the following algorithm used as given below.

Algorithm I:
CS-Based Channel Estimation of Massive MIMO-OFDM

**Input:** The first formulations \( A_0,Y_p \) and \( I_n \) are selected.

1. Initialize \( A_0 = I_n, A_0 = A_0|_{\lambda_0} \).
2. \( r_0 = Y_p - A_0(A_0^T A_0)^{-1} A_0^T Y_p \), \( t = 0 \) and \( \varepsilon \approx 0 \).
3. \( \lambda_t = \arg \max_{\lambda \in (0,N-1)} \{ |r_{t-1}^T A_0| \} \).
4. \( A_t = A_{t-1} \cup \{ \lambda_t \} \).
5. \( A_t = A_t \setminus \{ \lambda_t \} \).
6. \( \hat{h}_{n,t} = \arg \min \| Y_p - A_t \hat{h}_{n,t} \| = (A_t^T A_t)^{-1} A_t^T Y_p \).
7. \( r_t = Y_p - A_t \hat{h}_{n,t} \).
8. **End while**

**Output:** estimate the CIR \( \hat{h}_{n,t} \).

CS based schemes (Static or Dynamic LS, OMP, CS-Aided BCS), the number of iterations are based on sparsity level of the channel [3, 6, 11] whereas the proposed method closes iteration only when the residual is on the threshold of 0. Consequently, the recovery accuracy can be assured. Moreover, when acquired accurate partial common support information, the number of iterations are limited; leads decrease computational complexity of the proposed method.

To achieve this objective, we propose a Gaussian mixture (GM) methodical approach afterwards utilizing the expectation-maximization (EM) method [14] for determination of noisevariance and GM parameters. However, no need for concern quantitiesfor theEM updates because these computations made by suggested GAMP algorithm to decrease computational complexity [9]. The proposed generalized EM-TGM-AMP and EM-BGM-AMP can be effectively addressing at parametric estimation with i.i.d zero-mean Gaussian.

IV. GAUSSIAN MIXTURE GENERALIZED AMP

To address the random Gaussian noise, generalized AMP (GAMP) algorithm, proposal was made by Rangan [7, 16]. This proposed approach need not require knowledge about \( p_x(x) \) and the postulated noise variance, nevertheless it presents great recovery performance, that need to know about these postulated information. In this Gaussian-mixture GAMP algorithm, we consider the coefficient in \( x = [x_1,x_2,\ldots,x_N]^T \) is approaching to the i.i.d distribution with marginal probability density function can be expressed as

\[
p_x(x; \lambda, \omega, \theta, \phi) = (1 - \lambda) \delta(x) + \lambda \sum_{i=1}^{L} \omega_i N(x; \theta_i, \phi_i)
\]

where \( \delta(\cdot) \) function denotes Dirac delta identity and \( \lambda \) is the percentage of sparsity rate. And \( \omega, \theta, \phi \) coefficients are expressed as the weight, mean, and variance of \( k \) Gaussian mixture components respectively. In the remainder part \( \Sigma_{i=1}^{L} \omega_i = 1 \) and zero mean and variance \( \psi \) is used as noise. Here, the postulated parameters of GM-GAMP \( q \triangleq (\lambda, \omega, \theta, \phi, \psi) \) are taken into consideration as known and fixed variables. Firstly, carry out the conditional distribution \( p_{y|x}(y|x;q) \) the expanded postulated approximation can be expressed as

\[
p_{y|x}(y|x;q) = \frac{p_{y|x}(y|x;q) N(z; \hat{p}_n, \mu_n^q)}{\int_Z p_{y|x}(z|x;q) N(z; \hat{p}_n, \mu_n^q)} \tag{10}
\]

The moments of above density function under AWGN assumption is as

\[
E_{y|x}(y|x;q) = \hat{p}_n + \frac{\mu_n^q}{\mu_n^q + \psi} (y_n - \hat{p}_n) \tag{11a}
\]

\[
\text{var}_{y|x}(y|x;q) = \frac{\mu_n^q \psi}{\mu_n^q + \psi} \tag{11b}
\]

