

Applications of Fuzzy dot i^* algebra in Computer Vision



P.Manjula, P.Sundararajan

Abstract: Right now shows another route sort of identifying an edges and corners in the computer vision calculation. The Edge location is a key purpose of numerous calculations, both in picture preparing and video handling. It is significant that the calculation is proficient quick to bring out through the whole program. The custom system is to utilize the edge recognition it's not giving the better outcome dependent on the presumptions. In these conventional procedures here and there is vulnerability of the edge, and the man can't recognize whether it is the edge or not. So as to turn the fuzzy dot i^* algebra based edge and corner (named as FDIA) all things considered and tackle the above issues.

Fuzzy innovation has been a recent rising innovation utilized in numerous fields, particularly in the image handling, and computer vision is one significant piece of the fuzzy innovation. In light of this innovation, the edges and corners recognize by vigilant corner identification, calculation likewise to portray devices from picture preparing and the speed with the assistance of MATLAB programming.

Keywords: Fuzzy i^* algebra, Corner & Edge detection, image processing and computer vision.

I. INTRODUCTION

The field of computer vision has been experiencing enormous improvement as of late. The computer vision is worried about creating frameworks that can decipher the substance of characteristic scenes. The computer vision frameworks start with the way toward recognizing and finding a few highlights in the information picture.

As per [1] Corner discovery calculation can be separated into two kinds: one depends on the picture dim information; the other depends on picture edge information. How much a computer can extricate important data from the picture is the most dominant key to the development of shrewd picture getting frameworks.

Highlight extraction and picture division assume an indispensable job to fill the hole between what we can get and what we need to have in light of the fact that the corners are demonstrated to be steady across successions of pictures. Perhaps the greatest favorable position of highlight extraction lies that it altogether decreases the data to speak to a picture for understanding the substance of the picture.

Numerous computer vision calculations use highlight discovery as the underlying advance, so subsequently, countless element finders have been created dependent on edges and districts.

In this paper a fuzzy dot i^* algebra algorithm based edge and corner detection method is proposed, namely FDIA method and its performance are studied using real images with error tolerance. The most widely used existing methods, Harris, SUSAN, SIFT and FAST techniques, are briefly discussed in the section 2. The proposed FDIA technique and its computational algorithm are presented in the section 3. The performance of the proposed algorithm is carried out using different types of images/blurred images by using MATLAB software and the results thus obtained are summarized in the section 4. The last section discusses the conclusion of the study.

II. EXISTING MODELS FOR EDGE & CORNER DETECTION TECHNIQUES

2.1 Corners & Edge detection Approach

2.1.1 Moravec Corner Detection

The Moravec (1977) developed an operator for his research involving the navigation of the Stanford Cart through a clustered environment. Since it defines interest points as points where there is a large intensity variation in every direction, which is the case at the corners, the Moravec operator is considered a corner detector.

The idea is to consider the neighborhood of a pixel in the image and to determine mean changes of the intensity function when the neighborhood is moving in several directions. The algorithm is briefly summarized as follows:

Here, first compute the intensity variation $V_{u,v}(x,y)$ of each pixel (x,y) from a shift (u,v) which are $(1,0)$, $(1,1)$, $(-1,0)$, $(-1,-1)$, $(0,-1)$, $(1,-1)$. Find the corners map by calculating the corners measure $C(x,y)$ for each pixel (x,y) , where $C(x,y) = \text{Min}(V_{u,v}(x,y))$.

The Perform non-maximal suppression to find local maxima by setting all $C(x,y)$ below a threshold T to zero. Finally the corners are detected by all non-zero points remaining in the corners map. It is only a set of shifts at every 45 degrees is considered. The noisy response is low due to a binary window function.

2.1.2 Harris Corner Detection

Harris (1988) planned a way to resolve the issues of strident response thanks to a binary window operate, specifically Harris corner detector by applying the Gaussian strident filter.

The Harris corner detector is predicated on the native auto-correlation operate of a proof that measures the native changes of the signal with patches shifted a low quantity in several directions.

Revised Manuscript Received on March 30, 2020.

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Given a shift (x, y) a degree the auto-correlation operate is outlined as,

$$C(x,y)=\sum w[I(x_i,y_i)-I(x_i+\Delta x, y_i+\Delta y)]^2$$

where the image function I(.) is approximated by a Taylor expansion truncated to the primary order terms. C(x, y), the auto-correlation matrix which captures the intensity structure of the local neighborhood.

Finally, find the corner points as local maxima of the corner response by characterizing corner by the eigenvalues of C(x, y).