Secondly for computing the conditional distribution \( p_{y|x}(x; y;q) \) the expanded postulated approximation can be expressed as

\[
p_{y|x}(x; y;q) = \frac{p_{y|x}(x; q) N(x; \hat{r}_i, \mu_i^q)}{\int_{x} p_{x}(x;q) N(x; \hat{r}_i, \mu_i^q)} \tag{12}
\]

To achieve subsequent approximation of GM-GAMP substitute the postulated parameters (3) into (8) and simplified expression can be given as

\[
p_{y|x}(x; y;q) = \left[ (1 - \lambda) \delta(x) + \lambda \sum_{i=1}^{L} \omega_i N(x; \hat{r}_i, \mu_i) \right] \left[ (1 - \pi_i) \delta(x) + \pi_i \sum_{j=1}^{L} \beta_i^j N(x; \hat{r}_j, \mu_j) \right] \tag{13}
\]

In (13) \( \pi_i \) indicates posterior support probability values, \( \text{Pr}(x_i \neq 0|y;q) \) of GM-GAMPapproximation. The normalized factor in (13) can be written as

\[
\zeta_i = \int_{x} p_{x}(x;q) N(x; \hat{r}_i, \mu_i) = (1 - \lambda) N(0; \hat{r}_i, \mu_i^q)
+ \lambda \sum_{i=1}^{L} \omega_i N(0; \hat{r}_i - \theta_i, \phi_i) \tag{14}
\]

Both (13) and (14) can be derived from (13a) through Gaussian probability density function multiplication rule. In (14) the following dependent variables can be given by

\[
\pi_i \triangleq \frac{1}{1 + \left( \frac{\Sigma_{i=1}^{L} \beta_i^j}{(1 - \lambda)/N(0; \hat{r}, \mu_i^q)} \right)^{-1}} \tag{15a}
\]
\[ y_{i,j} \triangleq \frac{\hat{\mu}_i}{\mu_i^2} + \theta_i/\phi_i \quad \text{and} \quad v_{i,j} \triangleq \frac{1}{\mu_i^2} + 1/\phi_i \]  
\[
\beta_{i,j} \triangleq \lambda \omega_i N(0; \tilde{v}_i, \gamma_i \mu_i' + \phi_i) \quad \text{and} \quad \beta_{i,j} \triangleq \sum_{l=1}^{L} \beta_{i,k} \]  
(15b)

To achieve effectiveness of GAMP approximation along with L-term Gaussian Mixture is used to overcome difficulties on unrealistic implementations. Using Bayesian parameter estimate method through AMP algorithm [4, 26], provides accurate approximation that involves central-limit theorem, together with independent identically distributed zero-mean Gaussian A.

V. EM LEARNING OF THE PRIOR PARAMETERS

Let us focus on learning of the priori parameters \( q \triangleq (\lambda, \omega, \theta, \phi, \psi) \) with the help of expectation-maximization (EM) algorithm [5, 8, 14]. The maximum likelihood \( p(y; q) \) maximized a lower bound at each iteration. The given illustration approximates the priori parameters by the following EM procedure.

\[
\int_x \hat{p}(x) \ln p(y; q) = \int_x \hat{p}(x) \ln \left( \frac{p(x; y; q)}{\hat{p}(x)} \right) \]  
\[
E_{\hat{p}(x)} \left[ \ln p(x; y; q) + H(\hat{p}) + D(\hat{p}||p|x|y; q) \right] \]  
(16)

Here \( E_{\hat{p}(x)} \{ \cdot \} \), \( H(\hat{p}) \) and \( D(\hat{p}||p) \) represents the expectation, entropy and Kullback-Leibler (K-L) divergence respectively. Here EM bounds are fixed as \( (q = q^n) \) and \( (\hat{p} = \hat{p}^n) \) respectively: expectation \( \ln p(y; q^n) - D(\hat{p}||p|_{y|x}|q^n) \), afterwards the maximized function described as \( \hat{p}^n(x) = p|_{y|x}(x|y; q^n) \), maximization \( E_{\hat{p}(x)} \left[ \ln p(x; y; q) + H(\hat{p}) \right] \), after that the maximized function produces as \( q^{n+1} = \arg \max_q E \left[ \ln p(x; y; q) | y; q^n \right] \) [6]. Where \( E \) implies the use of said posterior approximation. In addition to update the noise variance \( \psi \) from determination of \( q^n \), therefore it can be expressed as

\[
\psi^{n+1} = \arg \max_{\psi > 0} \sum_{m=1}^{M} \int_x p_2(z_m \mid y_m; q^n) \]  
\[
\cdot \cdot \cdot \ln p_2(y_m \mid z_m; \psi) \]  
(17)

The maximized parameter \( \psi \) that the derivative of the sum value is zero, in such way that can obtain following noise variance parameter is

\[
\psi^{n+1} = \frac{1}{M} \sum_{m=1}^{M} (|y_m - \hat{z}_m|^2 + \mu_{\psi}^2) \]  
(18)

A. EM Updates of BGM case

Consider the marginal pdf of Bernoulli-Gaussian with \( \xi \), GM model makes it possible to reduce to (17) then results as \( p_2(x; \lambda, \omega, \theta, \phi) = (1 - \lambda) \delta(x) + \lambda N(x; \theta, \phi) \). Note that in this case need not to find out the weight because its unity, so the prior benchmarks can be expressed \( q^n \triangleq (\lambda^n, \omega^n, \theta^n, \phi^n, \psi^n) \).

\[
\lambda^{n+1} = \arg \max_{\lambda \in (0,1)} \sum_{i=1}^{L} E \left[ \ln p(x; \lambda^n, \omega^n, \theta^n, \phi^n, \psi^n) \right] \]  
(19)

The maximized parameter \( \lambda \) that the derivative of the sum value is zero, in such way that can obtain following parameter is

\[
\lambda^{n+1} = \frac{1}{L} \sum_{i=1}^{L} \pi_i \]  
(20)

In the similar way of (19), updated EM parameters of \( \theta, \phi \) are represented by

\[
\theta^{n+1} = \frac{1}{\lambda^{n+1}} \sum_{i=1}^{L} \pi_i y_{i,1} \]  
(21)

\[
\phi^{n+1} = \frac{1}{\lambda^{n+1}} \sum_{i=1}^{L} \pi_i (\theta^n - y_{i,1})^2 + v_{i,1} \]  
(22)

To estimate the channel performance to the CS-based massive MIMO OFDM, the EM-BGM-AMP algorithm is used as given below.

Algorithm II: EM-BGM-AMP

Initialize the value of \( L, \hat{x}^0 = 0 \) and unknown parameter of \( q^0 \).

For \( n = 1 \) to \( N_{max} \) do

\[
\text{Generate } \hat{x}^n, \hat{z}^n, (\mu^n)^n, (\beta^n)^{M I} \]  
\[
\text{through BGM-GEMP with } q^n - 1 \]  
\[
\text{if } ||\hat{x}^n - \hat{x}^{n-1}||_2 < \tau_{EM} ||\hat{x}^{n-1}||_2 \text{ then} \]  
Break

end if

Compute \( \lambda^n \) from \( \pi_{n-1} \).

For \( k = 1 \) to \( M \) do

if sparse mode value enabled then

Compute \( \theta^n \) from \( \pi_{n-1}, \gamma_k^n, \beta_k^n \) \( \hat{x}^{n-1} \) through BGM-GEMP.

end if

Compute \( \phi^n \) from \( \pi_{n-1}, \gamma_k^n, \beta_k^n \) \( \hat{x}^{n-1} \).

Compute \( \omega^n \) from \( \pi_{n-1} \) and \( \beta^{n-1} \).

end

Compute \( \psi^n \) from \( \hat{x}^n \) and \( (\mu^n) \).

end

Apply the Leibniz’s integral principle to interchange of differentate and integrate signs, the Dirac approximation using this \( \delta(x) = N(x; 0, \epsilon) \) for establishing randomly \( \epsilon > 0 \), then complete, and its differential coefficient with respect to \( \lambda \) make steadily. The similar interpretation can be addresses to all interchange of differentiation and integration in the sequence, also mentioned in section III.