2.3 Wang-Brady Corner Detection

In general, the corner operator is based on the cornerness measurement of total curvature, i.e., the second order tangential derivative. Conventionally directional derivatives are obtained from linear combinations of first and second derivatives with respect to the x and y components. These methods are does not provide the reliable result and also more computationally expensive.

Wang and Brady proposed method to solve this problem and get the improved accuracy of corner localization by adopting the linear interpolation scheme. The empirical parameters, constant measure of image surface curvature S and threshold T are determined depending on the context of the image.

2.4 Shi-Tomasi Corner Detection

Shi and Tomasi (1994) planned a way, that relies on a brand new trailing formula by extending the previous Newton-Raphson vogue search technique underneath affine image transformation.

$$\epsilon = \iint [J(Ax + d) - I(x)]^2 w(x) dx.$$

On the simplification the corner detection form of operator is

$$T = \iint \begin{bmatrix} U & V \\ V^T & Z \end{bmatrix}.$$

It finds N strongest corners within the image. First, specify the standard level, that could be a price between 0-1, that denotes the minimum quality of corner underneath that most are rejected supported the minimum geometric distance between corners detected. Then, the operator finds corners within the image.

All corners below quality level area unit rejected. Then it types the remaining corners supported quality within the descending order. Then operate takes an initial strongest corner, throws away all the close corners within the vary of minimum distance and returns N strongest corners.

2.5 Smallest Univalues Segment Assimilating Nucleus (SUSAN) Corner Detection

Smith and Brady (1997) entrenched a replacement approach to low level image process, especially, edge and corner detection and structure protective noise reduction. These ensuing strategy's area unit correct noises resistant, specifically smallest uni-values section assimilating nucleus. The SUSAN principle is developed within the following equation, wherever n(x0) is the USAN size at x0, on the simplification,

$$\frac{dI}{dx}(x_0 + a(x_0)) - \frac{dI}{dx}(x_0 + b(x_0)) = 0$$

The SUSAN detectors are a unit supported the minimizing of the native image region, and also the noise reduction methodology uses the region within the smoothing the neighborhood.

2.6 Trajkovic-Hedley Corner Detection

Trajkovic Associate in Nuring Hedley (1998) developed an operator supported the property of corners the modification of image intensity ought to be high all told directions. The comer response performs (CRF) is computed as a minimum modification of intensity overall doable directions.

A multigrid approach is utilized to cut back the machine complexes and to enhance the standard of the detected corners. To beat the matter of lines at sure orientations being detected as comers Associate in Nursing inter-pixel approximation was used.. The corner detection operator is as follows;

$$r_1(\alpha) = A \cos 2\alpha + B_1 \sin 2\alpha + C \quad \& \quad r_2(\alpha) = A \cos 2\alpha + B_2 \sin 2\alpha + C,$$

where $A = \frac{r_A - r_B}{2}$ & $B = \frac{r_A + r_B}{2}$

2.7 Scale Invariant Feature Transform (SIFT) Corner Detection Algorithm

SIFT (Scale Invariant Feature Transform) corner detection is realized by extracting distinctive invariant options from pictures, that was projected by DAVID G. LOWE (2004). For any object in a picture, attention-grabbing points on the item may be extracted to supply a "feature description" of the item. This description, extracted from a coaching image, will then be wanting to establish the item once attempting to find the item in an exceedingly take a look at image containing several alternative objects.

To perform reliable recognition, it's vital that the options extracted from the coaching image be detectable even under changes in image scale, noise and illumination. Such points, sometimes dwell high-contrast regions of the image, like object edges.

Another vital characteristic of those options is the relative positions between them within the original scene should not amend from one image to a different. Their rotation-invariant, which suggests, even though the image is turned, one will realize identical corners. However, a corner might not be a corner if the image is scaled.

The SIFT key points, distinctiveness is achieved by collecting a high-dimensional vector representing the image gradients inside a neighboring region of the image.

The key points are shown to be invariant to image rotation and scale and strong across a considerable variety of affine distortion, addition of noise, and alter in illumination. Massive numbers of key points may be extracted from typical pictures, that results in the strength in extracting little objects among the clutter. The SIFT key points perform well for pictures subject to noise/blur.

2.8 Sobel Operators

The computation of the partial derivation in gradient is also approximated in digital pictures by victimization the Sobel operators that square measure shown within the masks below:

-2	-1	-2	-1	0	1
0	0	0	-2	0	2
1	2	1	-1	0	1

Fig 1: Sobel Operator

These two masks together with any of the equations are used to obtain the gradient



$$|\nabla_f| = \sqrt{G_x^2 + G_y^2} \text{ \& } |\nabla_f| = |G_x| + |G_y|$$

2.9 Canny edge detection Operator

The Canny edge detection operator was developed by John F. Canny in 1986 and uses a multi-stage formula to discover a large variety of edges in pictures. Smart technique is incredibly necessary methodology realize to seek out to search out} edges by uninflected noise from the image before finding edges of an image, while not poignant the options of the sides within the image then applying the tendency to seek out the sides and therefore, the vital’s price for threshold.

The algorithmic steps for smart edge detection technique square measure follows:

1. A Deform image with a mathematician perform to urge sleek image.
2. Apply initial distinction gradient operator to figure edge strength, then edge magnitude and direction square measure acquire as before.
3. Apply non-maximal or vital suppression to the Gradient magnitude.
4. Apply threshold of the non-maximal suppression image.

2.10 Fuzzy Edge detection

Another way to discover the edges during a digital image is to use fuzzy logic (FL). Zadeh introduced the term symbolic logic in his seminal work “Fuzzy sets,” that represented the arithmetic of fuzzy pure mathematics (1965). The Philosopher sets the inspiration for what would become symbolic logic, indicating there was a 3rd region on the far side True and False. It had been Lukasiewicz agency initial projected a scientific different to the metallic element valued logic of Aristotle.

The third value Lukasiewicz projected is best translated as “possible,” and he appointed it a numeric price between True and False. Later he explored four-valued logic and 5 valued logic, then he declared that, in essence, there was nothing to forestall the derivation of infinite-valued logic.

FL provides the chance for the modeling conditions that square measure inherently inexactly outlined. Fuzzy techniques within the variety of approximate reasoning give call support and professional systems with powerful reasoning capabilities. The temperament of blurriness within the human thought method suggests that abundant of the logic behind the thought process isn’t ancient two- valued logic or maybe multi-valued logic, however, logic with fuzzy truths, fuzzy connects, and fuzzy rules of illation [3].

The fuzzy approach is utilized in image process, particularly for edge detection. The Fuzzy image processing is the assortment of all approaches that perceive, represent and method the pictures, their segments and options as fuzzy sets. The illustration and process rely upon the chosen fuzzy technique, and on the matter to be resolved. The Fuzzy image process has 3 main stages: image fuzzification, modification of membership values and, if necessary, image defuzzification.

III. METHODOLOGY

In this section, comparative study of existing methods of corner and edge detection techniques displayed in Table 1.

Fuzzy dot i* algebra system: The general form of fuzzy dot i* algebra on region v expressed as, $\sigma = \{(\mu_\sigma(x), x \in v)\}$ and $\mu_\sigma(x) \in [-1, 1]$, is called the generalized membership function

and fuzzy set. Obviously, the generalized fuzzy set extends the normal fuzzy set.

$$\mu_\sigma(x) = \begin{cases} \sqrt{1 - \{1 + \mu_\sigma(x)\}^2}, & -1 \leq \mu_\sigma(x) \leq 0 \\ \mu_\sigma^2, & 0 \leq \mu_\sigma(x) \leq r \\ \sqrt{1 - 2\{1 + \mu_\sigma(x)\}^2}, & r \leq \mu_\sigma(x) \leq 1 \end{cases} \quad (3.1)$$

The above operator has reinforced the contrast of the two areas and broadened the domain of action of $\mu_\sigma(x)$.

The gray image X made of m x n pixels may be looked upon the same scale matrix as given below,

$$X = \sum_{i=1}^m \sum_{j=1}^n \frac{p_{ij}}{x_{ij}} = \sum_{i=1}^m \sum_{j=1}^n \hat{p}_{ij} \quad (3.2)$$

Where x_{ij} is the grayscale of pixel (I,j) with line (i) and column (j). The \hat{p}_{ij} is the degree of the grayscale of maximum and let it is denoted as

$$\hat{p}_{ij} = \left[1 + \frac{v}{d}\right]^e \quad (3.3)$$

where $v = (x_{\max} - x_{ij})$ and e & d are the exponent and reciprocals of fuzzy algebra. Based on the above factor (3.3) with 16 pixels (like SIFT method) to apply linear membership function and it is given by

$$\hat{p}_{ij} = 1 - \frac{\hat{x}}{16\hat{y}}, \quad -1 \leq p_{ij} \leq 1 \quad (3.4)$$

where $\hat{x} = x_{ij} - x_{\max}$ and $\hat{y} = x_{\max} - x_{\min}$. The x_{\min} is the gray scale of the image. The gray scale image of the two dimensional space. So we can get the fuzzy algorithm reinforced the image as X^T the gray scale x_{ij} of pixel (i,j) is X^T is

$$X^T_{ij} = x_{\max} - 16(\hat{p}_{ij} - 1)\hat{y}$$

Several feature detectors have been established and many of them are really good. But when looking for a real-time application point of view, they are not fast enough. The FDIA method is based on the Harris corner detection. The center of a circular area is employed to work out brighter and darker neighboring pixels.