B. EM Updates of GM case

Firstly we initiate EM update for \( \lambda \) from priori parameters \( q^n \triangleq (\lambda^n, \omega^n, \theta^n, \phi^n, \psi^n) \). Since \( \lambda^n \) is presented in (19) BG case i.e. \( \lambda^{n+1} = \frac{1}{L} \sum_{i=1}^{L} \pi_i \), so for concise not be repeated here. Now we consider the remaining parameters \( \omega, \theta \) and \( \phi \). In this case, \( k = 1, 2, ..., L, \) the
updates are incremented one by one that is \( \theta_k \rightarrow \phi_k \rightarrow \omega \), all these parameters are fixed variables. The Prior parameters in the form of \( p_x(x) = (1 - \lambda) \delta(x) + \lambda f_x(x) \), is to provide randomly by \( f_x(x) \), the EM update for \( \lambda \) is specified by (20). Therefore the EM updates are identified by

\[
\theta_{k+1} = \arg \max_{\theta_k \in \mathbb{R}} \sum_{i=1}^{l} \mathbb{E} \left[ \ln p_x(x_i; \theta, q^n) \middle| y, q^n \right] \\
\phi_{k+1} = \arg \max_{\phi_k > 0} \sum_{i=1}^{l} \mathbb{E} \left[ \ln p_x(x_i; \phi_k, q^n) \middle| y, q^n \right] \\
\omega_{k+1} = \arg \max_{\omega_k > 0} \sum_{i=1}^{l} \mathbb{E} \left[ \ln p_x(x_i; \omega, q^n) \middle| y, q^n \right]
\]

(23a)  

(23b)  

(23c)

The maximized value of \( \theta_k \) is fundamentally requires zeros the derivative, i.e., that accomplished expression is

\[
\sum_{i=1}^{l} \int_{x} p(x|y; q^n) \frac{d}{d\theta} \ln p_x(x_i; \theta, q^n) \middle| y, q^n \right) = 0
\]

(24)

Substitute the maximized value (23) in (22a) then produces

\[
\sum_{i=1}^{l} \int_{x} p(x|y; q^n) \frac{d}{d\theta_k} \ln p_x(x_i; \theta_k, q^n) \middle| y, q^n \right) = 0
\]

(25)

Plugging in the derivative and apply the approximation \( N(x_i; \theta_k, \phi_k^n) \approx N(x_i; \theta_k^n, \phi_k^n) \) to numerator and denominator. Finally we acquired the simplified approximation coefficients are

\[
\theta_{k+1} = \sum_{i=1}^{l} \sum_{k=1}^{n} \pi_i \beta_i k \mu_{i,k} \\
\phi_{k+1} = \sum_{i=1}^{l} \sum_{k=1}^{n} \pi_i \beta_i k \left| \phi_{i,k} - \gamma_{i,k} \right|^2 + \nu_{i,k} \\
\omega_{k+1} = \sum_{i=1}^{l} \sum_{k=1}^{n} \pi_i \beta_i k
\]

(26)

(27a)  

(27b)

C. EM Updates of TGM Case

The advantage of GAMP method is to provide the approximation of the likelihood function \( p(\mathbf{y}; \mathbf{q}) \) through \( \hat{p}(\mathbf{y}; \mathbf{q}) = p(\mathbf{x}|\mathbf{y}; q^n) \) and the EM produces a new estimate of \( \mathbf{q}(\mathbf{x}) \) and \( \hat{q}(\mathbf{y}) \), in addition to posterior distributions of the other involved variables and determinate the boundary parameter \( \nu \). The algorithm summarizes the proposed approach as follows.

For the concise of this work we do not repeat the posterior approximations here; new updates of noise variance present as

\[
\psi_{n+1} = \sum_{m=1}^{M} p(z_m | y)^n \ln p(y_m | z_m; \psi) + \text{const}
\]

\[
= \frac{N}{2} \ln \psi - \frac{1}{2} \psi \sum_{m=1}^{M} (y_m - z_m)^2 + \mu_m^2
\]

(28)

The new approximate parameter of \( \psi \) is selected by setting to fundamental requirement of zeros the derivation refer (24), that leads an achieved expression is

\[
\psi_{n+1} = \frac{M}{\sum_{m=1}^{M} (y_m - z_m)^2}
\]

(29)

To estimate the channel performance to the CS-based massive MIMO-OFDM, the EM-TGM-AMP algorithm is used as given below.