However, in the case of FDIA, the whole area of the circle is not evaluated, only pixels in the discredited circle describing the segment is evaluated. Thus, for a full accelerated segment test 16 pixels have to be compared to the value of the nucleus. To prevent this extensive testing, the corner criterion uses a more relaxed approach.

A small rotation of the camera may yield pixel configurations which have not been measured in the test images. And even if all the pixel configurations are present, a small rotation about the optical axis would cause the probability distribution of the measured pixel configurations to change drastically.

This may result in an incorrect and slow corner response. To learn the probabilistic distribution of a certain scene is therefore not applicable unless only the same viewpoints and the same scene are expected. In the FDIA algorithm, the state of each pixel can be one of the possibilities.

The FAST approach which uses machine learning to address the two points. First, to create a corner detector for a given n, all of the 16 pixel rings are extracted a group of images (preferably from the target application domain).

These are labeled using a straightforward implementation of the segment test criterion for n and a convenient threshold. The FDIA assumes that the closest edge to the expected edge position is the correct match. This can lead to a large number of correspondence errors if the motion is large.

The feature detection using FDIA and machine learning approach procedures is summarized given below:

Algorithm:

- Select a group of images for training. In every image run the canny algorithm to detect the interest points by taking one pixel at a time and evaluating all the 16 pixels within the circle.
- For every pixel ‘p’, store the 16 pixels surrounding it, as a vector Repeat this for all the pixels altogether the pictures .
- Each value (one of the 16 pixels, say x) within the vector, can take three states. Darker than p, lighter than p or almost like p. Fuzzy dot i* algebra counting on the states the whole vector P.
- This order of querying which is learned from the choice tree are often used for faster detection in other images also. These algorithms exhibits high performance, but there are some limitations.

IV. RESULT

The FDIA calculation was actualized in MATLAB programming. The presentation of the FDIA is tried with pictures of various sorts incorporating both with/without uproarious (salt and pepper). The Canny edge finder is utilized for the extraction of edge focuses and holes for 1 pixel wide are filled for the location of edge highlights.

The edges in pictures with and without noise are condensed in Table 1 presentations the quantity of genuine/bogus corners distinguished alongside the preparing time. The bend and edge separated, the quantity of corners distinguished in the pictures appeared in figures 1 and 2 individually in appendix of last page.

Table. 1: Number of true/false corners detected with time taken (with and without noise)

Existing Methods	File Type	Number of Corners (without noise)		Number of Corners with noise (Added Salt and Pepper noisy)	
		Cameraman	Shape Box	Cameraman	Shape Box
Harris	$\begin{matrix} JP \\ G \end{matrix}$	160 [25] (0.03)	46 [14] (0.2) 9)	157 [27] (0.11)	48 [17] (0.08)
	$\begin{matrix} B \\ MP \end{matrix}$	159 [23] (0.06)	40 [16] (0.3) 0)	158 [24] (0.09)	55 [24] (0.08)
	$\begin{matrix} GI \\ F \end{matrix}$	161 [20] (0.07)	41 [17] (0.4) 2)	162 [22] (0.10)	40 [19] (0.07)
SUSAN	$\begin{matrix} JP \\ G \end{matrix}$	157 [24] (0.07)	45 [16] (0.2) 8)	155 [28] (0.09)	46 [18] (0.08)
	$\begin{matrix} B \\ MP \end{matrix}$	163 [21] (0.08)	38 [18] (0.2) 9)	160 [23] (0.09)	40 [19] (0.07)
	$\begin{matrix} GI \\ F \end{matrix}$	161 [19] (0.12)	40 [17] (0.3)	157 [22] (0.09)	41 [21] (0.87)

			4)		
SIFT	$\begin{matrix} JP \\ G \end{matrix}$	165 [18] (0.02)	50 [13] (0.2) 8)	161 [22] (0.08)	52 [16] (0.06)
	$\begin{matrix} B \\ MP \end{matrix}$	163 [20] (0.06)	47 [15] (0.2) 9)	160 [22] (0.08)	49 [19] (0.05)
	$\begin{matrix} GI \\ F \end{matrix}$	166 [17] (0.07)	45 [16] (0.2) 9)	161 [24] (0.08)	47 [18] (0.06)
CANNY	$\begin{matrix} JP \\ G \end{matrix}$	166 [16] (0.02)	50 [12] (0.2) 7)	165 [19] (0.07)	51 [16] (0.04)
	$\begin{matrix} B \\ MP \end{matrix}$	164 [19] (0.06)	49 [15] (0.2) 8)	164 [21] (0.06)	52 [19] (0.03)
	$\begin{matrix} GI \\ F \end{matrix}$	163 [21] (0.07)	47 [14] (0.2) 9)	161 [19] (0.08)	49 [18] (0.03)
FDIA	$\begin{matrix} JP \\ G \end{matrix}$	170 [12] (0.01)	55 [7] (0.2) 2)	168 [13] (0.06)	55 [11] (0.02)
	$\begin{matrix} B \\ MP \end{matrix}$	174 [14] (0.05)	54 [9] (0.2) 2)	171 [16] (0.05)	53 [13] (0.02)
	$\begin{matrix} GI \\ F \end{matrix}$	172 [12] (0.06)	52 [8] (0.2) 8)	171 [13] (0.07)	54 [11] (0.02)

Bold-True corners, [-] False corners, (.)Processing time (in seconds)

Table 1 shows that the proposed the FDIA method distinguishes a progressive number of genuine corners and less number of false corners when contrasted and the others existing methods like Harris, SUSAN, SIFT and Canny. Note that the genuine number of corners is 189 and 57 for the pictures cameraman and point box separately. It is observed that FDIA method beats with Harris, SUSAN, SIFT and Canny by considering the preparing time, bend and edge removed and number of genuine corners detected.

V. CONCLUSIONS

The uses of the proposed FDIA with regards to COMPUTER vision, particularly in edge based corner identification are talking about right now. Fluffy speck i* polynomial math (FDIA), a corner discovery model, has been built up which outflanks different methodology in both computational execution and repeatability. The FDIA mostly utilizes fluffy variable based math and is utilized by AI draws near. FDIA, can essentially improve its exhibition and it is joined edge based corner discovery technique. The principle highlight of FDIA is to utilize the edge focuses and their amassed data for corner discovery, for quick and increasingly precise outcomes. The exhibition of the FDIA has been considered through the analyses with genuine pictures and contrasted and Harris, SUSAN, SIFT and CANNY. It is seen that the presentation of the proposed FDIA calculation is all the more dominant when contrasted with different procedures with regards to the handling time, edge distinguished and the quantity of genuine corner recognized for the given picture. It infers that the proposed FDIA calculation is quick, dependable and can be utilized in conditions with and without clamor.



The examination uncovered that powerful estimators had not done that quite a bit of an effect in COMPUTER vision, regardless of hypothetical improvements in insights. The strategies presented right now, be useful to the specialists, who perform computer vision undertakings by considering the components, for example, clamor, computational time, ease algorithmic methodology and high dimensionality. The issue of fitting a model with loud information is as yet a difficult errand of analysts. Thus, there is an expanding requirement for hearty options rather than customary methodology, which can manage ever bigger informational collections, pictures and picture arrangements. It is recommended that it is useful to embrace and investigate the commitment of this theory with regards to AI and computer vision.

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APPENDIX





























































Methods	Image Type	Without Noise		With Noise (Added Salt and Pepper)	
		Cameraman	Angle Box	Cameraman	Angle Box
Harris	JPG				
	BMP				
	GIFF				
SUSAN	JPG				
	BMP				
	GIFF				
SIFT	JPG				
	BMP				
	GIFF				
CANNY	JPG				
	BMP				
	GIFF				
FDIA	JPG				
	BMP				
	GIFF				

Figure 1 Edge Extracted under FDIA with other procedure


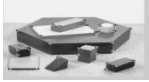





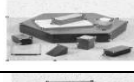





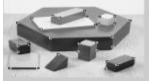



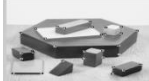

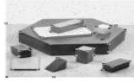

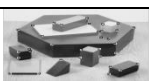































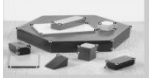





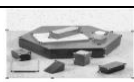
Methods		Without Noise		With Noise(Added Salt and Pepper)	
		Camerman	Angle Box	Camerman	Angle Box
Harris	JPG				
	BMP				
	GIFF				
SUSAN	JPG				
	BMP				
	GIFF				
SIFT	JPG				
	BMP				
	GIFF				
CANNY	JPG				
	BMP				
	GIFF				
FDIA	JPG				
	BMP				
	GIFF				

Figure 2: Corner detected using various procedures with FDIA