Algorithm II: EM-TGM-AMP

The first formulations \( \psi(0), v(0) \) are selected.

1. Initialize the mean, variance parameters of \( \mathbf{q}(\mathbf{x}) \) and GAMP iterations the iteration number, \( t \), with zero. Repeat until \( t \leq t_{\text{max}} \)

2. Calculate the approximate distribution \( \hat{p}(\mathbf{x}|\mathbf{y}; \mathbf{q}) \) and \( \hat{p}(\mathbf{z}|\mathbf{y}) \).

3. Utilize the approximate likelihoods \( \hat{p}(\mathbf{x}|\mathbf{y}; \mathbf{q}) \). update Posterior variables \( \hat{q}(\mathbf{y}) = \lambda^n, \theta^n, \phi^n \).

4. Compute noise variance \( \hat{v}_{n+1} \) from and obtain \( \hat{v}_{n+1} \).

5. \( t = t + 1 \).

Return to step 2.

Now consider the boundary parameter \( \nu \), to achieve this choose the mean of posterior distributed parameter of \( \mathbf{q}(\mathbf{x}) \).

\[
v_{n+1} = v_{n} + \Delta_{v}
\]

(30)

Where \( \Delta_{v} \) step-size of boundary points is: expand the boundary point \( \nu \) for that adequately smaller step-size \( \Delta_{v} \). Here we may be able to anticipate towards the signal \( x \) will increase as a result.

VI. SIMULATION RESULTS AND DISCUSSIONS

The efficiency of proposed truncated Gaussian mixture EM-GAMP and Gaussian Bernoulli EM-GAMP algorithm can be compared in accordance with obtained results of zero-forcing (ZF) pre-coding OMP and CS-Aided approach.

Fig. 1 presents the comparison of various schemes of NMSE performance with known error varie value of \( k_{\nu} \) (assumed estimate channel coefficients \( k_{\nu} = 2 \)). The estimation methods are employing with the previous support informationshow the poor performance upon the unbalanced parameter arises, whereas the quality of support information is trivial to the proposed approaches. Because the imperfect channel coefficients are evaluated by a compressed sensing (CS) algorithm and has low mismatched influence. In addition, if erroneous coefficients are selected by this method that clipping step can terminate the impact of erroneous coefficients. In addition, proposed and CS-Aided methods can be maintained the constant support information.
OFDM-Based Massive MIMO Channel Estimation using Gaussian Mixture learning and Compressed Sensing Methods

The effectiveness MSE with different algorithms is proved in Fig.3. It appears that the suggested schemes are achieved better Signal to noise ratio (SNR) performance as against the ZF pre-coding. However, the ZF provides the least-norm solution.

In order to sustain the same, must have to remove the undesirable characteristics, i.e. perfect normalization is must. In comparison to this, LS based schemes have less error. For SNR between 10-11 dBs, the proposed schemes are better than ZF and as reasonably good performance. Overall, the performed proposed methods have less error than conventional CS techniques.

According to estimate made by comparison, the GM-based CS approaches are easy to determine better training signals. Thus, quality of channel estimate is evaluated by the intended GM-based CS approaches which provides better performance through flagship challenge of the trainingsignals.

VII. CONCLUSION

This work focused on estimate the channel efficacy over OFDM based massive MIMO downlink system under Gaussian mixture learning with various approaches for compressed sensing. Particularly the composition of the GAMP technique with the EM iterative methods and they facilitate the less computational complexity through designed pilot approach. Through the continuous support of the CS-Aided approach, the pilot overhead is reduced. The favorable channel performance is achieved by the use of EM-TGM-GAMP, EM-BGM-GAMP, and CS-Aided schemes. The obtained simulation figures give the truncated GM appears better performance than GB distribution in CS, and also achieved better output compared to the ZF and OMP techniques.

REFERENCES


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